Relaxed Parameter Sharing: Effectively Modeling Time-Varying Relationships in Clinical Time-Series

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Abstract

Recurrent neural networks (RNNs) are commonly applied to clinical time-series data with the goal of learning patient risk stratification models. Their effectiveness is due, in part, to their use of parameter sharing over time (i.e., cells are repeated hence the name recurrent). We hypothesize, however, that this trait also contributes to the increased difficulty such models have with learning relationships that change over time. Conditional shift, i.e., changes in the relationship between the input X and the output y, arises when risk factors associated with the event of interest change over the course of a patient admission. While in theory, RNNs and gated RNNs (e.g., LSTMs) in particular should be capable of learning time-varying relationships, when training data are limited, such models often fail to accurately capture these dynamics. We illustrate the advantages and disadvantages of complete parameter sharing (RNNs) by comparing an LSTM with shared parameters to a sequential architecture with time-varying parameters on prediction tasks involving three clinically-relevant outcomes: acute respiratory failure (ARF), shock, and in-hospital mortality. In experiments using synthetic data, we demonstrate how parameter sharing in LSTMs leads to worse performance in the presence of conditional shift. To improve upon the dichotomy between complete parameter sharing and no parameter sharing, we propose a novel RNN formulation based on a mixture model in which we relax parameter sharing over time. The proposed method outperforms standard LSTMs and other state-of-the-art baselines across all tasks. In settings with limited data, relaxed parameter sharing can lead to improved patient risk stratification performance.

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1. Introduction

Recurrent neural networks (RNNs) capture temporal dependencies between past inputs $x_{1:t-1}$ and output y_t , in addition to the relationship between current input x_t and y_t . Their successful application to date is due in part to their explicit parameter sharing over time (Harutyunyan et al., 2019; Rajkomar et al., 2018). However, while advantageous in many settings, such parameter sharing could hinder the ability of the model to accurately capture time-varying relationships, i.e., tasks that exhibit temporal conditional shift.

In healthcare, temporal condition shift may arise in clinical prediction tasks when the factors that put a patient at risk for a particular adverse outcome at the beginning of a hospital visit differ from those that put a patient at risk at the end of their stay. Failure to recognize conditional shift when building risk stratification models could lead to temporal biases in learned models; models may capture the average trend at the cost of decreased performance at specific points in time. This could be especially detrimental to models deployed and evaluated in real time.

More formally, conditional shift refers to the change in the conditional distribution P(Y = y|X = x) across tasks. In particular, we consider temporal conditional shift, i.e., the setting in which the relationship between x and y is a function of both x and time $(y_t = f(x, t; \theta_t))$. We hypothesize that RNN's complete sharing of parameters across time steps makes it difficult to accurately model temporal conditional shift. To address this, one could jointly learn a different cell for each time step, but such an architecture may easily lead to overfitting. More importantly, such an approach does not leverage the fact that many relationships are shared, at least in part, across time.

On synthetic data, in which we can control the amount of conditional shift, we explore the trade-offs in performance between models that share parameters across time versus models that do not. Beyond synthetic data, we illustrate the presence of temporal conditional shift in real clinical prediction tasks. To tackle this issue, we propose a novel RNN framework based on a mixture approach that relaxes parameter sharing over time, without sacrificing generalization performance. Applied to three clinically relevant patient risk stratification tasks, our proposed approach leads to significantly better performance relative to a long short-term memory network (LSTM). Moreover, the proposed approach can help shed light on task relatedness across time.

Technical Significance. Our technical contributions can be summarized as follows:

- we formalize the problem setting of temporal conditional shift,
- we illustrate the presence of temporal conditional shift in three clinically relevant tasks
- we propose a novel approach for relaxed parameter sharing within an RNN framework, and
- we explore situations in which relaxed parameter sharing can help.

In theory, given enough data, RNNs should be able to accurately model relationships governed by temporal conditional shift. However, oftentimes in clinical applications, we have a limited amount of data to learn from. Going forward, researchers should check for the presence of conditional shift by comparing the proposed approach with an LSTM. If conditional shift is detected, then one may be able to more accurately model temporal dynamics through relaxed parameter sharing.

Clinical Relevance. Though tasks involving time-varying relationships are common in healthcare, current techniques rarely explicitly model temporal conditional shift. In this work, we investigate the extent to which temporal conditional shift impacts clinical prediction tasks. We consider clinical tasks involving prediction of three adverse outcomes: acute respiratory failure (ARF), shock, and in-hospital mortality during an ICU admission. These tasks were selected based on their clinical relevance. ARF contributes to over 380,000 deaths in the US per year (Stefan et al., 2013) and represents a challenging prediction task due to its multi-factorial etiology. Shock refers to the inadequate perfusion of blood oxygen to organs or tissues and can result in severe organ dysfunction and death when not recognized and treated immediately (Gaieski and Mikkelsen, 2016). Both of these conditions are upstream events that contribute to patient risk of in-hospital mortality, our third prediction task. The ability to identify patients at risk of developing ARF or shock could facilitate improved patient triage and timely intervention, preventing irreversible damage and ultimately better patient outcomes. Finally, though we consider only these three tasks, we hypothesize that time-varying risk factors may arise in other clinical prediction tasks.

2. Background & Related Work

We focus on developing techniques that can handle temporal conditional shift, a type of data shift that commonly occurs in tasks involving clinical time-series data. There are two main types of data shift: i) covariate shift and ii) conditional shift. Covariate shift is the scenario where P(X=x) varies across datasets (Reddi et al., 2015; Sugiyama et al., 2007), e.g., the distributions of patient demographics may differ across study populations. In contrast, conditional shift, our main focus, occurs when P(Y=y|X=x) changes (Zhang et al., 2013; Gong et al., 2016), e.g., two hospitals may have similar patient populations, but different factors could drive patient risk due to differences in clinical protocols. In conditional shift, the relationship between input x and output y has shifted. This can occur independently of a change in population. For some time, the study of data shift has driven research in the fields of domain adaptation, transfer learning, and multitask learning (Daumé III, 2007; Pan and Yang, 2010; Ding et al., 2017; Thiagarajan et al., 2018).

Methods for dealing with conditional shift are largely driven by the problem setting. Researchers have explored the use of pre-trained features (Sharif Razavian et al., 2014), generalizable representations (Glorot et al., 2011; Zhuang et al., 2015), and applying importance re-weighting techniques (Zhang et al., 2013). In contrast to these works, we focus on techniques for tackling conditional shift in which the shift is driven by changes in time. In this setting, there is no clear distinction between tasks, because the change occurs gradually. Though related, this differs from 'data drift' (i.e., the setting in which relationships change longitudinally) since we consider time on a local/relative scale as opposed to a global/absolute scale (dos Reis et al., 2016; Soemers et al., 2018). That is, instead of focusing on differences between 2018 and 2019, we focus on changes within an admission or a patient. Though such local shift is expected to occur (Bellera et al., 2010; Dekker et al., 2008), it is often overlooked when modeling patient risk.

In the linear setting, past work has explored the use of multitask learning to model the temporal evolution of risk factors within a patient admission, where each day corresponds to a different model, but models are learned jointly (Wiens et al., 2016). Related, Dekker

et al. (2008) proposed a variation to Cox regression analysis, studying different time windows separately and using time specific hazard ratios.

Nonlinear methods designed to explicitly deal with temporal conditional shift have more recently been explored, focusing primarily on modifications to RNN architectures (Ha et al., 2017; Park and Yoo, 2017), especially LSTMs. For example, Ha et al. (2017) proposed an extension to LSTMs, Hypernetwork, that relaxes parameter sharing by learning an auxiliary network that sets the primary network's parameters at each time step. Specifically, the auxiliary network can change the primary network's parameters through a scalar multiplier. Similar to Hypernetworks, we also consider a variation on the LSTM, in part because LSTMs are commonly applied to clinical time-series (Fiterau et al., 2017; Lipton et al., 2016; Harutyunyan et al., 2019). However, in contrast to previously proposed modifications for handling conditional shift, we impose fewer restrictions on how parameters can be modified at each time step.

Mixture of experts models are commonly used for multitask learning and conditional computation (Kohlmorgen et al., 1998; Ma et al., 2018; Wang et al., 2018; Eigen et al., 2014; Tan et al., 2016; Savarese and Maire, 2019). By framing conditional shift as a multitask problem, we can exploit the large body of work in mixture of experts. Kohlmorgen et al. (1998) proposed a two-step approach in which first, a hidden Markov model (HMM) learns a segmentation of the time series, so that each segment is assigned to an expert, and second, the learned experts are mixed at the segmentation boundaries. Eigen et al. (2014) stacked experts to form a deep mixture of experts; Tan et al. (2016) mixed the parameters of fully connected layers, stacking them to account for differences in the training and test sets in audio processing tasks; and Ma et al. (2018) learned a gating function to mix the output of experts in a multitask learning setting. The methods proposed by Savarese and Maire (2019) are particularly related. The authors learn coefficients for mixing convolution parameters, increasing parameter sharing across layers of a convolutional neural network (CNN). Building on these approaches, we investigate the utility of a mixture of LSTMs. At each time step, we apply the learned mixing coefficients to form a combined LSTM cell. This facilitates end-to-end learning and allows more than two experts to flexibly contribute to any time step's prediction. Our setting differs from Savarese and Maire (2019) as the mixing coefficients are a) constrained to belong to a simplex, b) learned for each time step instead of each layer, and c) applied to LSTM cells instead of CNN filters.

3. Methods

In this section, we describe extensions to LSTMs that facilitate learning in the presence of temporal conditional shift. Building off of an LSTM architecture, we present two variations that relax parameter sharing across time: shiftLSTM and mixLSTM. The first approach, shiftLSTM, represents a simple baseline in which different parameters are learned for different time steps (i.e., separate LSTM cells for different time periods). The second approach, mixLSTM, addresses the shortcomings of this simple baseline through a mixture approach. But first, we formalize the problem setting of temporal conditional shift and review the architecture of an LSTM.

3.1. Problem Setup - Temporal Conditional Shift & LSTMs

Given time-series data representing patient covariates over time, $\mathbf{X} = [\mathbf{x}_1, \mathbf{x}_2, ..., \mathbf{x}_T]$ where $\mathbf{x}_t \in \mathbb{R}^d$, we consider the task of predicting a sequence of outcomes $\mathbf{y} = [y_1, y_2, ..., y_T]$, where $y_t \in \mathbb{R}$ for $t \in [1, 2, 3, ..., T]$. We consider a scenario in which the relationship between $\mathbf{x}_{1:t}$ and y_t varies over time, i.e., $y_t = f(\mathbf{x}_{1:t}, t; \boldsymbol{\theta}_t)$, where $\boldsymbol{\theta}_t$ represent model parameters at time t. Because t is measured with respect to a patient-specific fiducial marker, we restrict ourselves to conditional shift within a patient-specific time scale (e.g., within an admission).

In the sequence-to-sequence setting described above, LSTMs take as input time-varying patient covariates and output a prediction at each time step. Dynamics are captured in part through a cell state C_t that is maintained over time. A standard LSTM cell is described below, where * represents element-wise multiplication. Here, h_t and \tilde{C}_t represent the hidden state and the update to the cell state, respectively.

$$i_t = \sigma(\mathbf{W}_i[\mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_i) \tag{1}$$

$$\tilde{\boldsymbol{C}}_t = \tanh(\boldsymbol{W}_{\tilde{\boldsymbol{c}}}[\boldsymbol{h}_{t-1}, \boldsymbol{x}_t] + \boldsymbol{b}_{\tilde{\boldsymbol{c}}})$$
(2)

$$\mathbf{f}_t = \sigma(\mathbf{W}_f[\mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_f) \tag{3}$$

$$C_t = i_t * \tilde{C}_t + f_t * C_{t-1} \tag{4}$$

$$o_t = \sigma(W_o[h_{t-1}, x_t] + b_o) \tag{5}$$

$$\boldsymbol{h}_t = \boldsymbol{o}_t * \tanh(\boldsymbol{C}_t) \tag{6}$$

$$\hat{y}_t = \mathbf{W}_y \mathbf{h}_t + b_y \tag{7}$$

Importantly, each of the learned parameters W and b in equations (1)-(3), (5) and (7) do not vary with time. To capture time-varying dynamics, the hidden and cell states (h_t , C_t) must indirectly model conditional shift.

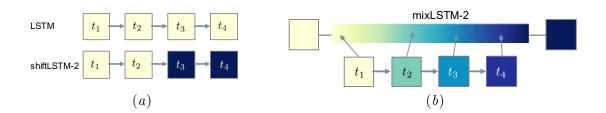


Figure 1: An illustrative plot comparing LSTM, shiftLSTM, and mixLSTM, with four time steps. Each square denotes an LSTM cell. Cells with the same color share the same parameters. Arrows denote transitions between time steps. (a) shiftLSTM-2 is similar to an LSTM, except it uses different cells for the first two time steps compared to the last two. (b) mixLSTM-2 has two independent underlying cells, and at each time step, it generates a new cell by mixing a convex combination of the underlying cells. For illustrative purposes, the parameters at each time step are drawn from sequential locations on the continuum, but in reality, the parameter combination is independent of the relative positions of time steps.

3.2. Relaxed Parameter Sharing in LSTMs

We hypothesize that in settings where the amount of training data is limited – this is often the case in health applications – an approach that more directly models conditional shift through time-varying parameters will outperform a standard LSTM. To this end, we explore two variations on the LSTM: the shiftLSTM and the mixLSTM, illustrated in Figure 1.

3.2.1. SHIFTLSTM - LEARNING ABRUPT TRANSITIONS

As a baseline, we consider an approach that naïvely minimizes parameter sharing across cells, by learning different parameters $W^{(t)}$ and $b^{(t)}$ at each time step t, instead of the time-invariant parameters in equations (1)-(3), (5), and (7). This mimics a feed-forward network, with the hidden state and cell state propagating forward at each time step, but computes the output sequentially. This naïve approach to relaxed parameter sharing assumes no shared relationships across time. As a result, its capacity is significantly greater than that of an LSTM. Given the same hidden state size, the number of parameters scales linearly with the number of time steps. We hypothesize that this naïve approach will result in overfitting and poor generalization, in settings with limited data. To strike a balance between the two extremes, complete sharing and no sharing, we explore a variation of this approach that assumes parameters are shared across a subset of adjacent time steps: shiftLSTM-K.

shiftLSTM-K. This approach sequentially combines K different LSTM cells over time, resulting in different model parameters every $\lceil T/K \rceil$ time steps (**Figure 1a**). $K \in \{1, ..., T\}$ is a hyperparameter, with shiftLSTM-1 being no different than an LSTM with complete parameter sharing, and shiftLSTM-T corresponding to different parameters at each time step. All parameters are learned jointly using backpropagation.

3.2.2. MIXLSTM - LEARNING SMOOTH TRANSITIONS

As described above, the shiftLSTM approach is restricted to sharing parameters within a certain number of contiguous time steps. This not only leads to a substantial increase in the number of parameters, but also results in possibly abrupt transitions. We hypothesize that changes in health data, and risk factors specifically, are gradual. To allow for smooth transitions in time, we propose a mixture-based approach: mixLSTM-K (Figure 1b).

mixLSTM-K. Given K independent LSTM cells with the same architecture, let $\mathbf{W}^{(k)}$ and $\mathbf{b}^{(k)}$ represent the k^{th} model's weight parameters from equations (1)-(3), (5) and (7). The parameters of the resulting mixLSTM at time step t are

$$\mathbf{W}_{t} = \sum_{k=1}^{K} \lambda_{t}^{(k)} \mathbf{W}^{(k)}, \qquad \mathbf{b}_{t} = \sum_{k=1}^{K} \lambda_{t}^{(k)} \mathbf{b}^{(k)}$$
 (8)

where $\lambda = \{\lambda_t^{(k)}: t=1\dots T, \ k=1\dots K\}$ are the mixing coefficients and each $\lambda_t^{(k)}$ represents the relevance of the k^{th} model for time step t. The mixing coefficients are learnable parameters (initialized randomly) and are constrained such that $\sum_k \lambda_t^{(k)} = 1$ and $\lambda_t^{(k)} \geq 0$. Similar to above, K is also a hyperparameter, but here it can take on any positive integer value. Note that for every K, all possible shiftLSTM-K models can be learned by mixLSTM-K.

By mixing models, instead of abruptly transitioning from one model to another, mixLSTM can learn to share parameters over time. Moreover, though we do not constrain the mixing coefficients to change smoothly, their continuous nature allows for smooth transitions. We verify these properties in our experiments.

4. Experimental Setup

We explore the effects of temporal conditional shift in both synthetic and real data. Here, we describe i) these datasets, ii) several baselines to which we compare our proposed approach, and iii) the details of our experimental setup.

4.1. Synthetic Data

We begin by considering a scenario in which we can control the extent of conditional shift in the problem. This allows us to test model performance in a setting where the amount of temporal conditional shift is known. Specifically, we consider a multitask variation of the 'copy memory task' (Arjovsky et al., 2016), with input sequence $\{x_1, \ldots, x_T\}, x_t \in \mathbb{R}^d$, and output sequence $\{y_{l+1},\ldots,y_T\},\ y_t\in\mathbb{R}$ (we start generating output once we have accumulated l values). The output at each time step is some predetermined, weighted combination of inputs from the previous l time steps, described by two probability vectors, $w_t^{(l)} \in \mathbb{R}^l$ and $w_t^{(d)} \in \mathbb{R}^d$, which are used for weighting the l time steps and d feature dimensions respectively. The parameters change gradually at every time step t, such that each time step's weighting (or task) is similar to the task from the previous time step. The parameter δ controls amount of change between temporally adjacent tasks. The generation process of these parameters is described below, followed by the generation process of the datasets. Here, $[x_{t-l}, \dots, x_{t-1}]^{\mathsf{T}} \in \mathbb{R}^{l \times d}$ is the concatenation of the previous l inputs at time step t. Inputs are generated to be sparse. Renormalize(v) refers to a renormalization process that ensures the weights in every w_t vector are positive and sum to 1. This is done every time step to ensure that the effect of δ does not diminish as t increases.

```
Procedure SampleData(T, w_{l+1:T}^{(l)}, w_{l+1:T}^{(d)}):
Procedure SampleWeights (T, l, m):
       w_{l+1} \sim \text{Uniform}(0,1) \in \mathbb{R}^m
                                                                                                   for t \in \{1, ..., T\}, i \in \{1, ..., d\} do
       w_{l+1} = \texttt{Renormalize}(w_{l+1})
                                                                                                         z_i \sim \text{Bernoulli}(0.1) \# \text{ for sparse inputs}
      for t \in \{l + 2, ..., T\} do
                                                                                                         x_i \sim \text{Uniform}(0, 100)
             \Delta_t \sim \text{Uniform}(-\delta, \delta) \in \mathbb{R}^m
                                                                                                      x_t[i] = z_i x_i
            w_t = \mathtt{Renormalize}(w_{t-1} + \Delta_t)
                                                                                                   end
                                                                                                  \begin{array}{l} \mathbf{for} \ t \in \{l+1, \dots, T\} \ \mathbf{do} \\ \big| \ \ y_t = w_t^{(l)^\intercal} \big[ \boldsymbol{x}_{t-l}, \dots, \boldsymbol{x}_{t-1} \big]^\intercal w_t^{(d)} \\ \mathbf{end} \end{array}
       end
      return w_{l+1}, \ldots, w_T
\begin{aligned} w_{l+1}^{(d)}, \dots, w_{T}^{(d)} &= \mathtt{SampleWeights}(T, l, d) \\ w_{l+1}^{(l)}, \dots, w_{T}^{(l)} &= \mathtt{SampleWeights}(T, l, l) \end{aligned}
                                                                                                   return \{x_1, ..., x_T\}, \{y_{l+1}, ..., y_T\}
```

Our goal is then to learn to predict $\{y_{l+1}, \ldots, y_T\}$ based on input from the current and all preceding time steps. For each $\delta \in \{0.0, 0.1, 0.2, 0.3, 0.4\}$, we generated five sets of temporal weights, and then used each set to create five different synthetic dataset tasks where T = 30, d = 3, and l = 10. These twenty-five tasks were kept the same throughout experiments involving synthetic data. Train, validation and test sets all had size N = 1,000 unless otherwise specified.

4.2. Clinical Prediction Tasks

In addition to exploring conditional shift in synthetic data, we sought to test our hypotheses using real clinical data from MIMIC-III (Johnson et al., 2016). Below we describe the three clinical prediction tasks of interest, in addition to their corresponding study populations, patient covariates, and evaluation criteria.

4.2.1. Outcomes

Throughout the first 48 hours of each ICU visit, we sought to make predictions regarding a patient's risk of experiencing three different outcomes: acute respiratory failure (ARF), shock, and in-hospital mortality, each described in turn below.

ARF. Acute respiratory failure is defined as the need for respiratory support with positive pressure mechanical ventilation (Stefan et al., 2013; Meduri et al., 1996). Onset time of ARF was determined by either the documented receipt of invasive mechanical ventilation (ITEMID: 225792) or non-invasive mechanical ventilation (ITEMID: 225794) as recorded in the PROCEDURESEVENTS_MV table, or documentation of positive end-expiratory pressure (PEEP) (ITEMID: 220339) in the CHARTEVENTS table, whichever occurs earlier. Ventilator records and PEEP settings that are explicitly marked as ERROR did not count as an event.

Shock. Shock is defined as inadequate perfusion of blood oxygen to organs or tissues (Gaieski and Mikkelsen, 2016), and is characterized by receipt vasopressor therapy. Onset time of shock was determined by the earliest administration of vasopressors (Avni et al., 2015). Using the INPUTEVENTS_MV table, we considered the following vasopressors:

- norepinephrine (ITEMID: 221906),
- epinephrine (ITEMID: 221289),
- dopamine (ITEMID: 221662),
- vasopressin (ITEMID: 222315), and
- phenylephrine (ITEMID: 221749).

Drug administration records with the status of REWRITTEN, incorrect units, or non-positive amounts/durations did not count towards an event.

In-hospital mortality. As in Harutyunyan et al. (2019), the time of in-hospital mortality was determined by comparing patient date of death (DOD column) from the PATIENTS table with hospital admission and discharge times from the ADMISSIONS table.

4.2.2. Cohort Selection

We considered adult admissions with a single, unique ICU visit. This excludes patients with transfers between different ICUs. Patients without labels or observations in the ICU were excluded. Since we are interested in how relationships between covariates and outcome change over time, we focused our analysis on patients who remained in the ICU for at least 48 hours. In addition, for ARF and shock prediction tasks, patients who experienced the event of interest before 48 hours were excluded. Using the full 48 hours allows us to focus on temporal trends that are more likely to be present in longer visits. **Table 1** shows the number of admissions and positive labels for the three tasks after applying exclusion criteria.

Table 1: We considered three clinical prediction tasks. The study population varied in size across tasks, as did the fraction of positive cases (i.e., the portion of patients who experienced the outcome of interest.)

Task	Number of ICU admissions (%positive)
ARF	3,789 (6.01%)
shock	5,481 (5.98%)
in-hospital mortality	$21,139 \ (13.23\%)$

4.2.3. Data Extraction and Feature Choices

We used the same feature extraction procedure as detailed in Harutyunyan et al. (2019)¹. For completeness, we briefly describe the feature extraction process here. For each ICU admission, we extracted 17 physiological features (e.g., heart rate, respiratory rate, Glasgow coma scale, see **Table 4** in Appendix A) from the first 48 hours of their ICU visit. We applied mean normalization for continuous values and mapped categorical values to binary features using one-hot encoding, resulting in 59 features. We resampled the time series with a uniform sampling rate of once per hour with carry-forward imputation. Mask features, indicating if a value had been imputed resulted in 17 additional features. After preprocessing, each example was represented by d = 76 time-series (see **Table 5** in Appendix A for the complete list of features) of length T = 48 and three binary labels indicating whether or not the patient developed ARF, developed shock or died during the remainder of the hospital stay.

4.2.4. EVALUATION

Given these data, the goal was to learn a mapping from the features to a sequence of probabilities for each outcome: ARF, shock or in-hospital mortality. We split the data into training, validation, and test as in Harutyunyan et al. (2019). We used target replication when training the model (Lipton et al., 2016). For example, if a patient eventually developed ARF, then every hour of the first 48 hours is labeled as positive (negative otherwise). We used the validation set for hyperparameter tuning, and report model performance as evaluated on the held-out test set. Since we consider a sequence-to-sequence setting, each model makes a prediction for every hour during the first 48 hours. These predictions were evaluated based on whether or not at least one prediction exceeds a given threshold. This threshold was swept across all ranges to generate a receiver operating characteristics curve (ROC) and precision-recall curve (PR). This resembles how the model is likely to be used in practice. With the goal of making early predictions, as soon as the real-time risk score exceeds some specified threshold, clinicians could be alerted to a patient's increased risk of the outcome. It should be noted that this differs from the evaluation used in Harutyunyan et al. (2019) where a single prediction was made during the 48-hour period. We report performance in terms of the area under the ROC and PR curves (AUROC, AUPR), computing 95% confidence intervals using 1,000 bootstrapped samples of the test set.

^{1.} https://github.com/YerevaNN/mimic3-benchmarks

4.3. Baselines for Comparison

In addition to the approaches with relaxed parameter sharing described in the Section 3, we considered a number of baselines, which are described below.

NN. A non-recurrent, feed-forward neural network with one hidden layer. The same network is applied *independently* at every time step to generate the prediction for that time step. This model has complete parameter sharing but no recurrent structure to capture temporal dynamics, and thus is a simpler model than LSTMs and less likely to overfit. This model serves as a simple baseline, but highlights the complexity of the tasks in terms of temporal dynamics.

NN+t. Similar to NN but with an additional input feature $\hat{x}_t = \frac{t}{T} \in \mathbb{R}$ at every time step, representing the relative temporal position. Given time as an input, this model has the capacity to model temporal conditional shift but cannot leverage longitudinal trends.

LSTM. We considered a standard LSTM in which parameters are completely shared across time. Synthetic tests used the default Pytorch v0.4.1 implementation (torch.nn.LSTM()). In our experiments on the clinical data, we implemented an LSTM that employed orthogonal parameter initialization and layer normalization, in order to match the settings used in the original HyperLSTM implementation (see below).

LSTM+t. shiftLSTM and mixLSTM intrinsically have an additional signal regarding the current time step (captured through the use of time-specific parameters). In order to test whether this was driving differences in performance, we tested LSTM+t, an LSTM with an additional input feature $\hat{x}_t = \frac{t}{T} \in \mathbb{R}$ at every time step, representing the relative temporal position.

LSTM+TE. Given that positional encoding has recently been shown to provide an advantage over simply providing position (Vaswani et al., 2017), we also explored adding a temporal encoding as additional input features. We used a 24-dimensional encoding for each time step. We tested encoding sizes of 12, 24, 36 and 48 on the in-hospital mortality task, and found 24 to result in the best validation performance. We calculated the temporal encoding as: $TE_{(t,i)} = \sin\left(\frac{t}{10000^{i/24}}\right)$ if i is even, and $TE_{(t,i)} = \cos\left(\frac{t}{10000^{(i-1)/24}}\right)$ if i is odd, where t represents the time step and i the position in the encoding indexed from 0.

HyperLSTM. First proposed by Ha et al. (2017), this approach uses a smaller, auxiliary LSTM to modify the parameters of a larger, primary LSTM at each time step. Since the parameters at each time step are effectively different, this is a form of relaxed parameter sharing. As in the original implementation, we used orthogonal parameter initialization and layer normalization. The two networks were trained jointly using backpropagation.

4.4. Model Training & Implementation Details

The two non-LSTM baselines both used one hidden layer with ReLU activation and a softmax nonlinearity at the output layer. Except in the case of the LSTM applied to synthetic data, LSTM models consisted of single-layer recurrent cells that were orthogonally initialized followed by a fully-connected layer and a softmax nonlinearity. For experiments involving synthetic data, to compensate for the lower capacity of the LSTM compared to mixLSTM and shiftLSTM which have multiple cells, we allowed it to use an additional layer. Capacity was less of an issue in the experiments involving real data. We tuned the size of the hidden state(s) in all methods based on validation performance.

We trained all models using the Adam optimizer (Kingma and Ba, 2015) (Pytorch implementation) with the default learning rate of 0.001. On synthetic data we aimed to minimize the mean squared error (MSE) loss, and for the clinical prediction tasks, we aimed to minimize the cross entropy loss with target replication. We used early stopping based on validation performance – MSE loss on synthetic data tasks, AUROC on real data tasks - with a patience of 5 epochs. Models for synthetic datasets were trained with 40 random initializations/hyperparameter settings for a maximum of 30 epochs. We used a batch size of 100 and performed a random search over hidden state sizes of {100, 150, 300, 500, 700, 900, 1100. For learning models on clinical tasks, we used a batch size of 8, because it was the optimal LSTM batch size setting used in the MIMIC-III benchmark paper on the in-hospital mortality task (Harutyunyan et al., 2019). When learning models for ARF and shock, we considered 20 random initializations, and trained for a maximum of 30 epochs. For LSTM models, we performed a random search over hidden state and auxiliary hidden states sizes of {25, 50, 75, 100, 125, 150}; for NN and NN+t, we performed a random search over the number of hidden units in $\{25, 50, \ldots, 1000\}$. When learning models for in-hospital mortality, we considered 10 random initializations and trained for a maximum of 10 epochs, in part because of the larger training set size. For LSTM models on this task, we performed a random search over hidden state size {100, 150, 300, 500, 700} and the same auxiliary hidden state size search as for ARF and shock; for NN and NN+t, we considered the same range of hyperparameters as for ARF and shock. To facilitate comparisons, the code for all of our experiments is publicly available online².

5. Results & Discussion

In this section, we first show that as temporal conditional shift increases, the performance of the LSTM decreases. Next, we provide evidence that suggests that conditional shift exists in the three clinical prediction tasks. Then, on both the synthetic and real datasets, we show that the proposed method consistently outperforms the baselines. Finally, we present a follow-up analysis focusing on the patterns by which mixLSTM learns to mix the parameters, and the robustness of mixLSTM when training data are limited.

 $^{2.\} https://gitlab.eecs.umich.edu/MLD3/MLHC2019_Relaxed_Parameter_Sharing$

5.1. Exploring the Effects of Temporal Conditional Shift

Does parameter sharing hinder the ability of an LSTM to capture time-varying relationships? The data generation process described in Section 4.1 allows us to control the amount of temporal conditional shift present in the task. Specifically, by increasing δ , we increase the variability between two temporally adjacent tasks. This allows us to test the effects of conditional shift on the performance of an LSTM. We hypothesize that because the LSTM shares parameters over time, it will struggle to adapt to temporal conditional shift. To test our hypothesis, we compare the performance of an LSTM with shiftLSTM across a range of δ values (Figure 2a). Here, the shiftLSTM approach learns different sets of parameters for each time step (30 in total). We observe a clear trend: as temporal conditional shift increases, the performance of the LSTM decreases. In contrast, shiftLSTM results in steady performance across the range of δ . At low $\delta \in \{0,0.1\}$, the LSTM outperforms the shiftLSTM in terms of MSE on the test set. In this experiment, we limited the amount of training data to 1,000 samples. Theoretically, given enough training data, LSTM should be capable of accurately modeling time-varying relationships. To verify this, we show that the test loss associated with the LSTM models approaches zero as the training set size increases (Figure 2b). These results support our initial hypothesis that in settings with limited data, temporal conditional shift negatively impacts LSTM performance and that this impact is in part due to the sharing of parameters.

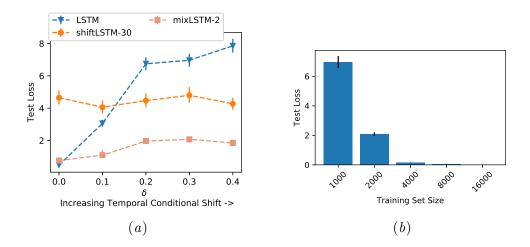


Figure 2: (a.1): LSTM performance decreases as conditional shift increases. With increasing conditional shift, the time-varying architecture outperforms the LSTM, suggesting that parameter sharing hurts LSTM performance. (a.2) mixLSTM bridges the performance tradeoff between LSTM and shiftLSTM. As conditional shift increases, mixLSTM's ability to relax parameter sharing helps it increasingly outperform LSTM. By assuming that tasks are unique but related it outperforms shiftLSTM. (b) This issue is only apparent when training data are limited; LSTMs can adapt to temporal conditional shift given enough training data. Error bars represent 95% confidence intervals based on bootstrapped samples of the test set. δ was set to 0.3.

Is there any evidence of time-varying relationships in the three clinical prediction tasks of interest? We tested for the presence of temporal conditional shift in three clinical prediction tasks: ARF, shock, and in-hospital mortality. For these tasks, the underlying parameters that govern the amount of temporal conditional shift (e.g., δ) are unknown. Instead, we indirectly measure temporal conditional shift by applying shiftLSTM-K varying K from $\{1, 2, 3, 4, 8, 48\}$, where K = 1 is a standard LSTM, and K = 48 implies a different set of parameters for each time step. Increasing the number of cells or K reduces sharing. As the difference between sequential tasks increases, we expect the benefit of learning different LSTM cells (less parameter sharing) to increase. Empirically, we observe that less parameter sharing results in better performance (**Figure** 3). This supports our hypothesis that architectures for solving clinical prediction tasks could benefit from relaxed parameter sharing.

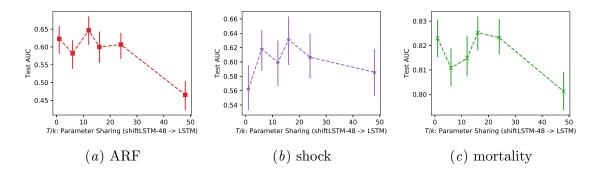


Figure 3: As we increase parameter sharing by increasing T/K along the x-axis, there is a drop in performance, supporting our hypothesis that temporal conditional shift is present in our real data tasks. Error bars represent the interquartile ranges based on bootstrapped samples of the test set.

5.2. Comparing the Proposed Approach to Baselines

In this section, we explore the performance of the proposed approach, mixLSTM, relative to the other baselines. Again, we hypothesize that it will outperform the other approaches due to a) smooth sharing of parameters and b) the ability to learn which cells to share. mixLSTM strikes a balance between complete parameter sharing (LSTM) and no parameter sharing (shiftLSTM-48). In addition, compared to shiftLSTM, mixLSTM can share parameters between distant time steps and learns how to accomplish this.

How does the proposed approach perform on synthetic data? mixLSTM has the ability to continuously interpolate between K independent cell parameters. In this instance, mixLSTM-2 has 15 times fewer parameters relative to shiftLSTM-30. On the synthetic data tasks, mixLSTM consistently outperforms shiftLSTM at all levels of temporal shift (Figure 2a). Moreover, mixLSTM outperforms LSTM at low δ , except when no temporal shift exist. This agrees with our intuition that smart sharing is better than no sharing (shiftLSTM) and indiscriminate sharing (LSTM).

Table 2: Performance on ARF, shock, & mortality with 95% confidence intervals. Though the differences are small, mixLSTM consistently outperforms the other approaches across all tasks in terms of both AUROC and AUPR. The number of test samples for each task is reported in parentheses.

Model	ARF (n=549)		shock (n=786)		mortality (n=3.236)	
Model	AUROC	AUPR	AUROC	AUPR	AUROC	AUPR
NN	0.57 [0.45, 0.67]	0.05 [0.03, 0.10]	0.60 [0.52, 0.68]	0.08 [0.05, 0.12]	0.80 [0.77, 0.82]	0.39 [0.34, 0.44]
NN+t	0.58 [0.46, 0.68]	0.06 [0.03, 0.11]	0.56 [0.47, 0.64]	0.10 [0.05, 0.19]	0.79 [0.77, 0.82]	0.38 [0.33, 0.43]
LSTM	0.47 [0.35, 0.58]	0.04 [0.02, 0.07]	0.59 [0.49, 0.69]	0.09 [0.05, 0.16]	0.80 [0.78, 0.83]	0.39 [0.33, 0.43]
LSTM+t	0.42 [0.30, 0.54]	0.04 [0.02, 0.07]	0.62 [0.53, 0.70]	0.08 [0.05, 0.15]	0.81 [0.79, 0.83]	0.41 [0.36, 0.47]
LSTM+TE	0.48 [0.35, 0.61]	0.05 [0.03, 0.10]	0.60 [0.50, 0.69]	0.10 [0.06, 0.20]	0.82 [0.80, 0.85]	0.43 [0.38, 0.48]
HyperLSTM	0.57 [0.44, 0.68]	0.06 [0.03, 0.10]	0.63 [0.54, 0.72]	0.08 [0.05, 0.12]	0.82 [0.80, 0.84]	0.42 [0.37, 0.47]
shiftLSTM	0.61 [0.49, 0.70]	0.10 [0.03, 0.21]	0.61 [0.52, 0.70]	0.09 [0.05, 0.16]	0.81 [0.79, 0.84]	0.43 [0.37, 0.48]
mixLSTM	0.72 [0.62, 0.80]	0.15 [0.06, 0.27]	0.67 [0.58, 0.76]	0.10 [0.06, 0.16]	0.83 [0.81, 0.85]	0.45 [0.40, 0.50]

How does the proposed approach perform on the clinical prediction tasks? Applied to the three clinical prediction tasks (with varying amounts of training data), mixLSTM consistently performs the best (Table 2). The NN and NN+t models are simpler architectures that outperform other LSTM-based baselines only under very low data settings (ARF). Compared to the LSTM baseline, LSTM+t and LSTM+TE performed better given sufficient training data, suggesting that having direct access to time either as a feature or a temporal encoding is beneficial. Relaxing parameter sharing further improves performance. As shown earlier, shiftLSTM consistently improves performance over the standard LSTM.

HyperLSTM, similar to mixLSTM, bridges the dichotomy of completely shared and completely independent parameters, and outperforms both LSTM and shiftLSTM in some cases but not consistently. mixLSTM outperforms all other baselines on all three tasks, though the differences are not statistically significant in all cases. Both HyperLSTM and mixLSTM achieve high performance and both models relax parameter sharing. This supports our hypothesis that relaxed parameter sharing is beneficial in some settings.

In these experiments, we selected K for each task based on validation performance, testing $K \in \{2,3,4,8,48\}$ for shiftLSTM and sweeping K from 2 to 4 for mixLSTM. For shiftLSTM, K represents the optimal number of sequential tasks to segment the input sequence into; the best K=2,2,8 for ARF, shock, and mortality respectively. For mixLSTM, K indicates the optimal number of operational or characteristic modes in the data; the best K=4,4,2, respectively. It appears that for shiftLSTM, the chosen K is correlated with the amount of training data available. Both ARF and shock have significantly smaller training set sizes compared to mortality. In contrast, mixLSTM learns more cells for ARF and shock. This suggests that the structure of mixLSTM is better suited to the problem setting than shiftLSTM, since it is able to train twice as many cells as shiftLSTM and attain a higher test performance. The converse also supports this claim. mixLSTM is able to train $\frac{1}{4}$ the number of cells as shiftLSTM for mortality and still attain better performance. The optimal K for mixLSTM appears to be less indicative of training set size, and more a reflection of the true number of operational or characteristic modes in the data. When we visualize the mixing ratios learned by mixLSTM-2 in later sections (Figure 5) we see that while mortality smoothly interpolates between cell1 and cell2 as time passes, ARF and shock both display an initial peak followed by a gradual interpolation. This suggests that the dynamics are more complex for ARF and shock.

5.3. Robustness and Sensitivity Analyses

In this section, we further analyze mixLSTM, focusing on its robustness in settings when training data are limited and investigate what it has learned in terms of mixing trends and changing feature importance.

5.3.1. Performance with Limited Training Data

Does the proposed approach still perform well when training data are limited? We hypothesized that mixLSTM will continue to outperform LSTM, even when training data are limited because mixLSTMs are better suited to problem settings exhibiting temporal conditional shift. To test our hypothesis, we compared the performance of mixLSTM-2 and LSTM trained using different training set sizes for the task of predicting in-hospital mortality. We chose to focus on the task of in-hospital mortality, since it had the most training data (training set size = 14,681). We subsampled the training set repeatedly for $N \in \{250, 500, 2000, 5000, 8000, 11000\}$. The test set was held constant across all experiments and K = 2 to limit the capacity of the model. mixLSTM consistently outperforms LSTM across all ranges of training set sizes (Figure 4). As one might expect, differences are subtle at smaller training set sizes, where an LSTM with complete parameter sharing is likely more sample efficient and therefore more competitive.

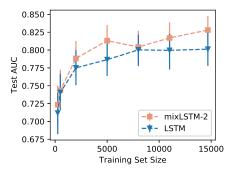


Figure 4: mixLSTM-2 is consistently better than LSTM at different training set sizes. Error bars represent 95% confidence intervals bootstrapped from the test set.

5.3.2. What has mixLSTM learned?

To dive deeper into what exactly the mixLSTM has learned, we visualize the learned mixing coefficients and the most important features.

Are mixLSTM's learned mixing coefficients smooth? In our learning objective function, mixLSTM's mixing coefficients are not constrained to be smooth. However, we hypothesize that this behavior reflects the underlying dynamics in clinical data. Figure 5 plots the mixing coefficients ($\lambda^{(1)}$) over time for mixLSTM-2 on the three clinical prediction tasks. Since there are only two independent cells (K = 2), we can infer $\lambda^{(2)} = 1 - \lambda^{(1)}$. The trend indicates that one cell captures the dynamics associated with the beginning of a patient's stay, while the second cell captures the dynamics 48 hours into the stay.

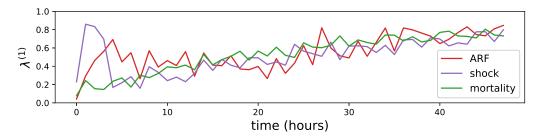


Figure 5: Visualization of the mixing coefficients learned by mixLSTM-2. $\lambda^{(1)}$ is shown on the y-axis, while $\lambda^{(2)}$ can be inferred ($\lambda^{(2)} = 1 - \lambda^{(1)}$). Although not constrained to be smooth, we observe a smooth transition of mixing coefficients between time steps, indicating that one cell is specialized for the beginning of a patient's ICU stay while the other is specialized for 48 hours into the ICU stay.

Does explicitly smoothing the mixing coefficients help? Based on patterns displayed in Figure 5, we hypothesized that additional smoothing of the mixing coefficients could aid classification performance. To test this hypothesis, we applied regularization based on a similarity measure between models at consecutive time steps. Following Savarese and Maire (2019), we used the normalized cosine similarity as the similarity measure. For consecutive time steps t and t+1, this similarity score is $s_t = \frac{\langle \lambda_t, \lambda_{t+1} \rangle}{\|\lambda_t\|_2 \|\lambda_{t+1}\|_2}$ where $\lambda_t := [\lambda_t^{(1)}, \dots, \lambda_t^{(K)}]$. Denoting \mathcal{L} as the original loss function and $\alpha \in \mathbb{R}^+$ as the regularization strength, we minimize the regularized objective $\mathcal{L}_R := \mathcal{L} - \alpha \sum_{t=1}^{T-1} s_t$ to encourage temporal smoothness.

Figure 6 illustrates the effect of temporal smoothness regularization on the model for the mortality task. As expected, larger regularization strength encourages models to share parameters. However, test performance drops monotonically as α increases. Additional regularization likely results in lower model complexity and in some settings underfitting. Our result aligns with Savarese and Maire (2019) in that while smoothness in patterns naturally arises, explicitly encouraging smoothness through regularization hurts performance.

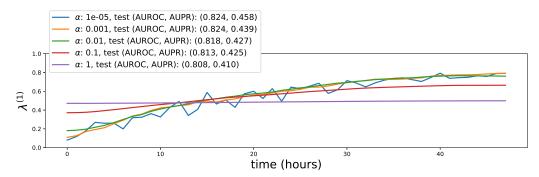


Figure 6: Visualization of the mixing coefficients learned by mixLSTM-2 with different regularization strengths for the mortality task. $\lambda^{(1)}$ is shown on the y-axis. $\lambda^{(2)}$ can be inferred $(\lambda^{(2)} = 1 - \lambda^{(1)})$. As regularization strength increase, mixing coefficients become smoother at the cost of lower performance.

What time-varying relationships does the mixLSTM learn to recognize? When attempting to understand which features drive a model's predictions, the focus is often put on the importance of certain features. However, because mixLSTM was designed to and has been shown to excel in situations with temporal conditional shift, we focus on identifying the features whose influence changes over time. To identify such features, we must first measure the effect of each feature at each time step. Here, we use the input gradient as a proxy for feature importance and visualize importance over time (Van Hasselt et al., 2016; Selvaraju et al., 2016; Graves, 2012) (Figure 7). More specifically, we traversed the test set, accumulating the input gradient with respect to the target class. One of the most noticeable patterns is the large amount of variation in feature importance in the first 6 hours of an ICU admission. This pattern is most apparent for the task of predicting shock (Figure 7b). This may reflect the significant physiological changes a patient may experience at the beginning of their ICU stay as interventions are administered in an effort to stabilize them.

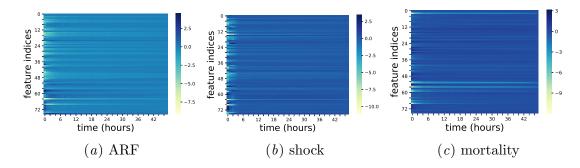


Figure 7: Input gradient based saliency map of mixLSTM-2 on three tasks. Each plot shows a proxy of importance of each feature across time steps. Some noticeable temporal patterns include high variability during the first six hours, which may be a reflection of increased physiological change a patient may experience at the beginning of their ICU stay when interventions are more frequent.

We list the continuous features ranked by importance in **Table 3**. Feature importance was calculated by summing importance over time and taking the absolute value. Here positive importance values are associated with increased risk, while negative importance values are associated with protection. The color scheme reflects the overall direction of association and the change over time. Dark red and dark green represent 'risk' and 'protective' factors that lead to increased and decreased risk over time, respectively; that is, their effects become amplified over time. Light red and light green represent 'risk' and 'protective' factors that lead to decreased and increased risk over time, respectively; that is, their effects diminish over time. For example, in all three tasks, 'fraction of inspired oxygen' (indicative of whether or not a patient is on supplemental oxygen) is a risk factor initially, and becomes more important over time. This suggests that if a patient is still on high levels of oxygen 48 hours into their ICU admission, their risk is elevated for all three outcomes. For ARF and shock a similar pattern holds for heart rate, where sustained high heart rate is associated with greater risk over time. This suggests that some features, when persistently abnormal, further amplify a patient's risk.

Table 3: Physiological data ranked by overall importance as identified by mixLSTM-2 on ARF, shock, and mortality using input gradient. The table is color coded. Light red denotes features that are initially risk factors, where risk *decreases* over time. Dark red denotes features that are initially risk factors, but where risk *increases* over time. Light green denotes features that are initially protective, but become less protective over time. Dark green denotes features that are initially protective, and becomes more protective over time.

ARF	shock	mortality
pН	Respiratory rate	Respiratory rate
Oxygen saturation	Height	Heart Rate
Weight	Mean blood pressure	Glucose
Respiratory rate	Heart Rate	Fraction inspired oxygen
Fraction inspired oxygen	Fraction inspired oxygen	Height
Heart Rate	pН	Weight
Height	Weight	Systolic blood pressure
Glucose	Glucose	pН
Systolic blood pressure	Oxygen saturation	Mean blood pressure
Mean blood pressure	Systolic blood pressure	Diastolic blood pressure
Temperature	Diastolic blood pressure	Oxygen saturation
Diastolic blood pressure	Temperature	Temperature

It is important to note that interpreting neural networks, and LSTMs in particular, remains an open challenge. Though the approach considered here is frequently used for interpreting LSTMs, it relies on the local effect of a feature and thus ignores the global trends (Ross et al., 2017; Ghorbani et al., 2019; Graves, 2012). Moreover, these methods merely identify associations and not causation.

Given the limitations of using input gradients to model the importance of discrete features, we also investigated feature importance using a permutation based sensitivity analysis (Fisher et al., 2018; Breiman, 2001). In the test set, we randomly permuted each covariate at each specific time period and measured predictive performance. By permuting each covariate in turn, we destroy any information that a particular covariate provides. If performance then drops significantly relative to a non-permuted baseline, we conclude the feature was important. To prevent correlated variables from leaking information, we simultaneously permuted variables with a correlation coefficient > 0.95. We permuted grouped features within periods of 12 hours to encourage consistency of perturbation along time. Figure 8 plots this measure of feature importance over time. Overall, we observe similar trends to the input gradient analysis. In addition to there being greater variability in the first part of the visit, we also observed significant changes in the importance of certain features (measured by sum of importance across time). For example, for the task of predicting in-hospital mortality, respiratory rate is initially the most important feature, but then temperature becomes more important as the patient state evolves. For ARF, a variable pertaining to the Glasgow coma scale is initially most important, before yielding to respiratory rate.

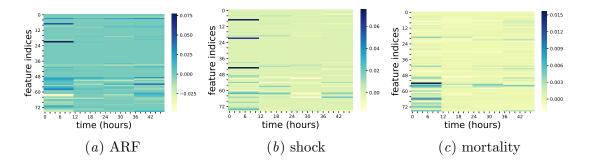


Figure 8: Permutation based saliency map of mixLSTM-2 on three tasks. Each plot shows AUROC degradation for permuting a feature. A larger decrease in AUROC means that the feature is more important with respect to the prediction task. Some noticeable temporal patterns include an increased variability during the first 12 hours which may be a reflection of increased physiological change a patient may experience at the beginning of their ICU stay when interventions are more frequent.

6. Conclusion

In this work, we present and explore the issue of temporal conditional shift in clinical time-series data. In addition, we propose a mixture of LSTM model (mixLSTM) and demonstrate that it effectively adapts to scenarios exhibiting temporal conditional shift, consistently outperforming baselines on synthetic and clinical data tasks. We also show that the mixLSTM model can adapt to settings with limited training data and learns meaningful, time-varying relationships from the data.

While mixLSTM achieves consistently better performance on all tasks considered, we note some important limitations. First, we only considered fixed-length datasets. It would be beneficial to compare LSTM and mixLSTM's ability to generalize to variable length data. Second, our features are largely physiological (e.g., heart rate, temperature). We hypothesize that other types of features such as medications may exhibit stronger time-varying relationships. Third, while it is reasonable to set time zero as the time of ICU admission, patients are admitted to the ICU at different points during the natural history of their illness. Future work should consider the alignment of patient time steps (e.g., learning an individualized model).

Despite these limitations, our results suggest that temporal conditional shift is an important aspect of clinical time-series prediction and future work could benefit from considering this problem setting. Our proposed mixLSTM presents a strong starting point from which future work can build.

Acknowledgments

This work was supported by the Michigan Institute for Data Science (MIDAS)³, the National Science Foundation (NSF award no. IIS-1553146), and the National Institute of Allergy and Infectious Diseases of the National Institutes of Health (grant no. U01AI124255). The views and conclusions in this document are those of the authors and should not be interpreted as necessarily representing the official policies, either expressed or implied, of the Michigan Institute for Data Science, the National Science Foundation, nor the National Institute of Allergy and Infectious Diseases of the National Institutes of Health.

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Appendix A. Details of Data & Features

Table 4: The 17 physiological features extracted from MIMIC-III database, the source tables, and the corresponding ITEMIDs $\frac{1}{2}$

Index	Variable Name	Table(s)	ITEMID(s)
1	Capillary refill rate	CHARTEVENTS	3348, 115, 8377
2	Diastolic blood pressure	CHARTEVENTS	8368, 220051, 225310, 8555, 8441, 220180, 8502, 8440, 8503, 8504, 8507, 8506, 224643
3	Fraction inspired oxygen	CHARTEVENTS	3420, 223835, 3422, 189, 727
4	Glascow coma scale eye opening	CHARTEVENTS	184, 220739
5	Glascow coma scale motor response	CHARTEVENTS	454, 223901
6	Glascow coma scale total	CHARTEVENTS	198,
7	Glascow coma scale verbal response	CHARTEVENTS	723, 223900
8	Glucose	CHARTEVENTS/LABEVENTS	50931, 807, 811, 1529, 50809, 51478, 3745, 225664, 220621, 226537
9	Heart Rate	CHARTEVENTS	221, 220045
10	Height	CHARTEVENTS	226707, 226730, 1394
11	Mean blood pressure	CHARTEVENTS	52, 220052, 225312, 224, 6702, 224322, 456, 220181, 3312, 3314, 3316, 3322, 3320
12	Oxygen saturation	CHARTEVENTS/LABEVENTS	834, 50817, 8498, 220227, 646, 220277
13	Respiratory rate	CHARTEVENTS	618, 220210, 3603, 224689, 614, 651, 224422, 615, 224690
14	Systolic blood pressure	CHARTEVENTS	51, 220050, 225309, 6701, 455, 220179, 3313, 3315, 442, 3317, 3323, 3321, 224167, 227243
15	Temperature	CHARTEVENTS	3655, 677, 676, 223762, 3654, 678, 223761, 679
16	Weight	CHARTEVENTS	763, 224639, 226512, 3580, 3693, 3581, 226531, 3582
17	рН	CHARTEVENTS/LABEVENTS	50820, 51491, 3839, 1673, 50831, 51094, 780, 1126, 223830, 4753, 4202, 860, 220274

Table 5: The 76 time-series features used as input to all the models.

Index	Feature Name	Type
0	Capillary refill rate->0.0	Binary
1	Capillary refill rate->1.0	Binary
2	Diastolic blood pressure	Numeric
3	Fraction inspired oxygen	Numeric
4	Glascow coma scale eye opening->To Pain	Binary
5	Glascow coma scale eye opening->3 To speech	Binary
6	Glascow coma scale eye opening->1 No Response	Binary
7	Glascow coma scale eye opening->4 Spontaneously	Binary
8	Glascow coma scale eye opening->None	Binary
9	Glascow coma scale eye opening->To Speech	Binary
10	Glascow coma scale eye opening->Spontaneously	Binary
11	Glascow coma scale eye opening->2 To pain	Binary
12	Glascow coma scale motor response->1 No Response	Binary
13	Glascow coma scale motor response->3 Abnorm flexion	Binary
14	Glascow coma scale motor response->Abnormal extension	Binary
15	Glascow coma scale motor response->No response	Binary
16	Glascow coma scale motor response->4 Flex-withdraws	Binary
17	Glascow coma scale motor response->Localizes Pain	Binary
18	Glascow coma scale motor response->Flex-withdraws	Binary
19	Glascow coma scale motor response->Obeys Commands	Binary
20	Glascow coma scale motor response->Abnormal Flexion	Binary
21	Glascow coma scale motor response->6 Obeys Commands	Binary
22	Glascow coma scale motor response->5 Localizes Pain	Binary
23	Glascow coma scale motor response->2 Abnorm extensn	Binary

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24	Glascow coma scale total->11	Binary
25 26	Glascow coma scale total>10	Binary
26	Glascow coma scale total->13	Binary
27	Glascow coma scale total->12	Binary
28	Glascow coma scale total->15	Binary
29	Glascow coma scale total->14	Binary
30	Glascow coma scale total->3	Binary
31	Glascow coma scale total->5	Binary
32	Glascow coma scale total->4	Binary
33	Glascow coma scale total->7	Binary
34	Glascow coma scale total->6	Binary
35	Glascow coma scale total->9	Binary
36	Glascow coma scale total->8	Binary
37	Glascow coma scale verbal response->1 No Response	Binary
38	Glascow coma scale verbal response->No Response	Binary
39	Glascow coma scale verbal response->Confused	Binary
40	Glascow coma scale verbal response->Inappropriate Words	Binary
41	Glascow coma scale verbal response->Oriented	Binary
42	Glascow coma scale verbal response->No Response-ETT	Binary
43	Glascow coma scale verbal response->5 Oriented	Binary
44	Glascow coma scale verbal response->Incomprehensible sounds	Binary
45	Glascow coma scale verbal response->1.0 ET/Trach	Binary
46	Glascow coma scale verbal response->4 Confused	Binary
47	Glascow coma scale verbal response->2 Incomp sounds	Binary
48	Glascow coma scale verbal response->3 Inapprop words	Binary
49	Glucose	Numeric
50	Heart Rate	Numeric
51	Height	Numeric
52	Mean blood pressure	Numeric
53	Oxygen saturation	Numeric
54	Respiratory rate	Numeric
55	Systolic blood pressure	Numeric
56	Temperature	Numeric
57	Weight	Numeric
58	Н	Numeric
59	mask->Capillary refill rate	Binary
60	mask->Diastolic blood pressure	Binary
61	mask->Fraction inspired oxygen	Binary
62	mask->Glascow coma scale eye opening	Binary
63	mask->Glascow coma scale motor response	Binary
64	mask->Glascow coma scale total	Binary
65	mask->Glascow coma scale verbal response	Binary
66	mask->Glucose	Binary
67	mask->Heart Rate	Binary
68	mask->Height	Binary
69	mask->Mean blood pressure	Binary
70	mask->Oxygen saturation	Binary
71	mask->Respiratory rate	Binary
72	mask->Systolic blood pressure	Binary
73	mask->Temperature	Binary
73 74	mask-> Temperature mask-> Weight	Binary
74 75	mask->pH	Binary
10	1100V- \ h11	Dinary