

# Temporal Fast Downward

Using the Context-enhanced Additive Heuristic for  
Temporal and Numeric Planning

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# Motivation

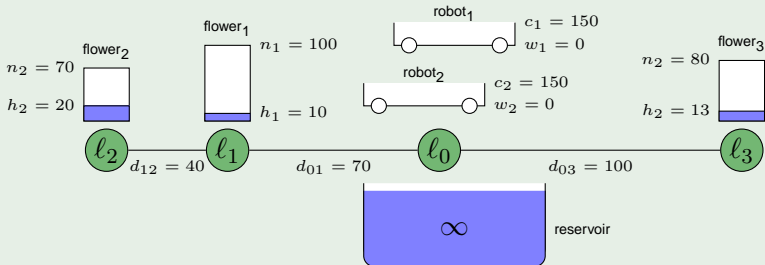
## Planning with Time and Resources

- Observations:
  - Time and resources important in real-world problems.
  - Heuristic search with context-enhanced additive (cea) heuristic successful in sequential planning.
- Question: Does the approach also work with time and resources?

# Planning with Time and Resources

## Example (Planning Task)

- Two gardening robots need to water flowers.
- Water levels, capacities and water needs are given.
- Robots can work concurrently.



# Planning with Time and Resources

## Durative Actions

- Actions have **durations** and may affect numeric variables.
- **Conditions** at-start, over-all, or at-end.
- **Effects** at-start or at-end.

### Example (Durative Actions)

Walking from one location to an adjacent one.

(at  $r_i$   $l_j$ )  
(connected  $l_j$   $l_k$ )

(walk  $r_i$   $l_j$   $l_k$ ) [ $d_{jk}$ ]

(not (at  $r_i$   $l_j$ ))

(at  $r_i$   $l_k$ )

# Planning with Time and Resources

## Durative Actions

### Example (Durative Actions, ctd.)

Watering a flower at a certain location.

$$w_i \geq n_k - h_k$$

(in  $f_k \ell_j$ )

(at  $r_i \ell_j$ )

(at  $r_i \ell_j$ )

(at  $r_i \ell_j$ )

(water  $r_i \ell_j f_k$ ) [ $n_k - h_k$ ]

$$h_k := n_k$$

$$w_i - = (n_k - h_k)$$

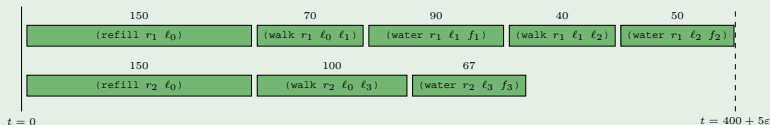
# Planning with Time and Resources

## Temporal Plans

- Must respect **causal** and **temporal constraints**.
- May contain **concurrent actions**.

### Example (Temporal Plan)

Robots  $robot_1$  and  $robot_2$  work concurrently.



# Temporal Numeric SAS<sup>+</sup> Planning Tasks

## Definition (Temporal Numeric SAS<sup>+</sup> Planning Task)

A temporal numeric SAS<sup>+</sup> planning task  $\Pi = \langle \mathcal{V}, s_0, s_*, \mathcal{A}, \mathcal{O} \rangle$  consists of the following components:

- A finite set  $\mathcal{V}$  of **state variables**. Each variable is either:
  - A **numeric variable** with values in  $\mathbb{R}$ .
  - A **comparison variable** with values in  $\{T, F\}$ .
  - A **logical variable** with arbitrary finite domain.
- An **initial state**  $s_0$ .
- A **goal description**  $s_*$ .
- A finite set  $\mathcal{A}$  of **axioms**.
- A finite set  $\mathcal{O}$  of **durative actions**.

# Temporal Numeric SAS<sup>+</sup> Planning Tasks

Representation of Subterms via Auxiliary Variable and Axioms

- **Axioms and auxiliary variables** used to represent **numeric and logic subterms**.
- Allows **sharing of subterms**.
- Convenient for heuristic computation.



# Temporal Numeric SAS<sup>+</sup> Planning Tasks

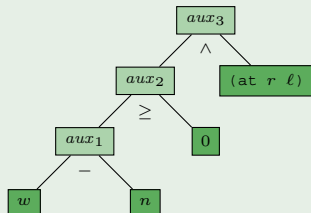
Representation of Subterms via Auxiliary Variable and Axioms

## Example (Auxiliary variables and axioms for subterms)

Consider the condition

$$\underbrace{(w - n \geq 0)}_{aux_1} \wedge (at\ r\ \ell)$$

$$\underbrace{\underbrace{aux_1}_{aux_2}}_{aux_3}$$



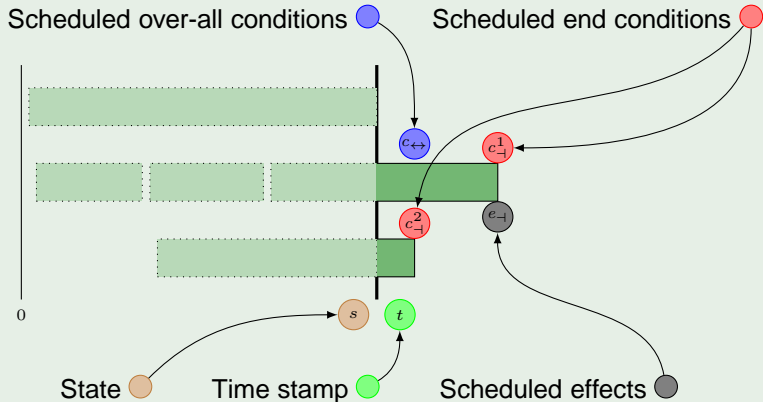
# Temporal Fast Downward (TFD)

- Extends **FAST DOWNWARD**.
- Uses FAST DOWNWARD architecture.
  - **Step 1: Translate** PDDL to temporal numeric SAS<sup>+</sup>.
  - **Step 2: Preprocess** temporal numeric SAS<sup>+</sup>.
  - **Step 3: Search** for plan. **[Topic of the rest of the talk]**
    - Best-first search.
    - Context-enhanced additive heuristic.
    - Deferred heuristic evaluation.
    - Preferred operators.

# Temporal Fast Downward Search

Search

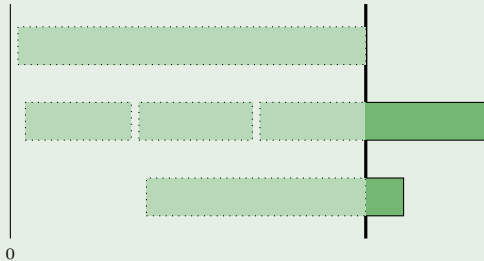
## Example (Time-stamped State)



# Temporal Fast Downward Search

Search

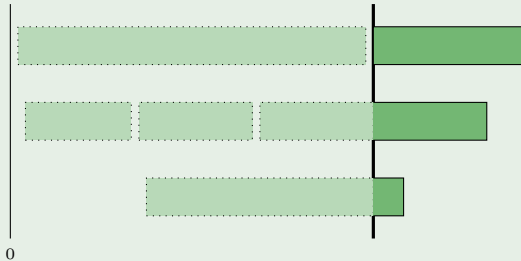
## Example (Time-stamped State)



# Temporal Fast Downward Search

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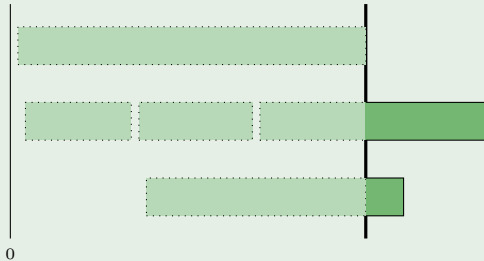
## Example (Time-stamped State)



# Temporal Fast Downward Search

Search

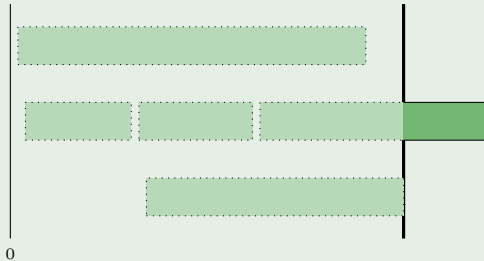
## Example (Time-stamped State)



# Temporal Fast Downward Search

Search

## Example (Time-stamped State)



# Context-Enhanced Additive Heuristic

- Idea:
  - Solve goals and
  - recursively take care of subgoals/preconditionsto **estimate makespan**.  
Return **accumulated costs**.
- **Local contexts**: Used to keep track of (side-)effects.
- **Drawback – inadmissibility**:
  - **Repeated solution** of subproblems.
  - Transformation to **instant-actions**.
  - **No concurrency-awareness**.
- **Advantage – preferred operators**:
  - **By-product** of heuristic.
  - Used to **guide search towards better operators**.



# Context-Enhanced Additive Heuristic

## Instant Actions

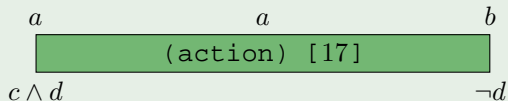
- **Problem:** Need to **simplify durative actions** for heuristic.
- **Solution:** **Ignore start-end distinction** for conditions and effects.
- **General form:** **instant action** = (conditions, effects, cost)

# Context-Enhanced Additive Heuristic

## Instant Actions

### Example (Compressed-action transitions)

Pretend that action happens instantly.



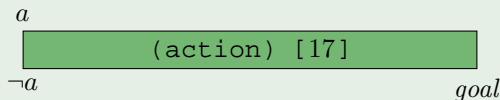
Corresponding compressed-action transitions:

- $cond = \{a, b\}; \quad eff = \{c, d, \neg d\}; \quad cost = 17$

# Context-Enhanced Additive Heuristic

## Instant Actions

### Example (Waiting transitions)



Assume that

- `action` is currently under execution and
- no other action can restore  $a$ , and we need the end-effect  $goal$ .

Then the other types of instant actions do not help in reaching  $goal$ , even though we can actually obtain  $goal$  by waiting long enough.

Corresponding waiting transitions:

- $cond = \emptyset$ ;  $eff = \{goal\}$ ;  $cost = \Delta t$

# Context-Enhanced Additive Heuristic

## Instant Actions

### Example (Axiom transitions)

All axioms are interpreted as instant actions with cost 0.

# Context-Enhanced Additive Heuristic

## Local Problems

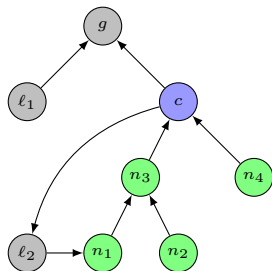
A **local problem** answers the question:

“What does it cost to change the value of  $v$  from  $w$  to  $w'$ ?”

# Context-Enhanced Additive Heuristic

## Example

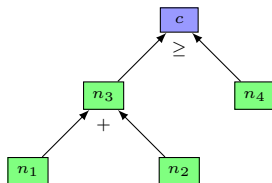
Causal graph



Current state:  $g = F$

Goal:  $g = T$

Comparison axiom



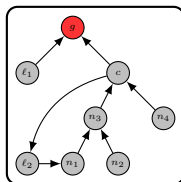
# Context-Enhanced Additive Heuristic

## Example

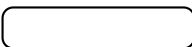
$h$  = accumulated cost

0

Causal Graph

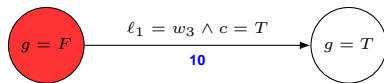


Queue



Local context of active node

$n_1 = -10$	$c = F$
$n_2 = +5$	$l_1 = w_1$
$n_3 = -5$	$l_2 = w_1$
$n_4 = 0$	$g = F$



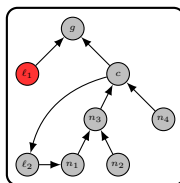
# Context-Enhanced Additive Heuristic

## Example

$h$  = accumulated cost

0

Causal Graph

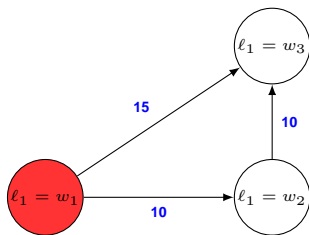


Queue

$\ell_1 = w_1$

Local context of active node

$n_1 = -10$	$c = F$
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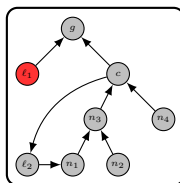
# Context-Enhanced Additive Heuristic

## Example

$h$  = accumulated cost

0

Causal Graph

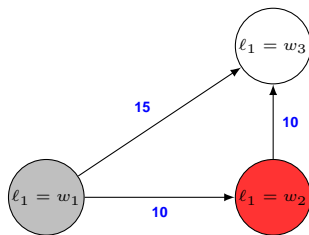


Queue

$\ell_1 = w_2$   $\ell_1 = w_3$

Local context of active node

$n_1 = -10$	$c = F$
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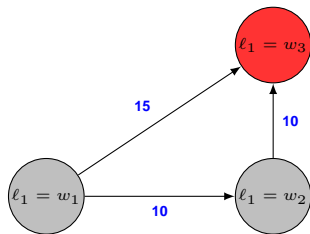


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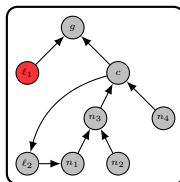
## Example

$h$  = accumulated cost

15



Causal Graph



Queue

$l_1 = w_3$

Local context of active node

$n_1 = -10$	$c = F$
$n_2 = +5$	$l_1 = w_3$
$n_3 = -5$	$l_2 = w_1$
$n_4 = 0$	$g = F$

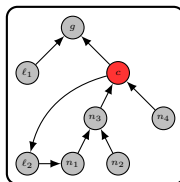
# Context-Enhanced Additive Heuristic

## Example

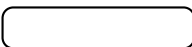
$h$  = accumulated cost

15

Causal Graph

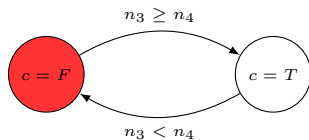


Queue



Local context of active node

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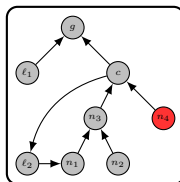
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Causal Graph



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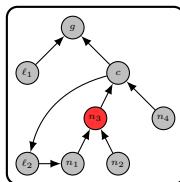
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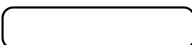
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Causal Graph

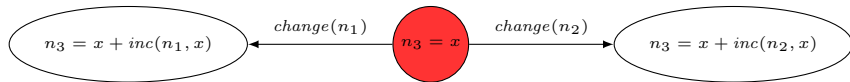


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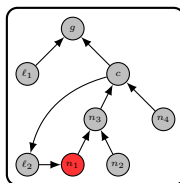
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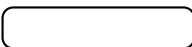
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Causal Graph

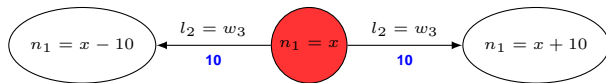


Queue



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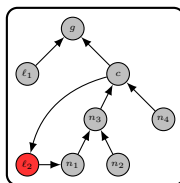
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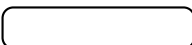
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Causal Graph

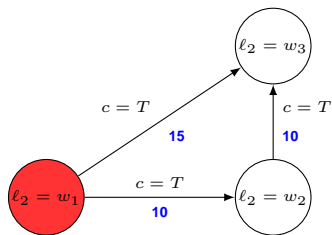


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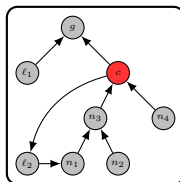
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## Example

$h$  = accumulated cost

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Causal Graph

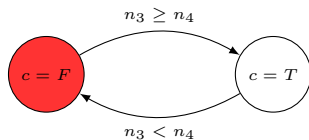


Queue



Local context of active node

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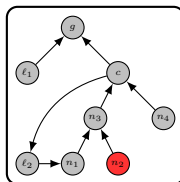
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## Example

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15

Causal Graph

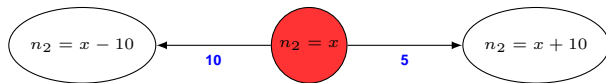


Queue

$n_2 = +15$

Local context of active node

$n_1 = -10$	$c = F$
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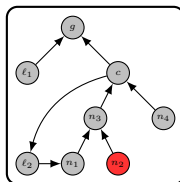
# Context-Enhanced Additive Heuristic

## Example

$h$  = accumulated cost

20

Causal Graph

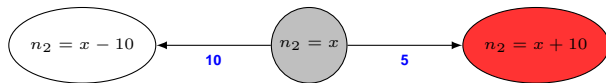


Queue

$n_3 = +5$

Local context of active node

$n_1 = -10$	$c = F$
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$n_3 = -5$	$l_2 = w_1$
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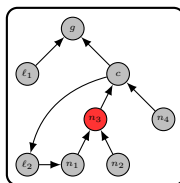
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$h$  = accumulated cost

20

Causal Graph

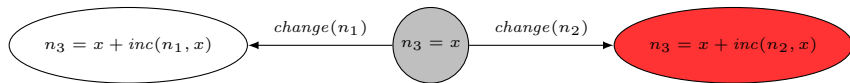


Queue

$c = T$

Local context of active node

$n_1 = -10$	$c = F$
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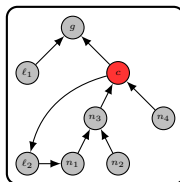
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$h$  = accumulated cost

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Causal Graph

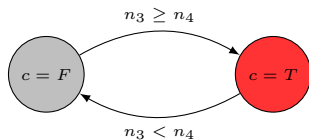


Queue

$g = T$

Local context of active node

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$n_3 = +5$	$l_2 = w_1$
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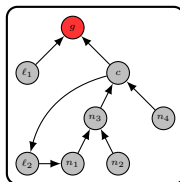
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## Example

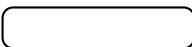
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20

Causal Graph

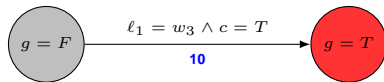


Queue



Local context of active node

$n_1 = -10$	$c = F$
$n_2 = +5$	$l_1 = w_1$
$n_3 = -5$	$l_2 = w_1$
$n_4 = 0$	$g = F$



# Experiments

## Setting

- **Planners:** Six temporal planning systems.
- **Benchmarks:** IPC 2008 deterministic temporal problems.
- **Evaluation Scheme:** Scheme used at IPC 2008

$$Score(Planner) = \sum_{\substack{\text{solved} \\ \text{problem } \pi \\ \text{(solution } p)}} \frac{\min_{\text{solution } p^* \text{ for } \pi} makespan(p^*)}{makespan(p)}$$

- **Environment:** 2.66 GHz Intel Xeon CPU, 2 GB memory limit, 30 minutes time limit per problem, anytime search.

# Experimental Results

Planners' Scores

Domain	Base	Crikey	LPG	Sapa	SGP	TFD
Crewplanning	16.19	22.59	12.76	—	22.44	28.72
Elevators	18.38	2.60	22.75	5.64	15.09	19.38
Modeltrain	11.92	—	—	—	11.11	0.96
Openstacks	18.14	20.67	14.35	25.90	12.49	26.66
Parcprinter	13.84	8.58	18.20	5.25	11.00	9.10
Pegsol	24.35	18.30	25.81	18.98	15.39	27.57
Sokoban	15.52	7.03	11.95	0.00	8.73	13.00
Transport	5.50	2.83	11.57	1.91	7.46	6.91
Woodworking	12.14	11.96	26.37	9.36	10.44	16.04
Overall	<b>135.97</b>	<b>94.55</b>	<b>143.76</b>	<b>67.02</b>	<b>114.15</b>	<b>148.34</b>

# Experimental Results

## Interpretation

- TEMPORAL FAST DOWNWARD scores highest.
- Reason for high score:
  - Not so much number of solved problems ...
  - ... but rather solution quality.



# Experimental Results

How Much Longer the Plans From Other Planners Are On Average

Domain	Base	Crikey	LPG	Sapa	SGP
Crewplanning	(18) 14%	(29) 38%	(13) 1%	—	(28) 39%
Elevators	(17) 58%	(10) 200%	(23) 11%	(12) 126%	(17) 84%
Modeltrain	(1) 5%	—	—	—	(1) 1%
Openstacks	(30) 55%	(30) 33%	(30) 166%	(30) 4%	(30) 144%
Parcprinter	(13) 37%	(13) 34%	(12) -30%	(5) 12%	(13) 32%
Pegsol	(28) 19%	(28) 60%	(28) 12%	(24) 28%	(18) 21%
Sokoban	(13) 29%	(9) 50%	(12) 50%	—	(9) 22%
Transport	(7) 18%	(6) 79%	(7) -25%	(3) 54%	(10) 37%
Woodworking	(27) 42%	(27) 44%	(28) -34%	(20) 37%	(21) 29%
Overall	(154) 36%	(152) 55%	(153) 31%	(94) 35%	(147) 60%

# Summary and Conclusion

- **Temporal** and **numeric** planning via **forward search** in space of time-stamped states.
- Heuristic guidance by extension of **context-enhanced additive heuristic**.
- **Competitive** with other approaches to temporal planning.

# Future Work

- Make heuristic concurrency-aware.
- Use weaker relaxation of numeric features in heuristic.