

# Higher-Dimensional Potential Heuristics: Lower Bound Criterion and Connection to Correlation Complexity

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The macro consists of  
a set-up,  
a main execution  
and a tear-down

The set-up and tear-down have to be inverse  
of each other. They can be n-times folded  
macros themselves. If they are, then the  
macro is folded n+1 times.

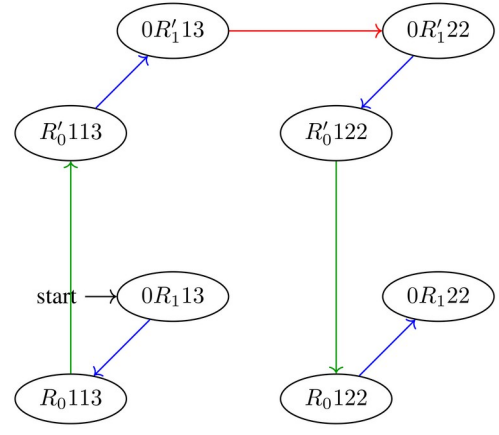
Each plan contains the macro

A sequence of actions

2 times folded macro in Terms

```
move-down pos-2 n1 pos-1 n0
create-block pos-1
move-up pos-1 n0 pos-2 n1
place-block pos-2 pos-3 n1 n2
move-up pos-2 n1 pos-3 n2
remove-block pos-3 pos-4 n3 n2
move-down pos-3 n2 pos-2 n1
move-down pos-2 n1 pos-1 n0
destroy-block pos-1
move-up pos-1 n0 pos-2 n1
```

# Critical, Folded Macros cause large Correlation Complexity



Dimension required for  
descending and dead-end avoiding  
potential heuristic

Each solvable + reachable state has an improving  
successor. Such improving successors are solvable.

Computed with a weighted count of the partial states that agree with the given state

$$h(s) = \sum_{p \in P} w(p) \cdot [p \subseteq s]$$

**Theorem:** If a macro is critical in a planning task and  
folded n times, then the task has correlation complexity  
of at least n+1.