

Formal Representations of Classical Planning Domains

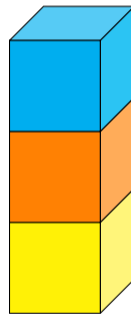
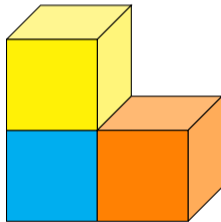
Claudia Grundke Gabriele Röger Malte Helmert

University of Basel

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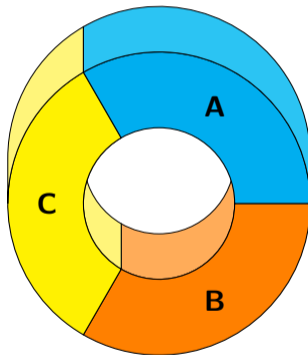
Blocksworld

$on(x, y)$
 $ontable(x)$
 $clear(x)$



Blocksworld?

$on(A, B)$
 $on(B, C)$
 $on(C, A)$



Who cares?

Domain Description + ~~Task Description~~

- Generalized Planning (e. g. Srivastava et al., 2011)
- Automated Instance Generation
- Reasoning over Domains

Aims

We want

- a formalism to describe domains precisely,
- it to be based on PDDL,
- to efficiently check if a task belongs to a domain.

PDDL Axioms

$$\mathit{above}(x, y) \leftarrow \mathit{on}(x, y) \vee \exists z (\mathit{on}(x, z) \wedge \mathit{above}(z, y))$$

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$$\mathit{above}(x, y) \leftarrow \mathit{on}(x, y) \vee \exists z (\mathit{on}(x, z) \wedge \mathit{above}(z, y))$$

$$\mathit{illegal}() \leftarrow \exists x \mathit{above}(x, x)$$

$$\mathit{illegal}() \leftarrow \dots$$

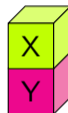
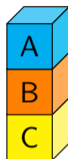


Fixed Goal Condition

All tasks of a domain **share same first-order goal**.

Example (full-ADL Miconic): $\forall p (passenger(p) \rightarrow served(p))$

Moving Goal into Initial State

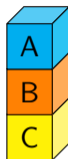


Goal:
New static atoms:

$on(A, B) \wedge on(B, C)$
 $on^g(A, B), on^g(B, C)$

$on(X, Y)$
 $on^g(X, Y)$

Moving Goal into Initial State



Goal:
New static atoms:

$$\cancel{on(A, B)} \wedge \cancel{on(B, C)}$$

$$on^g(A, B), on^g(B, C)$$

$$\cancel{on(X, Y)}$$

$$on^g(X, Y)$$

Shared goal:

$$\forall x, x' (on^g(x, x') \rightarrow on(x, x'))$$

Aims

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- a formalism to describe domains precisely,
- it to be based on PDDL,
- to efficiently check if a task belongs to a domain.
- **Maximal expressiveness.**

Linear Order

Even number of blocks?

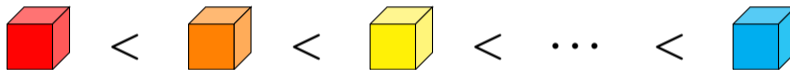


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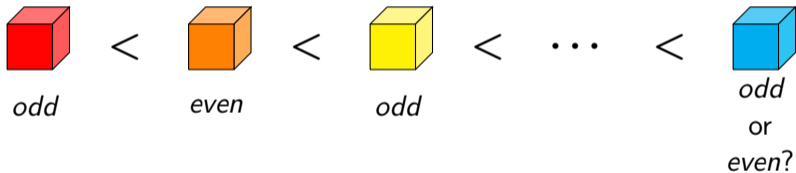
Linear Order

Even number of blocks?



Linear Order

Even number of blocks?



illegal if largest block is *odd*

Capturing P

With linear orders our formalism (using PDDL axioms) can express any polynomial-time algorithm that can decide if a task is legal. (Immerman-Vardi Theorem)

Summary



Link to our paper
[Formal Representations
of Classical Planning
Domains](#)

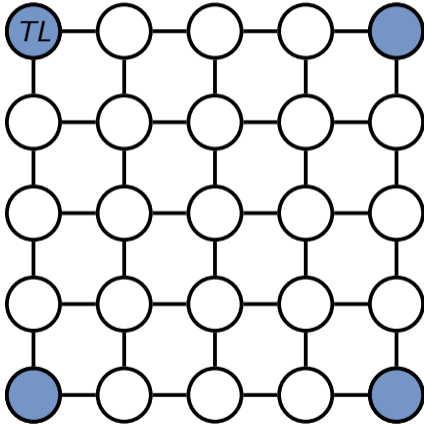
Using PDDL axioms we can restrict which states are **legal initial states** for tasks of a domain.

- Given a linear order our formalism captures **polynomial-time decision algorithms**.

All tasks of a domain share same first-order goal.

- Move conjunctive goals into initial state to preserve them.

Linear Order: Grid Graph



$$corner(x) \leftarrow degree_{\geq 2}(x) \wedge \neg degree_{\geq 3}(x)$$

$$TL(x) \leftarrow corner(x) \wedge \neg \exists y (corner(y) \wedge y < x)$$