

Hitting Set Heuristics for Overlapping Landmarks

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University
of Basel

Planning a Camping Trip with LAMA

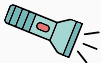


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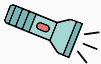
- knife
- can opener
- place to sleep
- weather protection
- flashlight
- navigation device

Different Options to Achieve Landmarks



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knife



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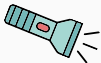
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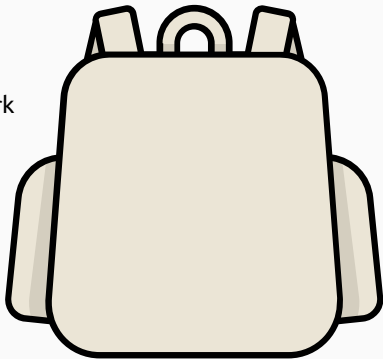


navigation device

What does LAMA pack?



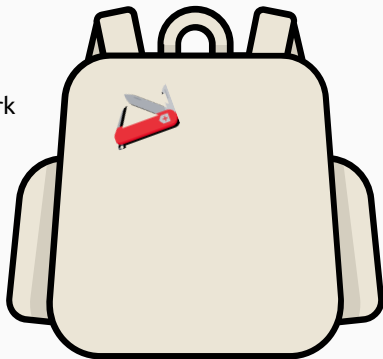
- **cheapest** item from every landmark



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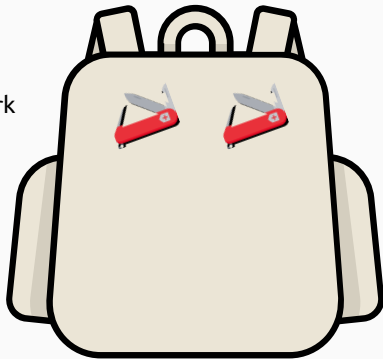
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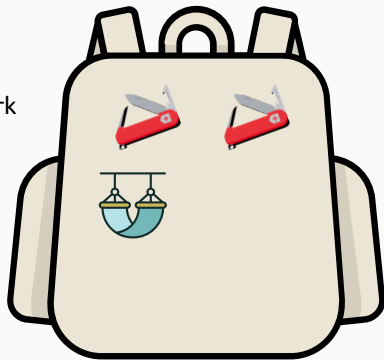
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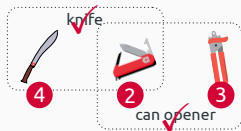
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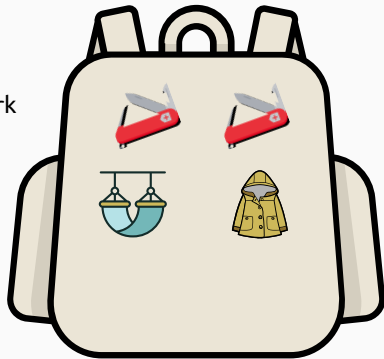
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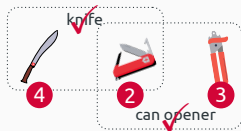
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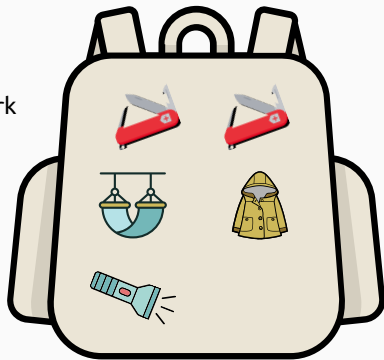
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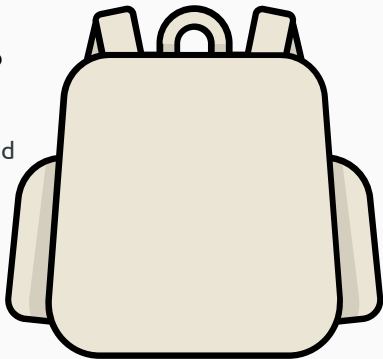
- **cheapest** item from every landmark
- $h^{\text{LAMA}} = 25$
- That's more stuff than necessary!
- **remove duplicates**: $h^{\text{HS}} = 23$



Greedy Hitting Set



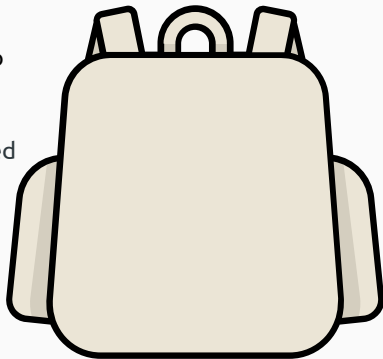
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2. discard achieved landmarks
3. repeat until all landmarks achieved



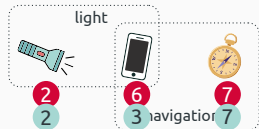
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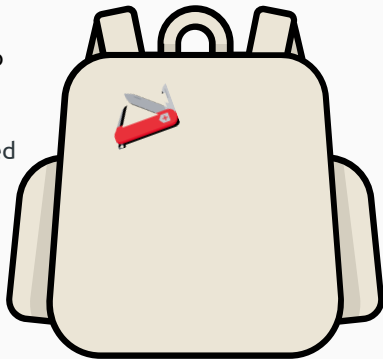
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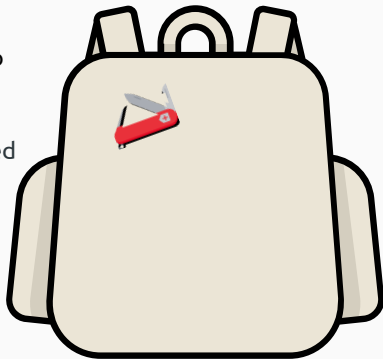
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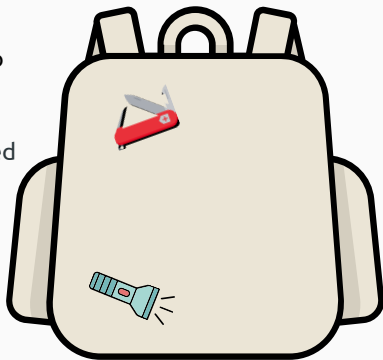
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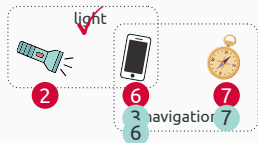
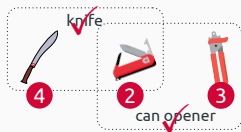
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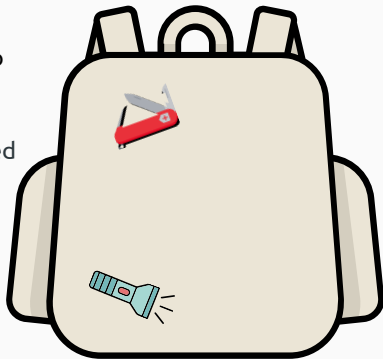
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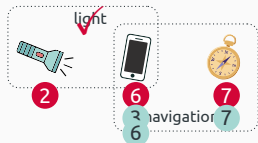
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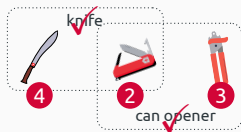
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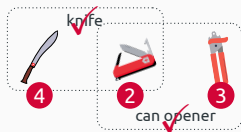


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- $h^{\text{GHS}} = 18$
- $h^{\text{MHS}} = 16 \rightsquigarrow \text{NP-complete}$



Greedy Best First Search

	(total)	h^{LAMA}	h^{HS}	h^{GHS}
Coverage	(2804)	1998	2006	1983

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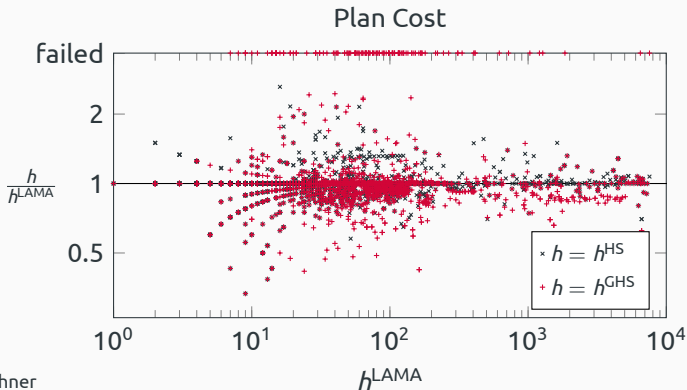
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Approximation: **all actions** can achieve derived landmarks.

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- open lists for **multiple heuristics**
- **preferred operators**
- improve plans by restarting **weighted A*** search

Full LAMA Configurations

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	Coverage	Score
h^{LAMA}	2458	2357.3
h^{HS}	2426	2324.2
h^{GHS}	2444	2361.9

Full LAMA Configurations

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no derived variables		
h^{LAMA}	2056	1957.8
h^{HS}	2052	1952.0
h^{GHS}	2068	1987.3

- overlapping landmarks express **synergies**
- **hitting set heuristics** exploit these synergies
- tradeoff between **heuristic accuracy** and **computation time**
- **plan quality** improves with more accurate heuristics in practice

Hitting Set Problem

Definition

Given:

- **universe** U 
- **set of sets** $\mathcal{S} \subseteq 2^U$ knives: {   }
- **cost function** $cost: U \rightarrow \mathbb{R}_0^+$ $cost() = 2$

Problem:

- Find **hitting set** $H \subseteq U$ s.t. $H \cap S \neq \emptyset$ for all $S \in \mathcal{S}$.
- **minimal** hitting set: no cheaper hitting set exists

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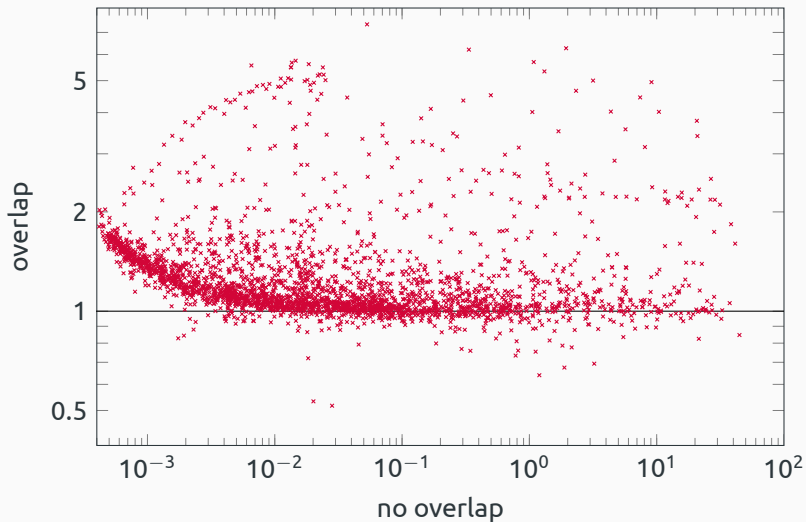
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Our approach: **keep everything**, let the heuristic deal with it.

Landmark Generation Time



overapproximation of h^{GHS} bounded $\rightsquigarrow h^{\text{GHS-opt}}$

	(total)	$h^{\text{GHS-opt}}$	h^{OCP}	h^{UCP}
Coverage	(1847)	904	907	1007

h^{OCP} : optimal cost partitioning $\approx h^{\text{MHS}}$

h^{UCP} : uniform cost partitioning