

Modelling and Stabilizing Control Laws Design Based on Sliding Mode for an UAV Type-Quadrotor

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Abstract-In this paper; we are interested principally in dynamic modelling of quadrotor while taking into account the high-order nonholonomic constraints in order to develop a new synoptic control scheme as well as the various physical phenomena, which can influence the dynamics of a flying structure. These permit us to introduce a new state-space representation and a new control scheme. We present also the development and the synthesis of a control algorithm based on sliding mode technique ensuring desired tracking trajectories, regulation and Lyapunov stability. Finally simulation results are also provided in order to illustrate the performances of the proposed controller.

Keywords-Dynamic modelling, High-order nonholonomic Constraints, Sliding mode.

I. INTRODUCTION

Unmanned aerial vehicles (UAV) have shown a growing interest thanks to recent technological projections, especially those related to instrumentation. They made possible the design of powerful systems (mini drones) endowed with real capacities of autonomous navigation at reasonable cost.

Despite the real progress made, researchers must still deal with serious difficulties, related to the control of such systems, particularly, in the presence of atmospheric turbulences. In addition, the navigation problem is complex and requires the perception of an often constrained and evolutionary environment, especially in the case of low-altitude flights.

Nowadays, the mini-drones invade several application domains [4]: safety (monitoring of the airspace, urban and interurban traffic); natural risk management (monitoring of volcano activities); environmental protection (measurement of air pollution and forest monitoring);

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intervention in hostile sites (radioactive workspace and mine clearance), management of the large infrastructures (dams, high-tension lines and pipelines), agriculture and film production (aerial shooting).

In contrast to terrestrial mobile robots, for which it is often possible to limit the model to kinematics, the control of aerial robots (quadrotor) requires dynamics in order to account for gravity effects and aerodynamic forces [3].

In [7], authors propose a control-law based on the choice of a stabilizing Lyapunov function ensuring the desired tracking trajectories along (X, Z) axis and roll angle. However, they do not take into account nonholonomic constraints. In [9], authors do not take into account frictions due to the aerodynamic torques nor drag forces or nonholonomic constraints. They propose a control-law based on backstepping in order to stabilize the complete system (i.e. translation and orientation). In [1], authors take into account the gyroscopic effects and show that the classical model-independent PD controller can stabilize asymptotically the attitude of the quadrotor aircraft. Moreover, they used a new Lyapunov function, which leads to an exponentially stabilizing controller based upon the PD^2 and the compensation of coriolis and gyroscopic torques. While in [2] the authors develop a PID controller in order to stabilize altitude.

Others papers; presented the sliding mode and high-order sliding mode respectively like an observer [13] and [14] in order to estimate the unmeasured states and the effects of the external disturbances such as wind and noise.

In this paper, based on the vectorial model form presented in [2] we are interested principally in the modelling of quadrotor to account for various parameters which affect the dynamics of a flying structure such as frictions due to the aerodynamic torques, drag forces along (X, Y, Z) axis and gyroscopic effects which are identified in [2] for an experimental quadrotor and for high-order nonholonomic constraints [11]. Consequently, all

these parameters supported the setting of the system under more complete and more realistic new state-space representation and new control scheme which cannot be found easily in the literature being interested in the control laws synthesis for such systems.

Then, we present a control technique based on the development and the synthesis of a control algorithm based upon sliding mode using linear sliding surfaces and ensures Lyapunov stability and desired tracking trajectories expressed in term of the center of mass coordinates along (X, Y, Z) axis and yaw angle, while the desired roll and pitch angles are deduced from nonholonomic constraints unlike to [9].

Finally, all synthesized control laws are validated by simulations for the complete model.

II. MODELLING

A. Quadrotor Dynamic Modelling



Figure. 1: Typical example of a quadrotor.

The aerial robot under consideration consists of a rigid cross frame equipped with four rotors [1] as shown in figure 1. The up-down motion is achieved by increasing or decreasing the total thrust while maintaining an equal individual thrust. The forward/backward, left/ right and the yaw motions are achieved through a differential control strategy of the thrust generated by each rotor. In order to avoid the yaw drift due to the reactive torques, the quadrotor aircraft is configured such that the set of rotors (right-left) rotates clockwise and the set of rotors (front-rear) rotates counter-clockwise. There are no direction changes in the rotors rotation. If a yaw motion is desired, one has to reduce the thrust of one set of rotors and increase the thrust of the other set while maintaining the same total thrust to avoid an up-down motion. Hence, the yaw motion is then realized in the direction of the induced reactive torque. On the other hand, forward and backward motion are achieved by pitching in the desired direction by increasing the front (rear) rotor thrust and decreasing the rear (front) rotor thrust to maintain the total thrust. Finally, a sideways motion is achieved by rolling in the desired direction by increasing the left (right) rotor thrust and decreasing the right (left) rotor thrust to maintain the total thrust.

Let $E(O, X, Y, Z)$ denote an inertial frame, and $B(o', x, y, z)$ denote a frame rigidly attached to the quadrotor as shown in figure 2.

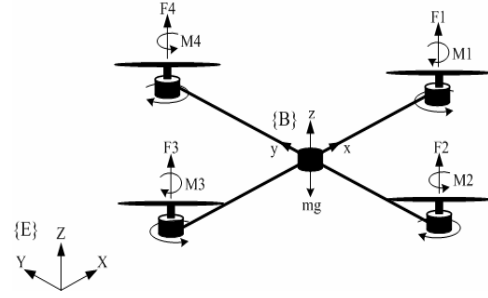


Figure. 2 : quadrotor configuration.

We will make the following assumptions:

- The quadrotor structure is rigid and symmetrical.
- The center of mass and o' coincides.
- The propellers are rigid.
- Thrust and drag are proportional to the square of the propellers speed.

Under these assumptions, it is possible to describe the fuselage dynamics as that of a rigid body in space to which come to be added the aerodynamic forces caused by the rotation of the rotors.

Using the formalism of Newton-Euler, the dynamic equations are written in the following form:

$$\begin{cases} \dot{\xi} = v \\ m\ddot{\xi} = F_f + F_t + F_g \\ \dot{R} = RS(\Omega) \\ J\dot{\Omega} = -\Omega \wedge J\Omega + \Gamma_f - \Gamma_a - \Gamma_g \end{cases} \quad (1)$$

ξ is the position of the quadrotor center of mass with respect to the inertial frame. m is the total mass of the structure and $J \in R^{3 \times 3}$ is a symmetric positive definite constant inertia matrix of the quadrotor with respect to B .

$$J = \begin{pmatrix} I_x & 0 & 0 \\ 0 & I_y & 0 \\ 0 & 0 & I_z \end{pmatrix} \quad (2)$$

Ω is the angular velocity of the airframe expressed in B :

$$\Omega = \begin{pmatrix} 1 & 0 & -\sin \theta \\ 0 & \cos \phi & \cos \theta \sin \phi \\ 0 & -\sin \phi & \cos \phi \cos \theta \end{pmatrix} \begin{bmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{bmatrix} \quad (3)$$

In the case where the quadrotor performs many angular motions of low amplitude Ω can be assimilated to $\begin{bmatrix} \dot{\phi} & \dot{\theta} & \dot{\psi} \end{bmatrix}^T$.

R is the homogenous matrix transformation [12].

$$R = \begin{pmatrix} C\theta C\psi & C\psi S\theta S\phi - S\psi C\phi & C\psi S\theta C\phi + S\psi S\phi \\ C\theta S\psi & S\psi S\theta S\phi + C\psi C\phi & S\psi S\theta C\phi - C\psi S\phi \\ -S\theta & S\phi C\theta & C\phi C\theta \end{pmatrix} \quad (4)$$

Where C and S indicate the trigonometrical functions **cos** and **sin** respectively. $S(\Omega)$ is a skew-symmetric matrix. For a given vector $\Omega = [\Omega_1 \ \Omega_2 \ \Omega_3]^T$ it is defined as follows:

$$S(\Omega) = \begin{pmatrix} 0 & -\Omega_3 & \Omega_2 \\ \Omega_3 & 0 & -\Omega_1 \\ -\Omega_2 & \Omega_1 & 0 \end{pmatrix}$$

F_f is the resultant of the forces generated by the four rotors.

$$F_f = \begin{pmatrix} C\phi C\psi S\theta + S\phi S\psi \\ C\phi S\theta S\psi - S\phi C\psi \\ C\phi C\theta \end{pmatrix} \sum_{i=1}^4 F_i \quad (5)$$

$$F_i = K_p \omega_i^2 \quad (6)$$

Where K_p is the lift coefficient and ω_i is the angular rotor speed.

F_t is the resultant of the drag forces along (X, Y, Z) axis.

$$F_t = \begin{pmatrix} -K_{f_{tx}} & 0 & 0 \\ 0 & -K_{f_{ty}} & 0 \\ 0 & 0 & -K_{f_{tz}} \end{pmatrix} \dot{\xi} \quad (7)$$

Where $K_{f_{tx}}, K_{f_{ty}}$ and $K_{f_{tz}}$ are the translation drag coefficients.

F_g is the force gravity.

$$F_g = [0 \ 0 \ -mg]^T \quad (8)$$

Γ_f is the moment developed by the quadrotor according to the body fixed frame. It is expressed as follows:

$$\Gamma_f = \begin{bmatrix} d(F_3 - F_1) \\ d(F_4 - F_2) \\ K_d(\omega_1^2 - \omega_2^2 + \omega_3^2 - \omega_4^2) \end{bmatrix} \quad (9)$$

d is the distance between the quadrotor center of mass and the rotation axis of propeller and K_d is the drag coefficient.

Γ_a is the resultant of aerodynamics frictions torques.

$$\Gamma_a = \begin{bmatrix} K_{f_{ax}} & 0 & 0 \\ 0 & K_{f_{ay}} & 0 \\ 0 & 0 & K_{f_{az}} \end{bmatrix} \Omega^2 \quad (10)$$

$K_{f_{ax}}, K_{f_{ay}}$ and $K_{f_{az}}$ are the aerodynamic friction coefficients.

Γ_g is the resultant of torques due to the gyroscopic effects.

$$\Gamma_g = \sum_{i=1}^4 \Omega \wedge J_r \begin{bmatrix} 0 \\ 0 \\ (-1)^{i+1} \omega_i \end{bmatrix} \quad (11)$$

Where J_r is the rotor inertia.

Consequently, the complete dynamics is as follows:

$$\begin{cases} \ddot{\phi} = \frac{1}{I_x} \{ \dot{\theta} \dot{\psi} (I_y - I_z) - K_{f_{ax}} \dot{\phi}^2 - J_r \bar{\Omega} \dot{\theta} + dU_2 \} \\ \ddot{\theta} = \frac{1}{I_y} \{ \dot{\phi} \dot{\psi} (I_z - I_x) - K_{f_{ay}} \dot{\theta}^2 + J_r \bar{\Omega} \dot{\phi} + dU_3 \} \\ \ddot{\psi} = \frac{1}{I_z} \{ \dot{\theta} \dot{\phi} (I_x - I_y) - K_{f_{az}} \dot{\psi}^2 + K_d U_4 \} \\ \ddot{x} = \frac{1}{m} \{ (C\phi S\theta C\psi + S\phi S\psi) U_1 - K_{f_{tx}} \dot{x} \} \\ \ddot{y} = \frac{1}{m} \{ (C\phi S\theta S\psi - S\phi C\psi) U_1 - K_{f_{ty}} \dot{y} \} \\ \ddot{z} = \frac{1}{m} \{ (C\phi C\theta) U_1 - K_{f_{tz}} \dot{z} \} - g \end{cases} \quad (12)$$

U_1, U_2, U_3 and U_4 are the control inputs of the system which are written according to the angular velocities of the four rotors as follows:

$$\begin{bmatrix} U_1 \\ U_2 \\ U_3 \\ U_4 \end{bmatrix} = \begin{pmatrix} K_p & K_p & K_p & K_p \\ -K_p & 0 & K_p & 0 \\ 0 & -K_p & 0 & K_p \\ K_d & -K_d & K_d & -K_d \end{pmatrix} \begin{bmatrix} \omega_1^2 \\ \omega_2^2 \\ \omega_3^2 \\ \omega_4^2 \end{bmatrix} \quad (13)$$

and $\bar{\Omega} = (\omega_1 - \omega_2 + \omega_3 - \omega_4)$

B. Nonholonomic Constraints

Taking into account nonholonomic constraints for our system is of major importance as are in compliance with physical laws and define the coupling between various states of the system.

From the equations of the translation dynamics (12) we can extract the expressions of the high-order nonholonomic constraints:

$$\left\{ \begin{array}{l} \tan \theta = \frac{\left(\ddot{x} - \frac{K_{fx}}{m} \dot{x} \right) C\psi + \left(\ddot{y} - \frac{K_{fy}}{m} \dot{y} \right) S\psi}{\ddot{z} + g - \frac{K_{fz}}{m} \dot{z}} \\ S\phi = \frac{-\left(\ddot{x} - \frac{K_{fx}}{m} \dot{x} \right) S\psi + \left(\ddot{y} - \frac{K_{fy}}{m} \dot{y} \right) C\psi}{\sqrt{\left(\ddot{x} - \frac{K_{fx}}{m} \dot{x} \right)^2 + \left(\ddot{y} - \frac{K_{fy}}{m} \dot{y} \right)^2 + \left(\ddot{z} + g - \frac{K_{fz}}{m} \dot{z} \right)^2}} \end{array} \right. \quad (14)$$

C. Rotor Dynamic

The rotor is a unit constituted by D.C-motor actuating a propeller via a reducer. The D.C-motor is governed by the following dynamic equations:

$$\left\{ \begin{array}{l} V = ri + L \frac{di}{dt} + k_e \omega \\ k_m i = J_r \frac{d\omega}{dt} + C_s + k_r \omega^2 \end{array} \right. \quad (15)$$

The different parameters of the motor are defined as follows:

- V : motor input.
- k_e, k_m : electrical and mechanical torque constants, respectively.
- k_r : load constant torque.
- r : motor internal resistance.
- J_r : rotor inertia.
- C_s : solid friction.

Then, the model chosen for the rotor is as follows:

$$\dot{\omega}_i = bV_i - \beta_0 - \beta_1 \omega_i - \beta_2 \omega_i^2 \quad (16)$$

$i \in [1, 4]$

with:

$$\beta_0 = \frac{C_s}{J_r}, \beta_1 = \frac{k_e k_m}{r J_r}, \beta_2 = \frac{k_r}{J_r} \text{ and } b = \frac{k_m}{r J_r}$$

III. SLIDING MODE CONTROL OF QUADROTOR

The choice of this method is not fortuitous considering the major advantages it presents:

- It ensures Lyapunov stability.
- It ensures the robustness and all properties of the desired dynamics.
- It ensures the handling of all system nonlinearities.

The model (12) developed in the first part of this paper can be rewritten in the state-space form:

$\dot{X} = f(X) + g(X, U) + \delta$ and $X = [x_1 \dots x_{12}]^T$ is the state vector of the system such as:

$$X = [\phi, \dot{\phi}, \theta, \dot{\theta}, \psi, \dot{\psi}, x, \dot{x}, y, \dot{y}, z, \dot{z}]^T \quad (17)$$

From (12) and (17) we obtain the following state representation:

$$\left\{ \begin{array}{l} \dot{x}_1 = x_2 \\ \dot{x}_2 = a_1 x_4 x_6 + a_2 x_2^2 + a_3 \bar{\Omega} x_4 + b_1 U_2 \\ \dot{x}_3 = x_4 \\ \dot{x}_4 = a_4 x_2 x_6 + a_5 x_4^2 + a_6 \bar{\Omega} x_2 + b_2 U_3 \\ \dot{x}_5 = x_6 \\ \dot{x}_6 = a_7 x_2 x_4 + a_8 x_6^2 + b_3 U_4 \\ \dot{x}_7 = x_8 \\ \dot{x}_8 = a_9 x_8 + U_x \frac{U_1}{m} \\ \dot{x}_9 = x_{10} \\ \dot{x}_{10} = a_{10} x_{10} + U_y \frac{U_1}{m} \\ \dot{x}_{11} = x_{12} \\ \dot{x}_{12} = a_{11} x_{12} + \frac{C x_1 C x_3}{m} U_1 - g \end{array} \right. \quad (18)$$

$$\left\{ \begin{array}{l} a_1 = \left(\frac{I_y - I_z}{I_x} \right), a_2 = \frac{-K_{fax}}{I_x}, a_3 = \frac{-J_r}{I_x} \\ a_4 = \left(\frac{I_z - I_x}{I_y} \right), a_5 = \frac{-K_{fay}}{I_y}, a_6 = \frac{J_r}{I_y} \\ a_7 = \left(\frac{I_x - I_y}{I_z} \right), a_8 = \frac{-K_{faz}}{I_z}, a_9 = \frac{-K_{fz}}{m} \\ a_{10} = \frac{-K_{fyz}}{m}, a_{11} = \frac{-K_{fzx}}{m} \\ b_1 = \frac{d}{I_x}, b_2 = \frac{d}{I_y}, b_3 = \frac{1}{I_z} \end{array} \right. \quad (19)$$

$$\left\{ \begin{array}{l} U_x = C x_1 S x_3 C x_5 + S x_1 S x_5 \\ U_y = C x_1 S x_3 S x_5 - S x_1 C x_5 \end{array} \right. \quad (20)$$

The state representation of the system under this form has never been developed before.

From the high-order nonholonomic constraints developed in (14), ϕ and θ angles depend not only on the ψ but also on the motions along (X, Y, Z) axis and their dynamics. However, the adopted control strategy is summarized in the control of two subsystems: the first relates to the position control while the second is that of the attitude control, as shown in figure 3.

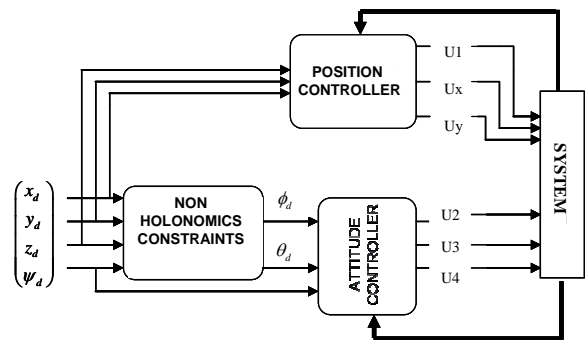


Figure. 3: Synoptic scheme of the proposed controller

A. Stabilizing Control Laws Synthesis

In this section, the purpose is to design a sliding mode controller. The basic sliding mode controller design procedure in our case is performed in two steps. Firstly, the choice of sliding surface (S) according to the tracking error. In the second step, design a Lyapunov function which can satisfy the necessary sliding condition ($S\dot{S} < 0$).

The synthesized stabilizing control laws are as follows:

$$\left\{ \begin{array}{l} U_2 = \frac{1}{b_1} \{-k_1 \text{sign}(S_\phi) - a_1 x_4 x_6 - a_2 x_2^2 - a_3 \bar{\Omega} x_4 + \ddot{\phi}_d + \lambda_1 e_2\} \\ U_3 = \frac{1}{b_2} \{-k_2 \text{sign}(S_\theta) - a_4 x_2 x_6 - a_5 x_4^2 - a_6 \bar{\Omega} x_2 + \ddot{\theta}_d + \lambda_2 e_4\} \\ U_4 = \frac{1}{b_3} \{-k_3 \text{sign}(S_\psi) - a_7 x_2 x_4 - a_8 x_6^2 + \ddot{\psi}_d + \lambda_3 e_6\} \\ U_x = \frac{m}{U_1} \{-k_4 \text{sign}(S_x) - a_9 x_8 + \ddot{x}_d + \lambda_4 e_8\} \quad / U_1 \neq 0 \\ U_y = \frac{m}{U_1} \{-k_5 \text{sign}(S_y) - a_{10} x_{10} + \ddot{y}_d + \lambda_5 e_{10}\} \quad / U_1 \neq 0 \\ U_z = \frac{m}{C\phi C\theta} \{-k_6 \text{sign}(S_z) - a_{11} x_{12} + \ddot{z}_d + \lambda_6 e_{12} + g\} \end{array} \right. \quad (21)$$

Proof:

Let us choose the sliding surfaces given by:

$$\left\{ \begin{array}{l} S_\phi = e_2 + \lambda_1 e_1 \\ S_\theta = e_4 + \lambda_2 e_3 \\ S_\psi = e_6 + \lambda_3 e_5 \\ S_x = e_8 + \lambda_4 e_7 \\ S_y = e_{10} + \lambda_5 e_9 \\ S_z = e_{12} + \lambda_6 e_{11} \end{array} \right. \quad (22)$$

Such as:

$$\lambda_i > 0 \text{ and } \begin{cases} e_{i+1} = \dot{e}_i \\ e_i = x_{id} - x_i \end{cases} \quad i \in [1,11] \quad (23)$$

We assume that:

$$V(S_\phi) = \frac{1}{2} S_\phi^2 \quad (24)$$

If $V(S_\phi) < 0$, so $S_\phi \dot{S}_\phi < 0$ then, the necessary sliding condition is verified and Lyapunov stability is guaranteed.

The chosen law for the attractive surface is the time derivative of (21) satisfying ($S_\phi \dot{S}_\phi < 0$):

$$\begin{aligned} \dot{S}_\phi &= -k_1 \text{sign}(S_\phi) \\ &= \ddot{x}_{1d} - \dot{x}_2 + \lambda_1 \dot{e}_1 \\ &= -a_1 x_4 x_6 - a_2 x_2^2 - a_3 \bar{\Omega} x_4 - b_1 U_2 + \ddot{\phi}_d + \lambda_1 (\dot{\phi}_d - x_2) \\ U_2 &= \frac{1}{b_1} \{-k_1 \text{sign}(S_\phi) - a_1 x_4 x_6 - a_2 x_2^2 - a_3 \bar{\Omega} x_4 + \ddot{\phi}_d + \lambda_1 e_2\} \end{aligned} \quad (25)$$

The same steps are followed to extract U_3 , U_4 , U_x , U_y and U_z .

B. Simulation Results

The simulation results are obtained based on the following real parameters [15]:

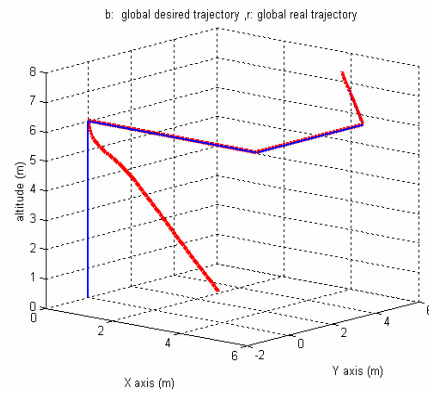


Figure 4: Global trajectory of the quadrotor in 3D

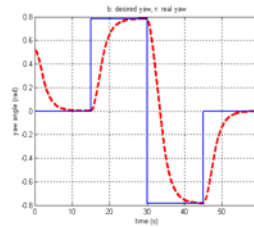


Fig. 5.a

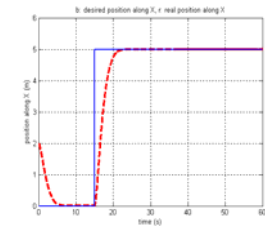


Fig. 5.b

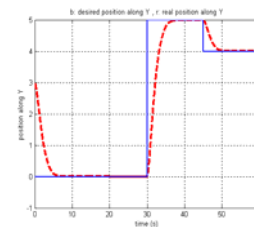


Fig. 5.c

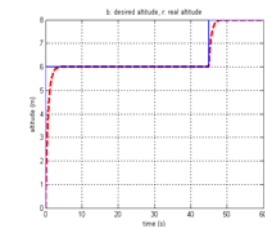


Fig. 5.d

Figure 5: Tracking simulation results of the desired trajectories along yaw angle (ψ) and (X, Y, Z) axis.

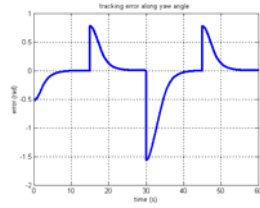


Fig. 6.a

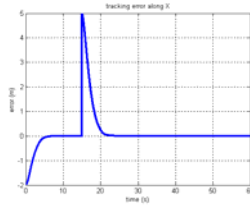


Fig. 6.b

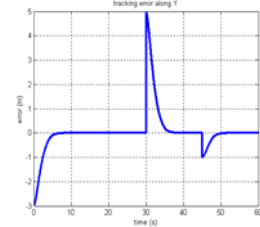


Fig. 6.c

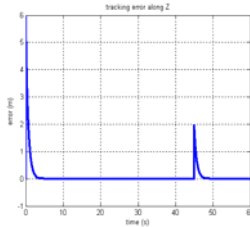


Fig. 6.d

Figure 6: Tracking errors along yaw (ψ) angle and (X, Y, Z) respectively.

Figure (4) shows the tracking of desired trajectory by the real one and the evolution of the quadrotor in space and its stabilization.

Figure (5) highlights the tracking of the desired trajectories along yaw angle (ψ) and (X, Y, Z) axis respectively. The response time of the system is about 5s.

Figure (6) represents the tracking errors made on the desired trajectories.

IV. CONCLUSION

In this paper, we presented a stabilizing control laws synthesis by sliding mode using linear sliding surfaces based firstly, on the development of the dynamic model of the quadrotor taking into account the different physical phenomena which can influence the evolution of our system in the space and secondly on the development of the high-order nonholonomic constraints imposed on the system motions. These control laws allowed the tracking of the various desired trajectories and Lyapunov stability expressed in terms of the center of mass coordinates of the system in spite of the complexity of the proposed model. As prospects we plan to develop other control techniques in order to improve the performances and to implement them on a real system.

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