

Merge-and-Shrink Task Reformulation for Classical Planning

Álvaro Torralba, Silvan Sievers

HSDIP 2019

Classical Planning

Definition. A *planning task* is a 4-tuple $\Pi = (V, A, I, G)$ where:

- V is a set of *state variables*, each $v \in V$ with a finite *domain* D_v .
- A is a set of *actions*; each $a \in A$ is a triple (pre_a, eff_a, c_a) , of *precondition* and *effect* (partial assignments), and the action's *cost* $c_a \in \mathbb{R}_0^+$.
- *Initial state* I (complete assignment), *goal* G (partial assignment).

→ **Solution (“Plan”):** Action sequence mapping I into s s.t. $s \models G$.

Classical Planning

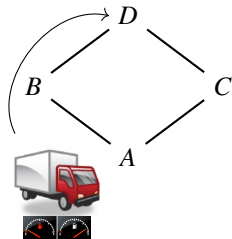
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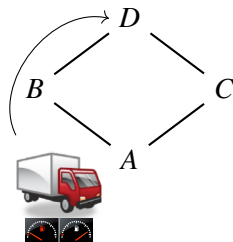
Running Example:

- $V = \{T, F\}$ with $D_t = \{A, B, C, D\}$,
 $D_F = \{0, 1, 2\}$.
- $A = \{drive(x, x', f, f')\}$
- $I = \{T = A, F = 2\}$
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Accidental Complexity

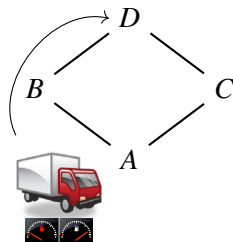
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Accidental complexity: when solving the problem is harder due to how it is encoded

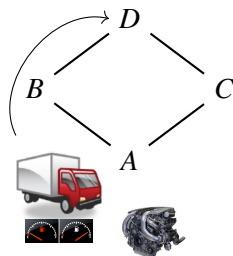
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Accidental complexity: when solving the problem is harder due to how it is encoded

- $V = \{T, F, E\}$ with $D_t = \{A, B, C, D\}$,
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Reformulation

Transform the model to get rid of “accidental” complexity

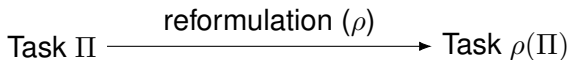
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Task II

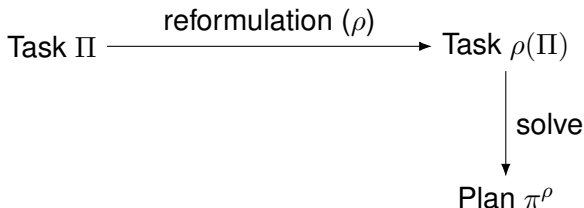
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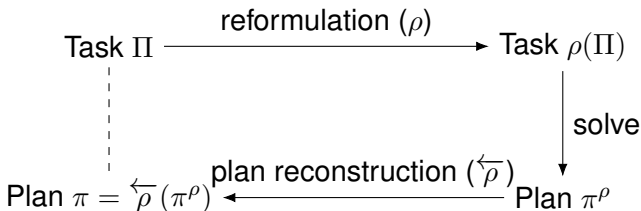
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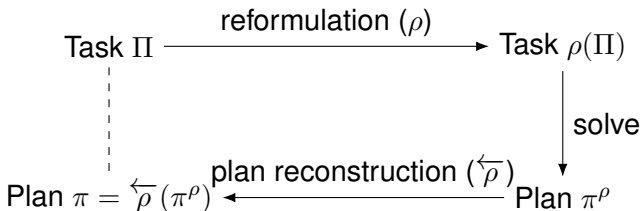
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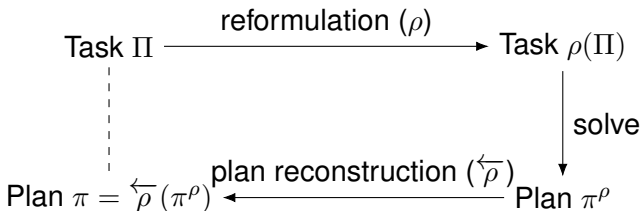


Properties:

- Polynomial: ρ and $\overleftarrow{\rho}$ run in polynomial time in the $|\Pi|$ and $|\overleftarrow{\rho}(\pi^\rho)|$.

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- Polynomial: ρ and $\overleftarrow{\rho}$ run in polynomial time in the $|\Pi|$ and $|\overleftarrow{\rho}(\pi^\rho)|$.
- Optimal: π^ρ is optimal for $\rho(\Pi) \Rightarrow \overleftarrow{\rho}(\pi^\rho)$

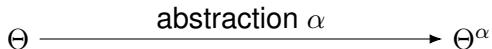
Abstraction Heuristics

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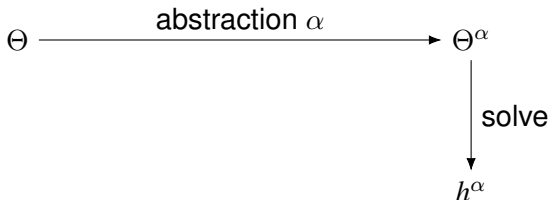
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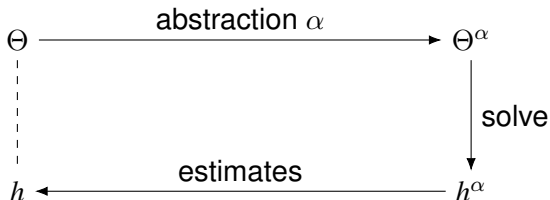
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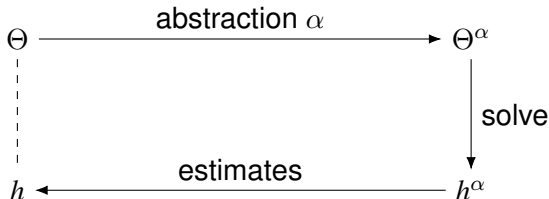
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Abstraction Heuristics



Abstraction Heuristics



→ An abstraction is **refinable** if a solution for the abstract task can be transformed in polynomial time in a solution for the original

FDR Reformulation

Free DTG: The domain transition graph of a variable only considering **actions without preconditions or effects on other variables**.

Variable Abstraction (Helmert, 2006)

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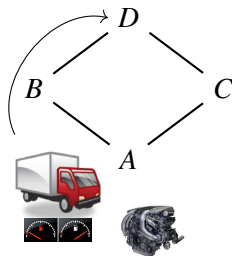
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Extensions:

- Haslum (2007) gave a stronger criteria
- Tozicka et al. (2016) use this to merge values of a variable

Running Example with Accidental Complexity

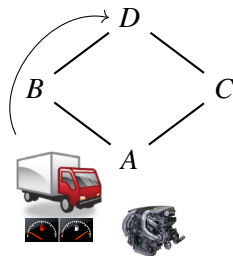
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→ Before turning on the engine, we need to check that we have 2 units of fuel with the check-fuel action

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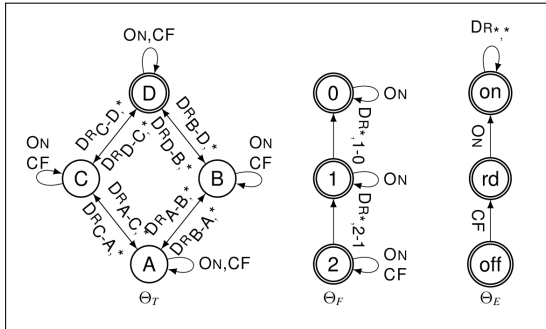
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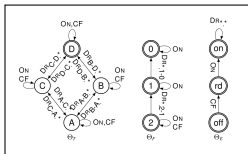
- | | |
|---|--|
| <ul style="list-style-type: none"> • check-fuel:
pre: E=off, F=2
eff: E=rd | <ul style="list-style-type: none"> • turn-on:
pre: E=rd
eff: E=on |
|---|--|

Merge-and-Shrink



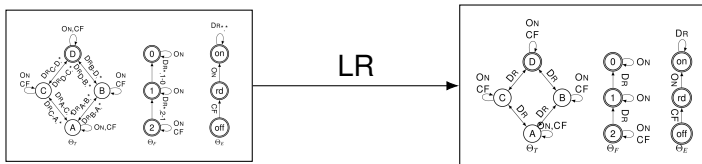
Atomic: One TS per variable such that $\Theta_1 \otimes \Theta_2 \otimes \Theta_3 = \Theta$

Merge-and-Shrink



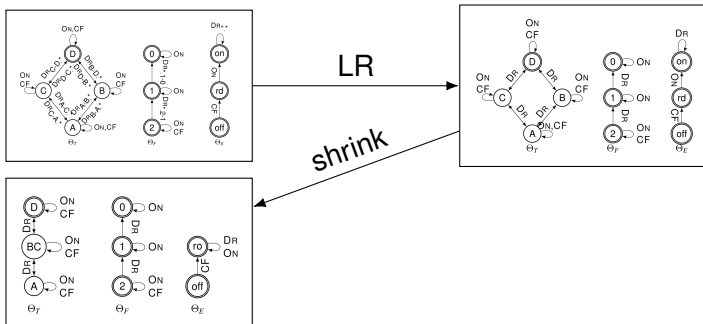
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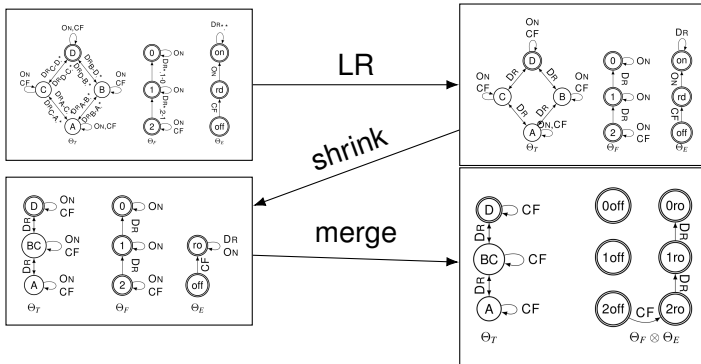
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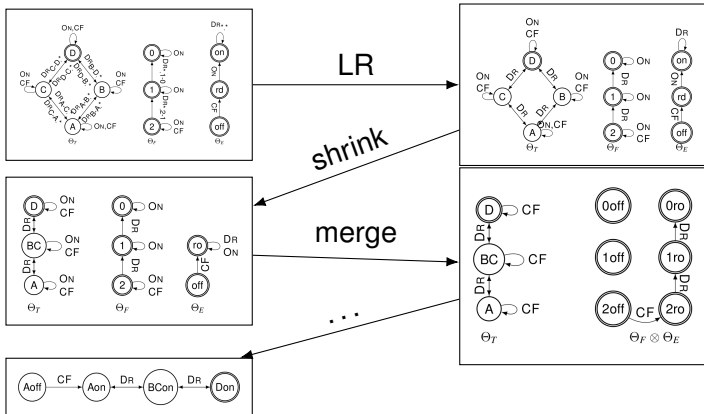
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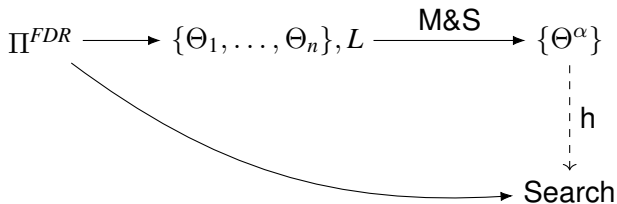
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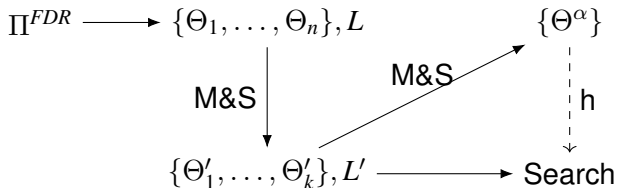


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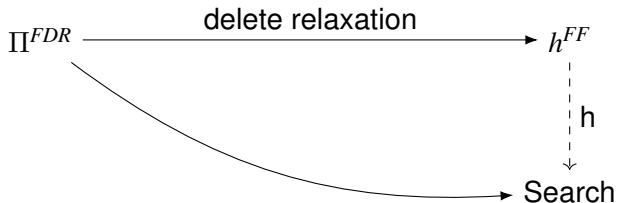
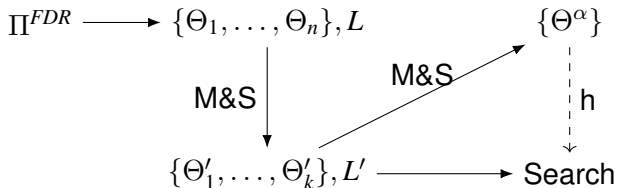
M&S as Reformulation Framework



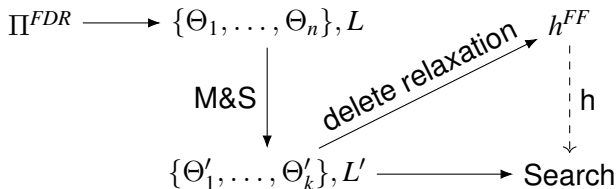
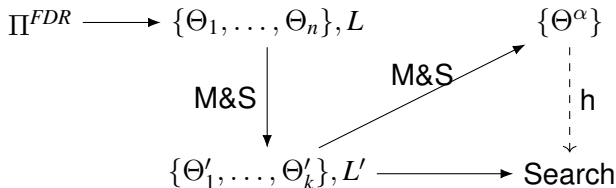
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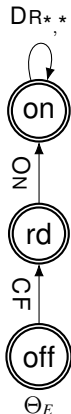
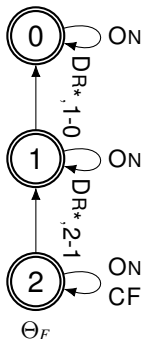
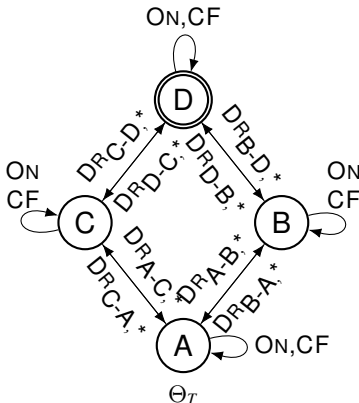
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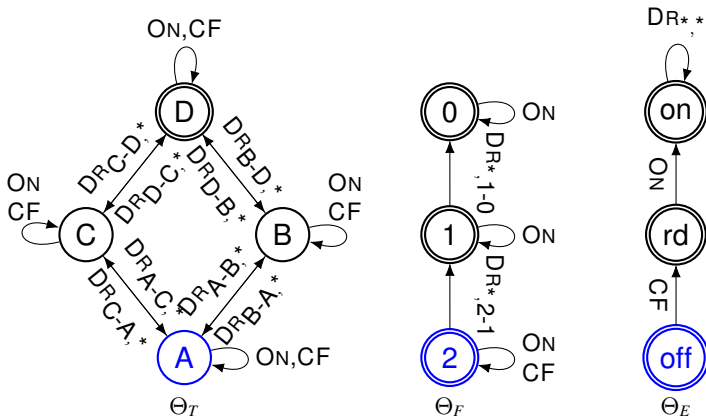
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FTS Representation and Successor Generation

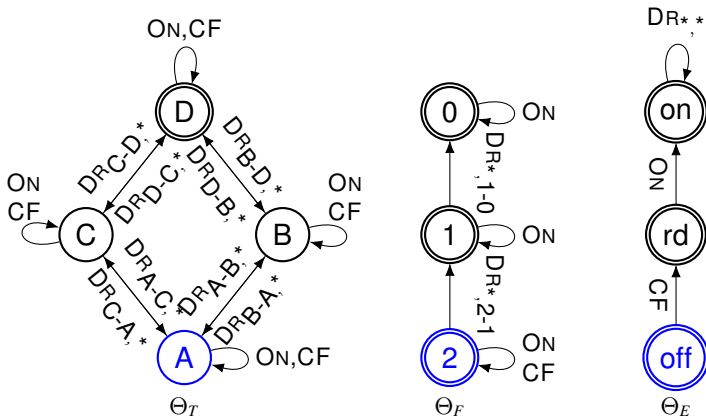


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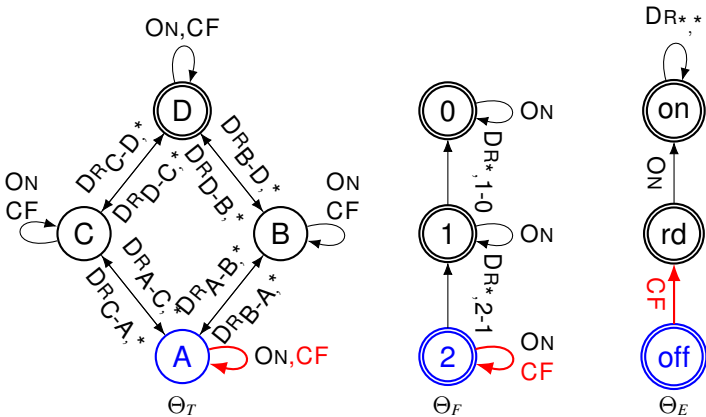


State: $\langle T=A, F=2, E=off \rangle$

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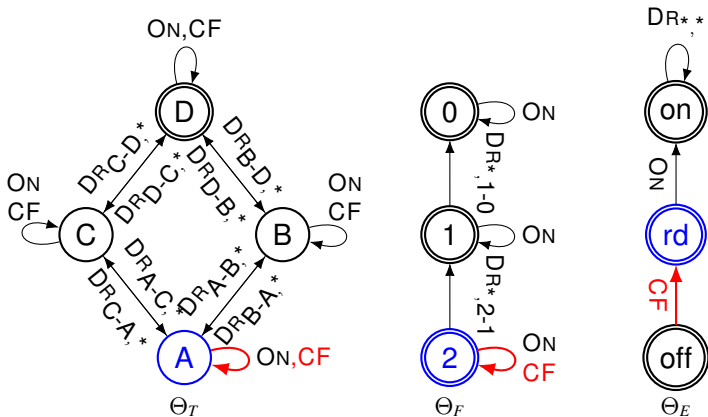


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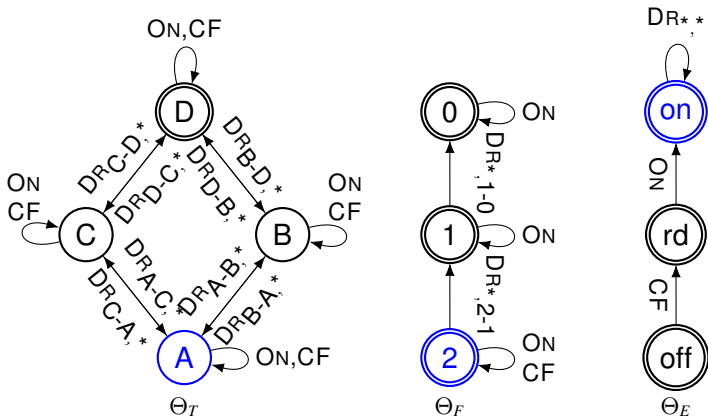


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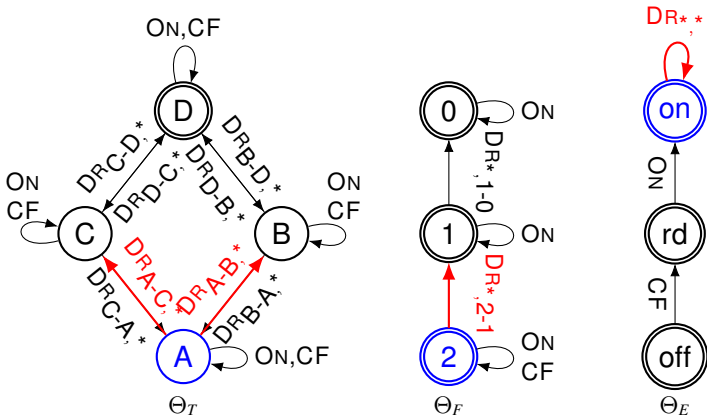
Successor: $\langle T=A, F=2, E=rd \rangle$

FTS Representation and Successor Generation



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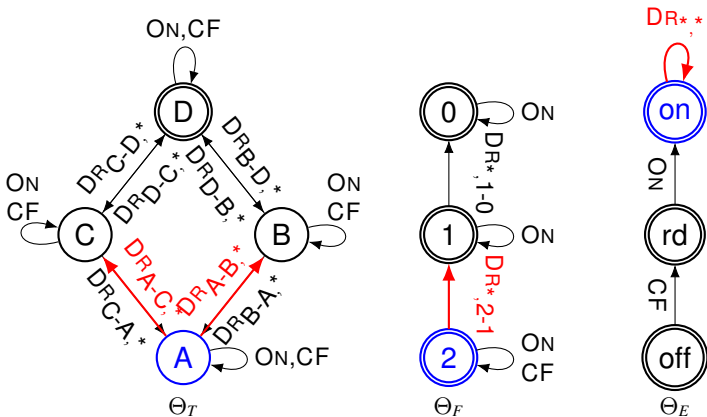
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FTS Representation and Successor Generation



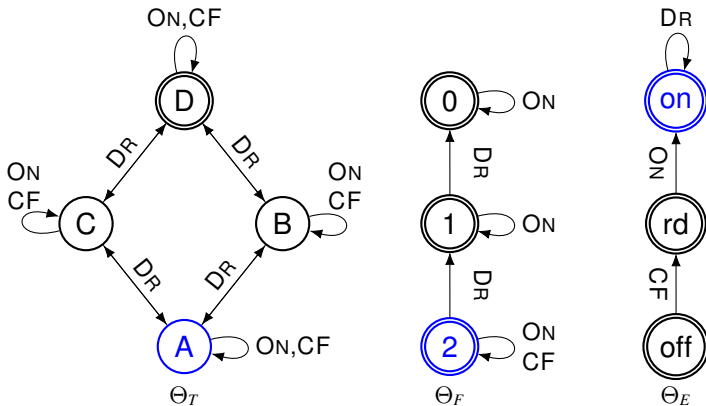
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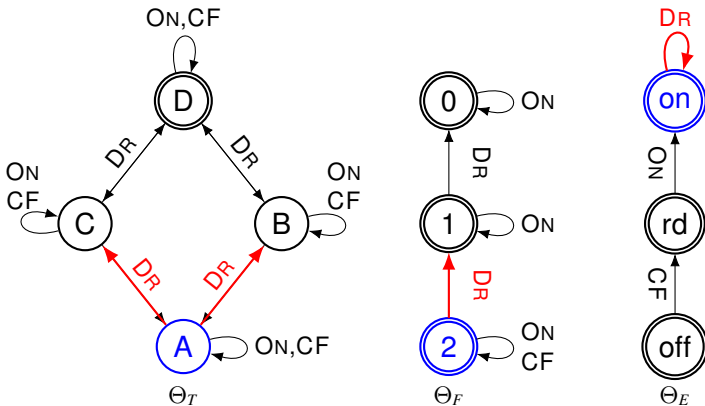
Successor ($DR_{A-B,2-1}$): $\langle T=B, F=1, E=on \rangle$

Successor ($DR_{A-C,2-1}$): $\langle T=C, F=1, E=on \rangle$

FTS Representation and Successor Generation



FTS Representation and Successor Generation



State: $\langle T=A, F=2, E=on \rangle$

Applicable labels: $\{DR\}$

Successor (DR): $\langle T=B, F=1, E=on \rangle$

Successor (DR): $\langle T=C, F=1, E=on \rangle$

What's the Difference Anyway?

Advantage of FTS over FDR:

- Limited form of disjunctive preconditions
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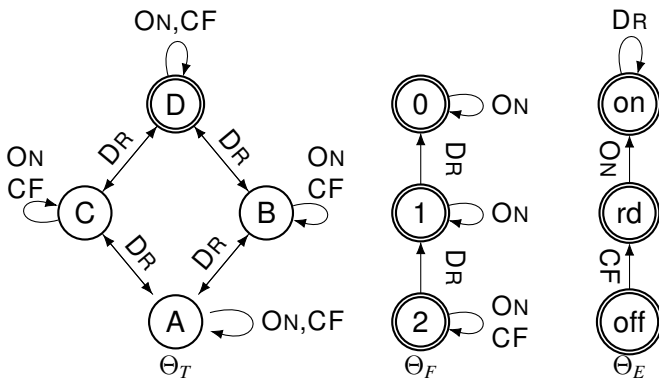
Replaces a TS Θ_i by an abstraction thereof ($\alpha(\Theta_i)$)

The state space of the new task is an abstraction of the original

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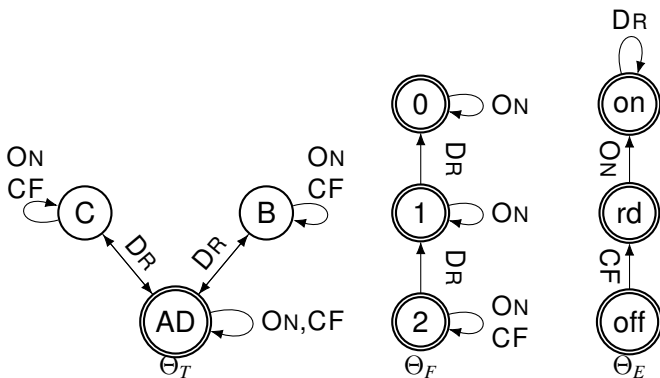
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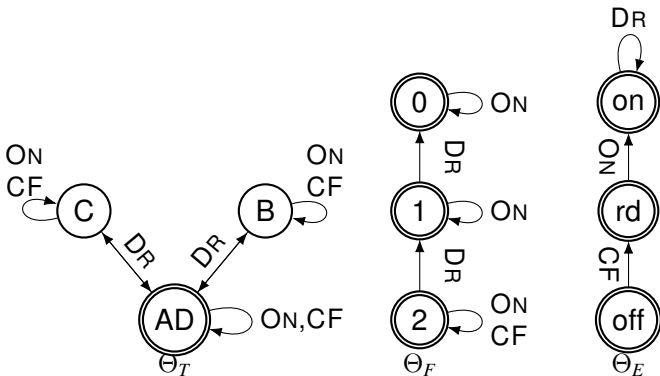
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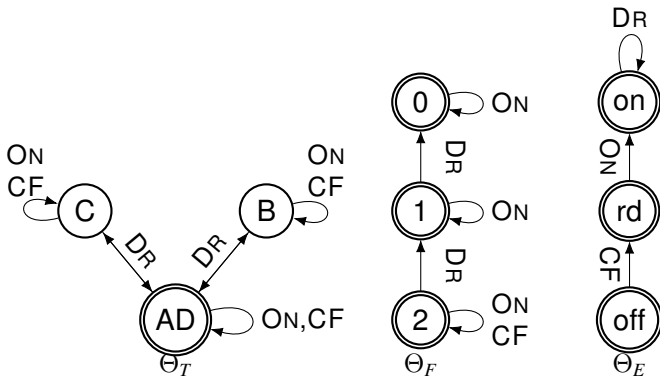


Plan = $\langle \rangle$

Shrink

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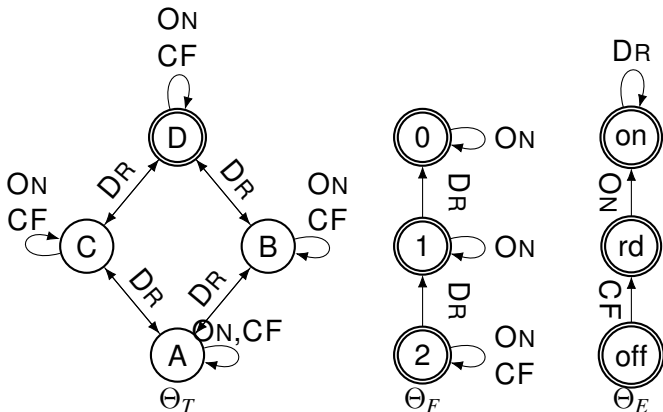
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Plan = $\langle \rangle \Rightarrow$ Only “refinable” abstractions are suitable for reformulation

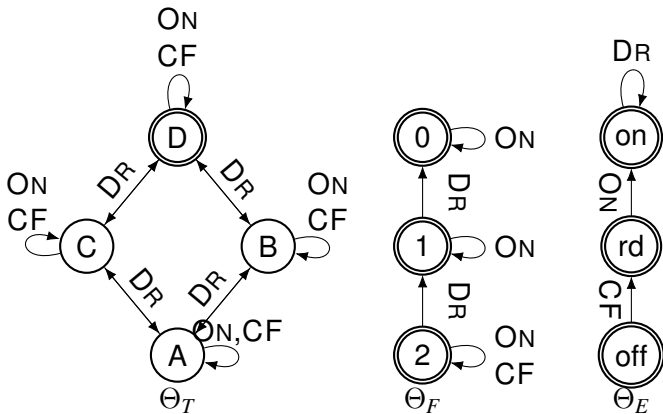
(Strong) Bisimulation Shrinking

Two states are equivalent if they have the same outgoing transitions



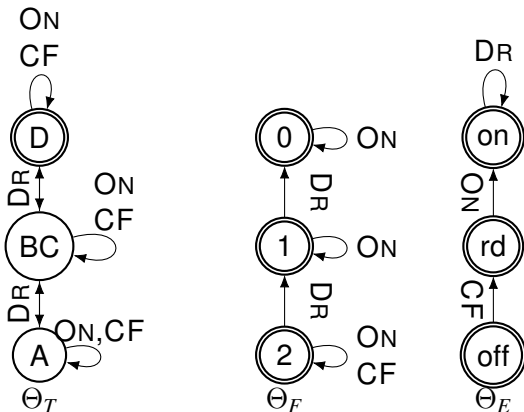
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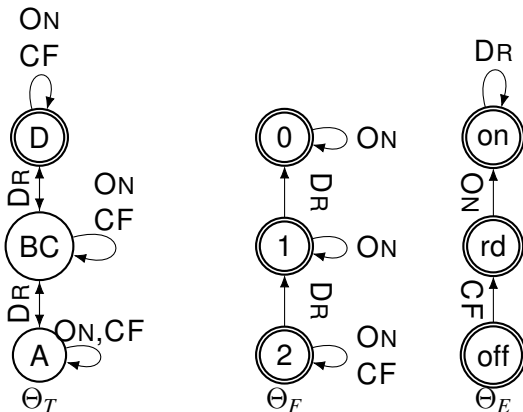
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Plan = $\langle CF, ON, DR(BC), DR(D) \rangle \rightarrow$

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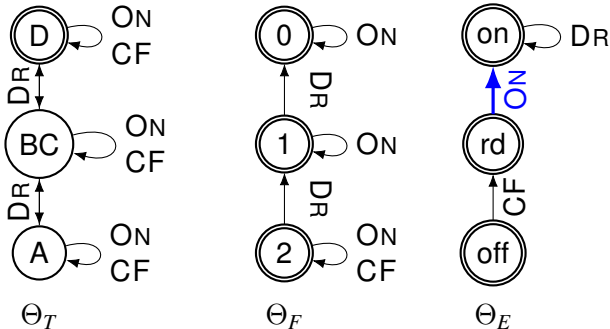
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Plan = $\langle CF, ON, DR(BC), DR(D) \rangle \rightarrow \langle CF, ON, DR(B), DR(D) \rangle$

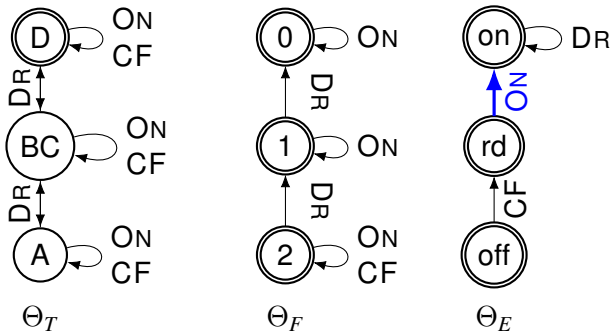
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- 1 Identify τ labels that are internal to a TS (self-loop everywhere)



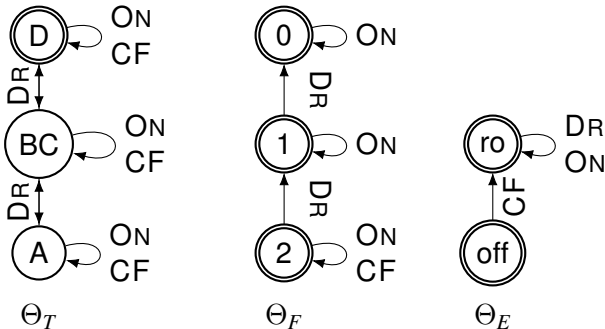
Weak Bisimulation Shrinking

- 1 Identify τ labels that are internal to a TS (self-loop everywhere)
- 2 Bisimulation allowing free-use of τ labels



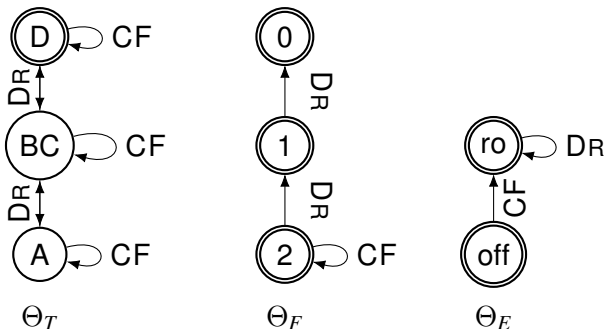
Weak Bisimulation Shrinking

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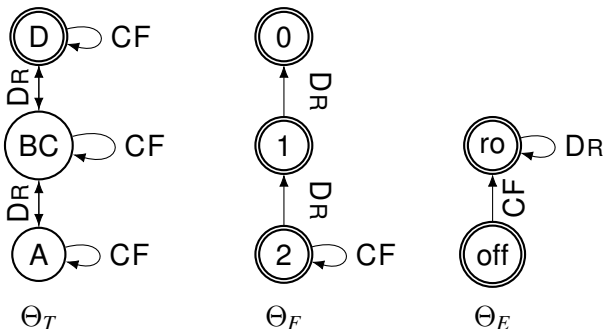
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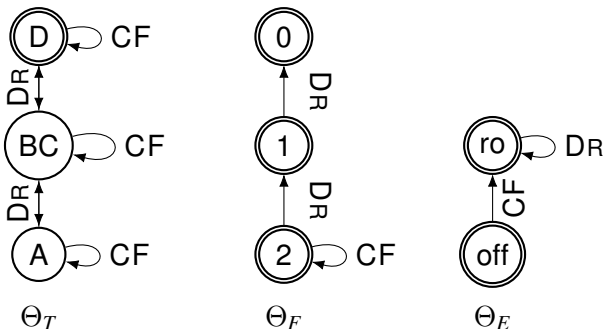
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Plan = $\langle \text{CF}, \text{DR}(BC), \text{DR}(D) \rangle \rightarrow$

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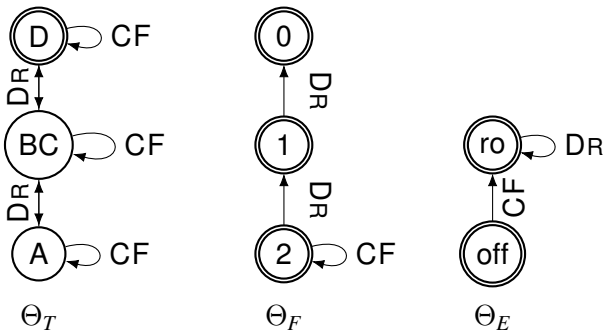
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Plan = $\langle \text{CF}, \text{DR}(BC), \text{DR}(D) \rangle \rightarrow \langle \text{CF}, \text{ON}, \text{DR}(BC), \text{DR}(D) \rangle$

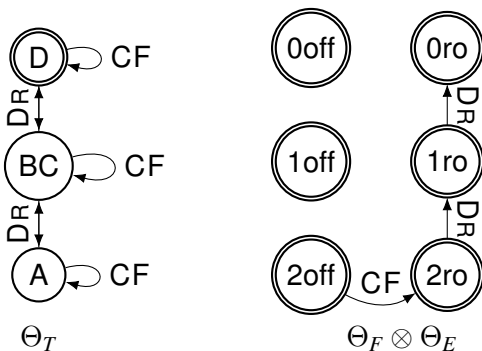
Merge

Replace Θ_i and Θ_j by their product: $\Theta_i \otimes \Theta_j$



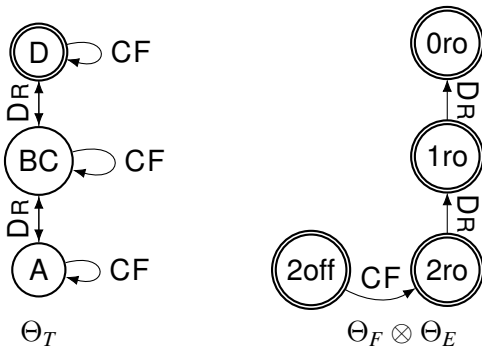
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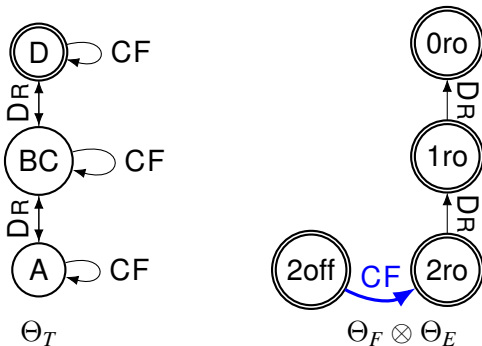
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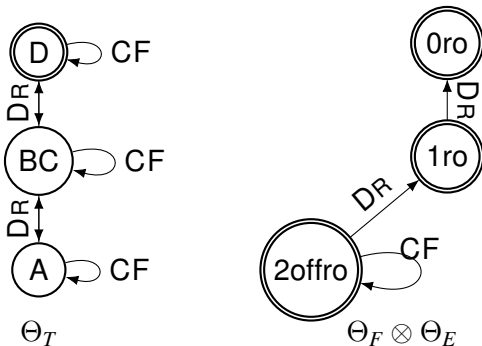
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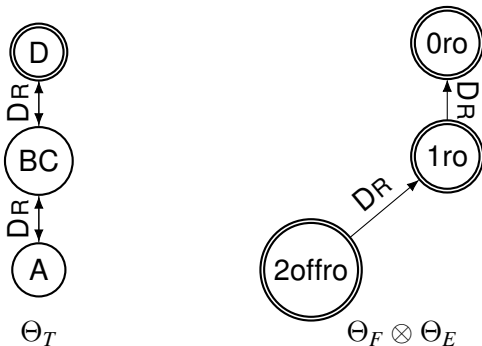
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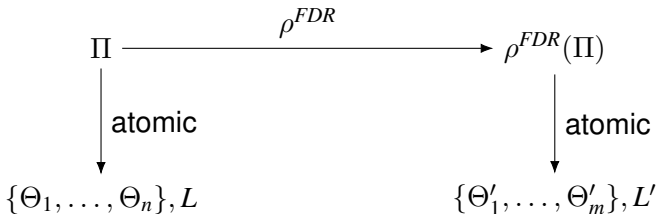
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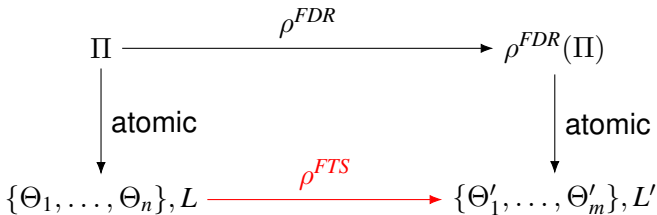
Relation to FDR Reformulation Methods

An FTS reformulation method **dominates** an FDR reformulation method if it **can do the same reformulations**:



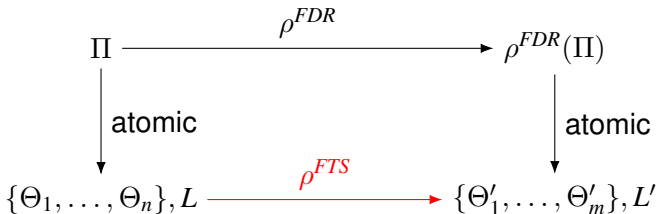
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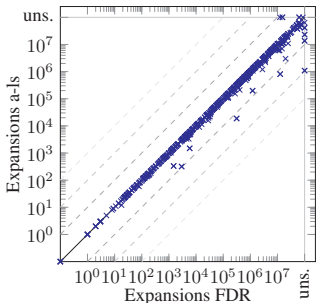
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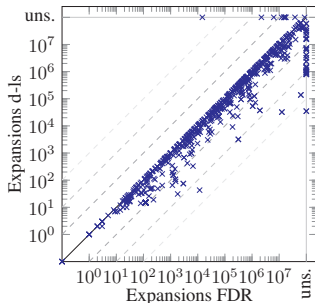


- Variable abstraction and merge values are dominated by weak bisimulation shrinking (plus removing TSs with a core state)
- Generalize actions is dominated by label reduction

Search Space Reduction: Optimal

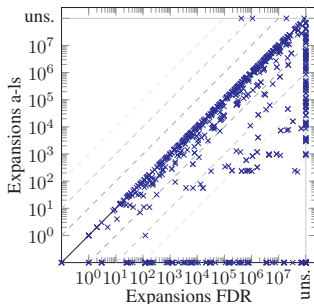


Bisimulation + LR

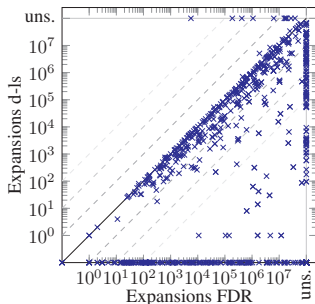


Merge (DFP) + LR + Bisimulation

Search Space Reduction: Satisficing



Weak Bisimulation + LR



Merge (DFP) + LR + Weak Bisimulation

Optimal Planning

	FDR	a	a-ls	d-ls	m-ls	tot	orcl
FDR						797	h_{\max} : 801
a						770	
a-ls						780	
d-ls					600		
m-ls					632		
FDR						822	$h_{M\&S\ d}$: 910
a						826	
a-ls						831	
d-ls					815		
m-ls					849		

Optimal Planning

	FDR	a	a-ls	d-ls	m-ls	tot	orcl
FDR						797	
a						770	$h_{\max}: 801$
a-ls		4				780	
d-ls		2	1			600	
m-ls		4	4			632	
FDR						822	
a						826	$h_{M\&Sd}: 910$
a-ls		4				831	
d-ls		11	10			815	
m-ls		15	15			849	

Optimal Planning

	FDR	a	a-ls	d-ls	m-ls	tot	orcl
FDR	–	12	13	37	36	797	$h^{\max}: 801$
a	1	–	1	36	36	770	
a-ls	3	4	–	36	35	780	
d-ls	2	2	1	–	7	600	
m-ls	4	4	4	19	–	632	
FDR	–	2	3	12	14	822	$h^{\text{M\&S}d}: 910$
a	4	–	1	13	16	826	
a-ls	7	4	–	13	16	831	
d-ls	13	11	10	–	11	815	
m-ls	16	15	15	16	–	849	

Satisficing Planning

	FDR	a	a-ls	d-ls	m-ls	tot	orcl
FDR						1326	$h^{FF}: 1413$
a						1272	
a-ls						1368	
d-ls					1208		
m-ls					1224		
FDR						1502	$h^{FF} p.: 1589$
a						1461	
a-ls						1471	
d-ls					1357		
m-ls					1322		

Satisficing Planning

	FDR	a	a-ls	d-ls	m-ls	tot	orcl
FDR						1326	
a						1272	
a-ls		15				1368	
d-ls		10	4			1208	
m-ls		15	7			1224	
FDR						1502	
a						1461	
a-ls		8				1471	
d-ls		6	2			1357	
m-ls		7	3			1322	

 $h^{FF}: 1413$ $h^{FF} p: 1589$

Satisficing Planning

	FDR	a	a-ls	d-ls	m-ls	tot	orcl
FDR	–	18	15	27	22	1326	$h_{FF}^p: 1413$
a	6	–	13	28	22	1272	
a-ls	18	15	–	31	24	1368	
d-ls	10	10	4	–	11	1208	
m-ls	13	15	7	21	–	1224	
FDR	–	17	15	24	23	1502	$h_{FF}^p: 1589$
a	8	–	11	25	24	1461	
a-ls	13	8	–	26	26	1471	
d-ls	9	6	2	–	15	1357	
m-ls	9	7	3	16	–	1322	

Conclusion

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- Provide a plan reconstruction for M&S **transformations**
 - Merge, LR, Pruning, Bisimulation → optimal reformulation
 - Weak bisimulation → satisficing reformulation
 - Dominance-based pruning
 - Tunnel macros