

# Cost-Partitioned Merge-and-Shrink Heuristics for Optimal Classical Planning

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## TL;DR

### Setting/Background

- ▶ classical planning
- ▶ merge-and-shrink (M&S) framework
- ▶ cost partitioning (CP): optimal and saturated (OCP/SCP)

### Goals/Contributions

- ▶ investigate how CP can be applied for M&S
- ▶ investigate how M&S interacts with CP
- ▶ improve M&S heuristics through CP in practice

## Theoretical Contributions

### Label Cost Partitioning

cost partitioning defined for factored transition systems:

- ▶ works with label reduction (labels differ from original labels used in the cost partitioning)
- ▶ works with factors from different factored transition systems (factors can have different labels)

### Impact of M&S Transformations on CP Heuristics

transformation	OCP	SCP
exact label reduction	preserved	preserved
$h$ -preserving shrinking	not increased	preserved
merging	not decreased	incomparable

## Merge-and-Shrink Algorithm with SCP Added

**procedure** MERGEANDSHRINK(Planning Task  $\Pi$ )

$F \leftarrow$  factored transition system of  $\Pi$

$\mathcal{H} \leftarrow \emptyset$

**while not** TERMINATE() **do**

apply label reduction to  $F$

$\mathcal{H} \leftarrow \mathcal{H} \cup \{\text{COMPUTESCP}(F)\}$

select two factors  $\Theta_i, \Theta_j$  from  $F$

optionally shrink  $\Theta_i$  and/or  $\Theta_j$

replace  $\Theta_i$  and  $\Theta_j$  by their product in  $F$

**end while**

$\mathcal{H} \leftarrow \mathcal{H} \cup \{\text{COMPUTESCP}(F)\}$

**return**  $h^{\text{M\&S}} = \max_{\Theta \in F} h_{\Theta}^*$

▷ original M&S

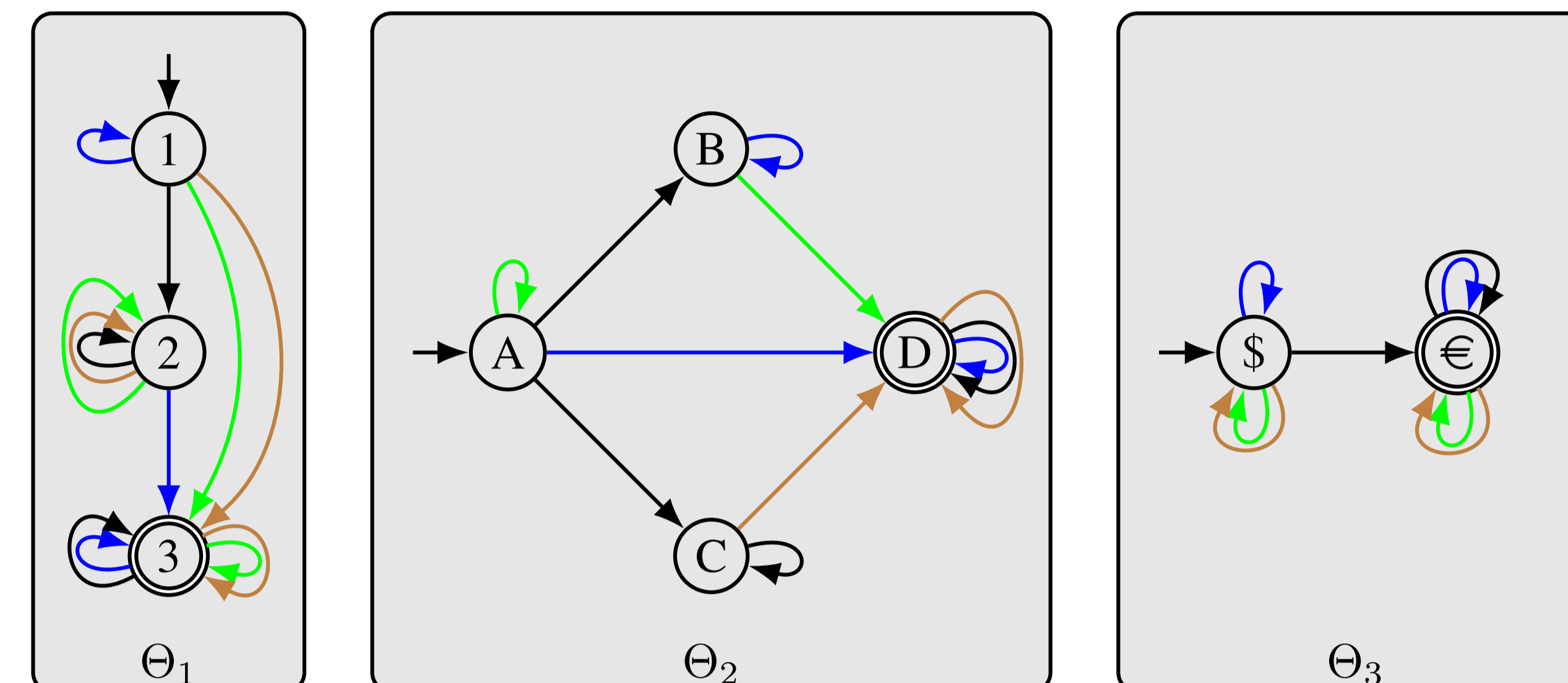
**return**  $h^{\text{M\&S+SCP}} = \max_{h \in \mathcal{H}}$

▷ M&S + SCP

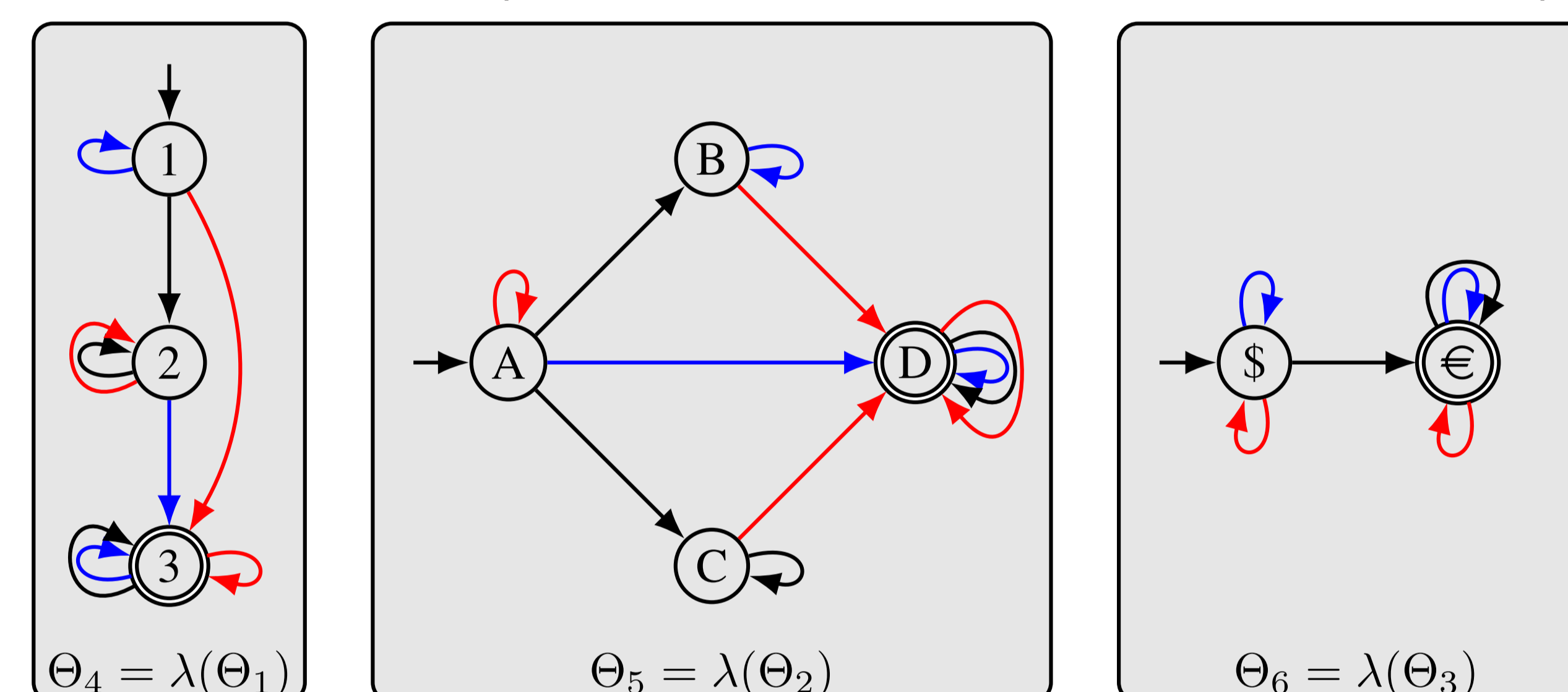
**end procedure**

## Initialization and First Iteration of M&S

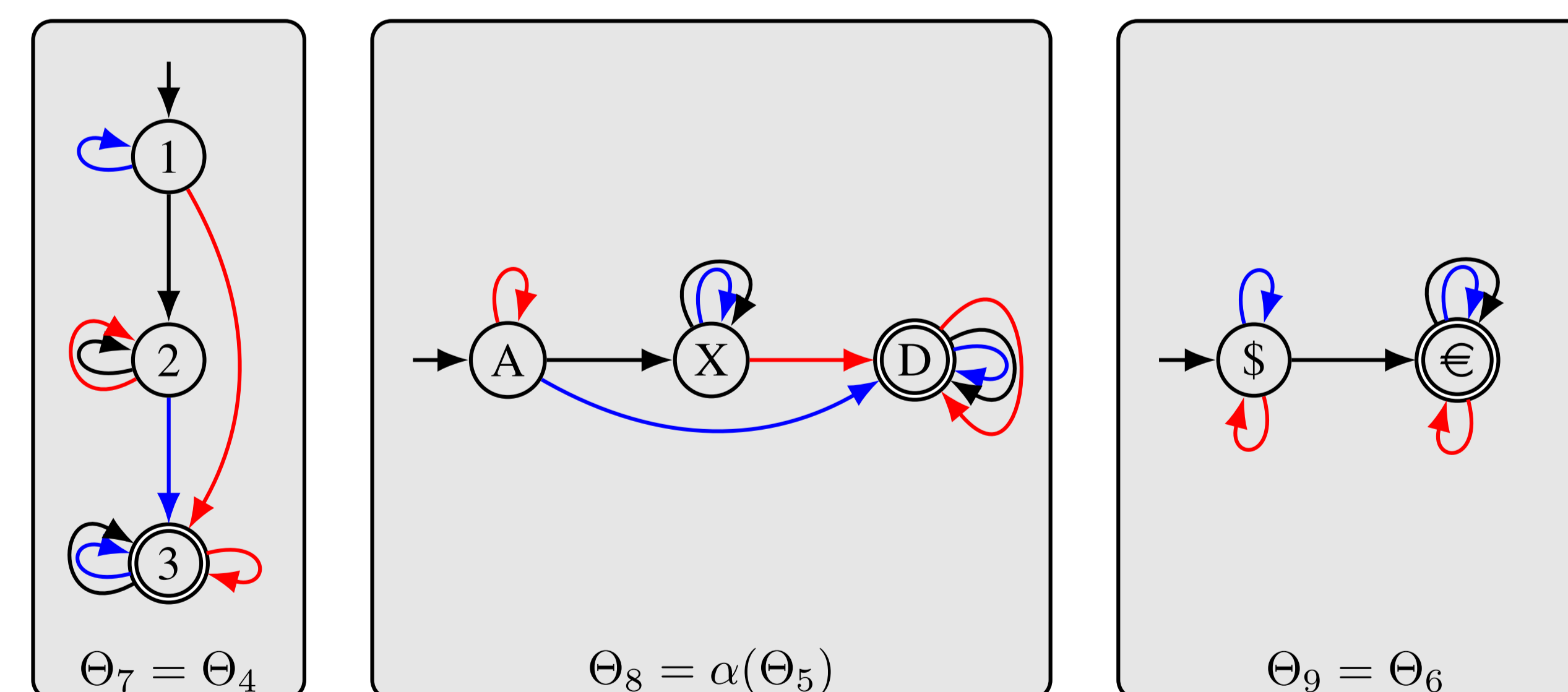
atomic FTS:



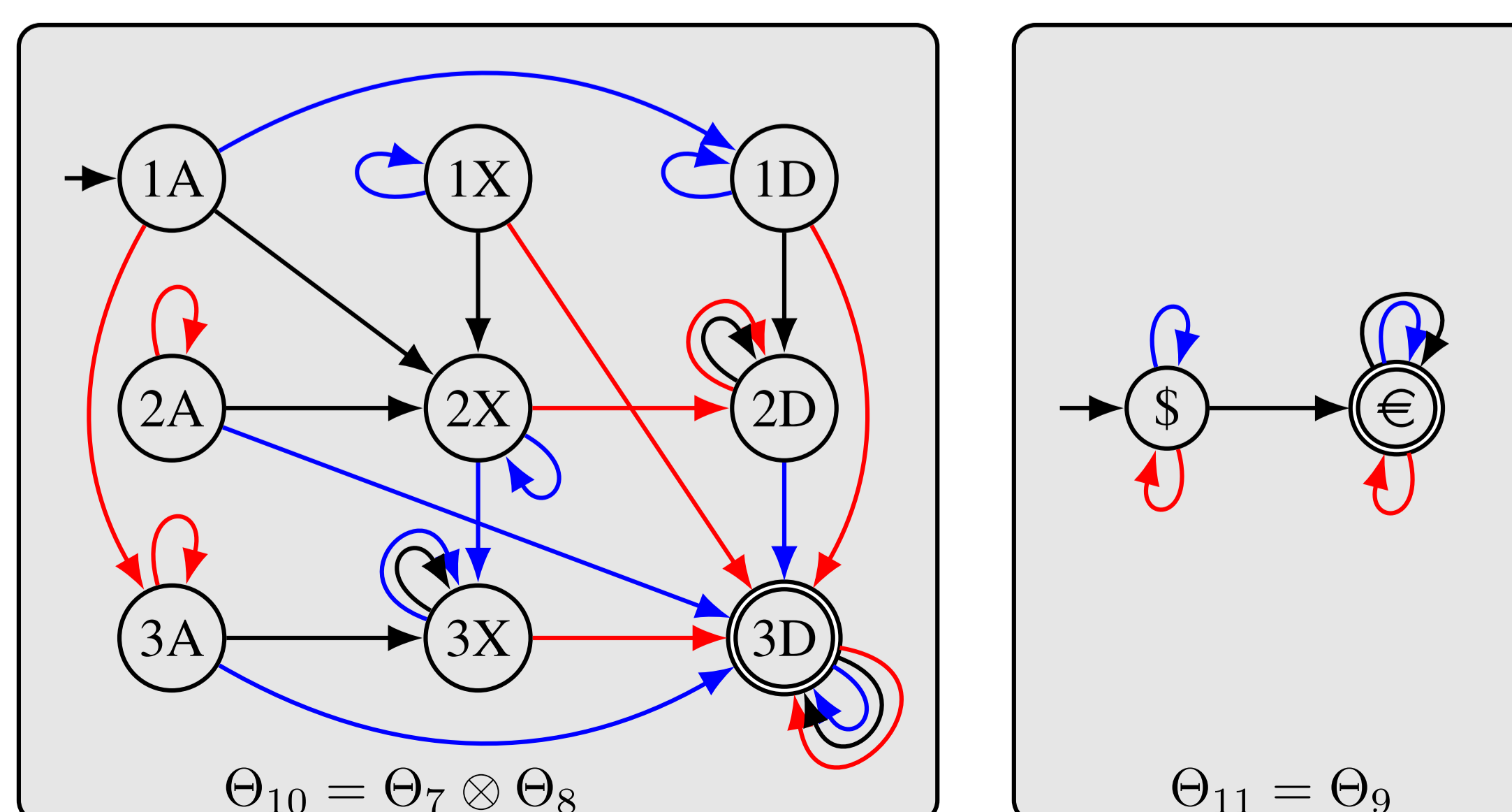
after label reduction (with label mapping  $\lambda$  applied to all factors):



after shrinking (with abstraction  $\alpha$  applied to  $\Theta_5$ ):



after merging (of  $\Theta_7$  and  $\Theta_8$ ):



## Heuristic Values for the Example

perfect heuristic

$$h^*(init) = 3$$

(example optimal plan:  $\rightarrow \rightarrow \rightarrow$ )

best SCP in iteration 1  
(over  $F = \langle \Theta_4, \Theta_5, \Theta_6 \rangle$ )

$$h_{(4,5,6)}^{\text{M\&S+SCP}}(init) = 1 + 0 + 1 = 2$$

best SCP after main loop  
(over final  $F = \langle \Theta_{10}, \Theta_{11} \rangle$ )

$$h_{(10,11)}^{\text{M\&S+SCP}}(init) = 2 + 1 = 3$$

original M&S heuristic  
(over final  $F = \langle \Theta_{10}, \Theta_{11} \rangle$ )

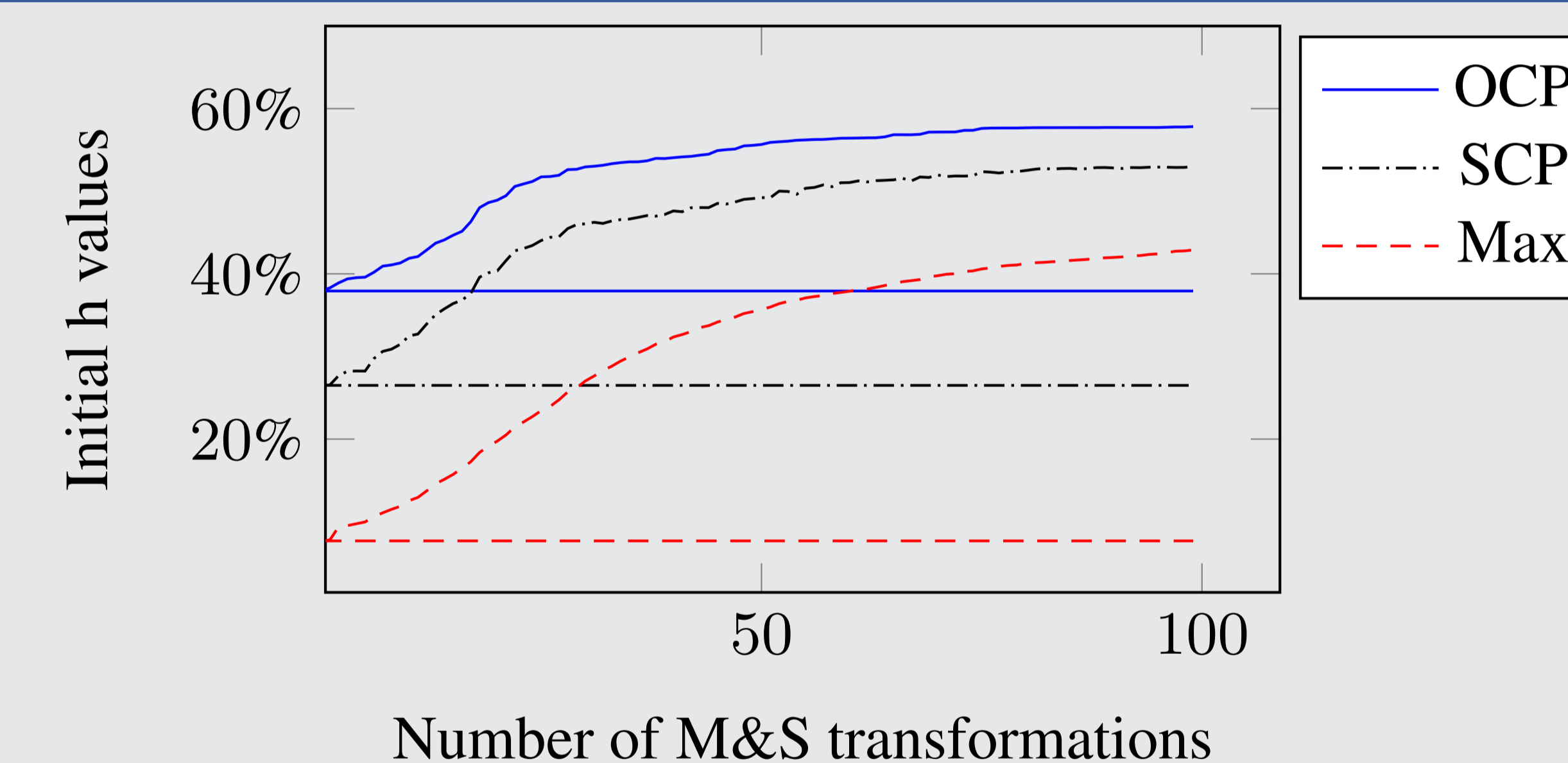
$$h^{\text{M\&S}}(init) = \max(2, 1) = 2$$

M&S+SCP heuristic  
(max over collected SCPs)

$$h^{\text{M\&S+SCP}}(init) = \max(2, 3) = 3$$

## Experiments

### SCP vs OCP



### How often to Compute an SCP & Memory-efficient Variant

	after label reduction			
	$i = 1$	$i = 2$	$i = 5$	$i = 10$
full	922	923	923	916
shallow	<b>933</b>	930	926	917

### When to Compute an SCP

	$i = 1$ , shallow
after label r.	<b>933</b>
after shrinking	<b>933</b>
after merging	925

### Comparing Interleaved and Offline SCPs computed over Different Orders/with Order Diversification Strategies

		rnd	otn	nto	mhsc	mh	msc
$h_{int}^{\text{SCP}}$	<b>933</b>	932	928	928	927	930	
$h_{off}^{\text{SCP}}$	841	836	905	869	905	837	
$h_{off-div}^{\text{SCP}}$	915	841	904	887	907	838	