

# Novelty vs. Potential Heuristics: A Comparison of Hardness Measures for Satisficing Planning

Simon Dold Malte Helmert  
University of Basel

## Motivation

- ▶ Correlation complexity (Seipp et. al 2016) and novelty width (Lipovetzky and Geffner, 2012; 2014) are different approaches to quantify the hardness of planning tasks
- ▶ These measures are not closely related
- ▶ Provide a measure that is closely related to both

## Potential Heuristics

A **potential heuristic** is a heuristic that is computed with a weighted count of the partial assignments that agree with the given state.

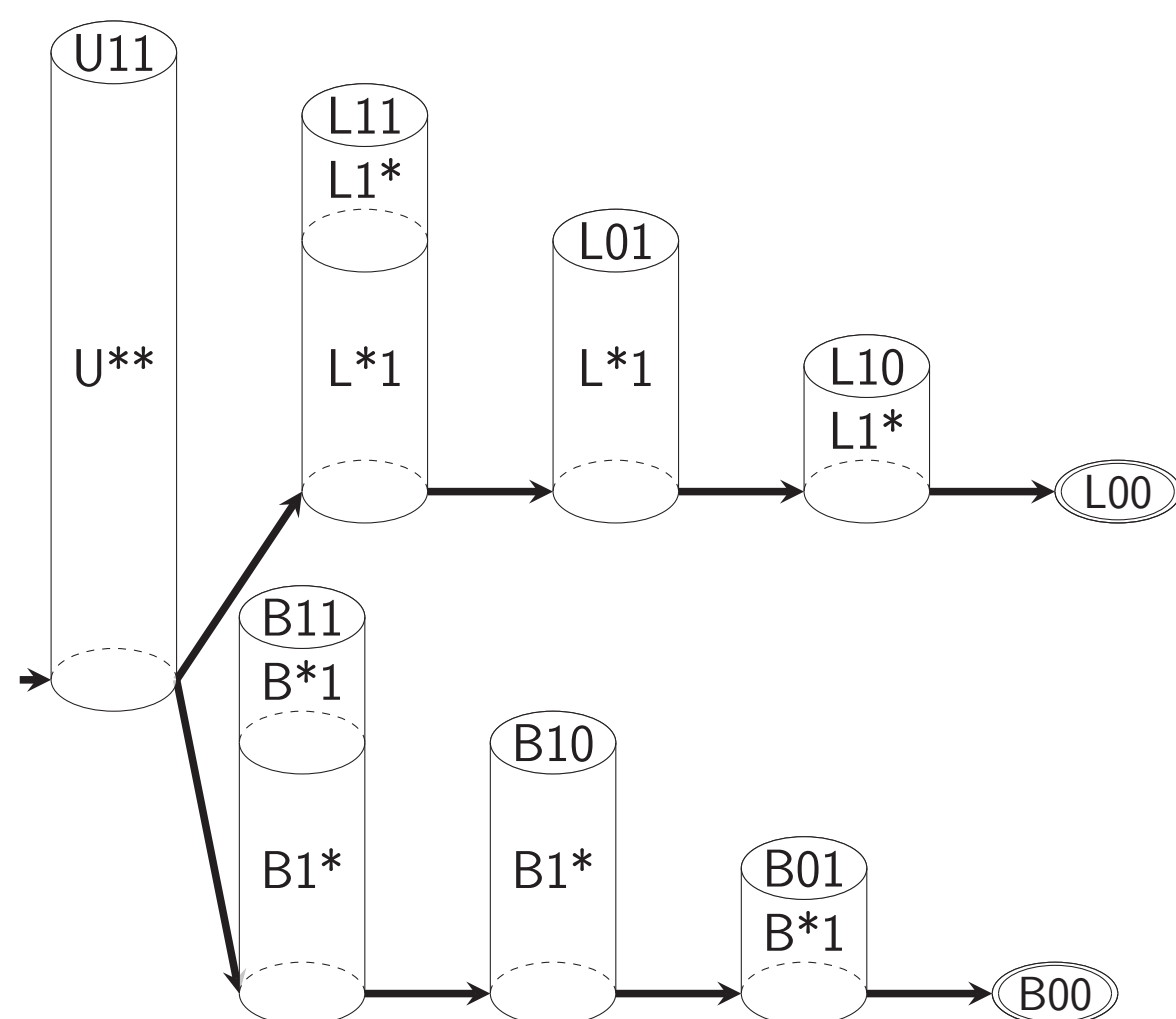
$$h^{pot}(s) = \sum_{p \in \mathcal{P}} (w(p) \cdot [p \subseteq s])$$

The **dimension** of  $h^{pot}$  is  $\max_{p \in \mathcal{P}, w(p) \neq 0} |p|$ .

## Correlation Complexity vs. River Measure

Correlation complexity:

- ▶ alive = reachable + solvable
- ▶ What dimension is required to construct a potential heuristic where all descending paths from **all alive states** lead to a goal?



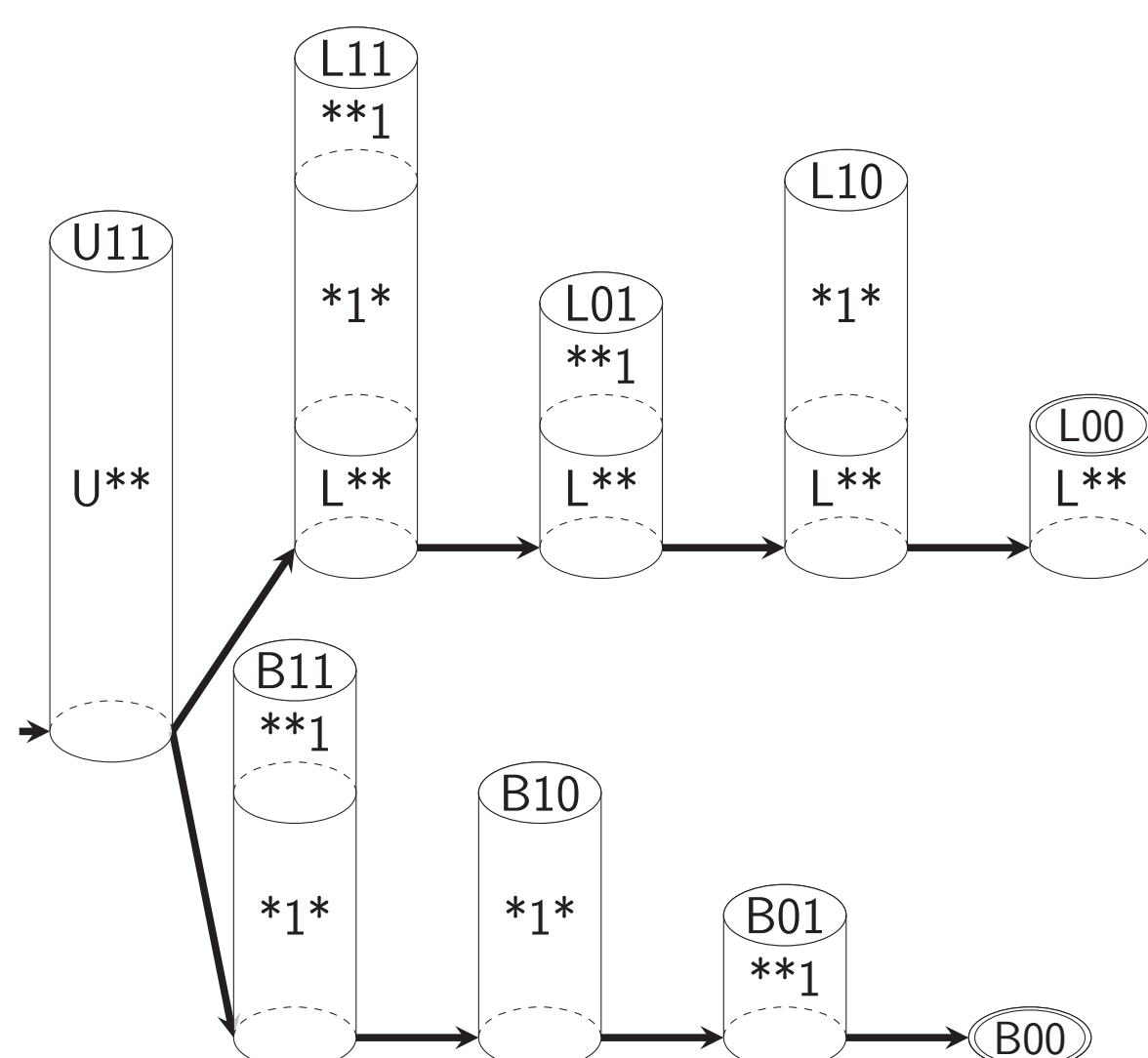
Initial state  $I = U11$   
Goal  $\gamma = *00$

$p$	$w(p)$
$U^{**}$	5
$L1^*$	1
$L^*1$	2
$B1^*$	2
$B^*1$	1

dimension = 2

River Measure:

- ▶ What dimension is required to construct a potential heuristic where all descending paths from **the initial state** lead to a goal?



$p$	$w(p)$
$U^{**}$	4
$L^{**}$	1
$*1^*$	2
$**1$	1

dimension = 1

## Novelty Width

- ▶ Novelty width is the smallest  $k$  that guarantees to find a plan with novelty width search:

```

if  $\gamma \subseteq I$ :
    return extractPlan(I)
open := [I]
closed := { $p \mid p \subseteq I, |p| = k$ }
while open  $\neq \emptyset$ :
    s := pop first element of open
    foreach  $s' \in successors(s)$ :
        if  $\gamma \subseteq s'$ :
            return extractPlan(s')
        if  $\exists q \subseteq s'$  with  $|q| = k, q \notin closed$ :
            insert each  $p \subseteq s'$  with  $|p| = k$  in closed
            append  $s'$  to open
return fail, k is not sufficiently large
    
```

## Comparison

Novelty width is not comparable to correlation complexity.

- ▶  $NW(\Pi') < CC(\Pi')$  for some  $\Pi'$
- ▶  $NW(\Pi'') > CC(\Pi'')$  for some  $\Pi''$

River measure is comparable to both.

- ▶  $RM(\Pi) \leq NW(\Pi) + 1$
- ▶  $RM(\Pi) \leq CC(\Pi)$

River measure is a bridge to compare novelty width and correlation complexity.

## Novelty Width vs. River Measure

- ▶ Construct  $h^{pot}$  to prove  $RM(\Pi) \leq NW(\Pi) + 1$
- ▶ States of plan found with novelty width search:  $\pi_0, \pi_1, \dots, \pi_L$
- ▶ Pick weights such that  $\pi_i$  is the only improving successor of  $\pi_{i-1}$

