Complex networks theory and precursors of financial crashes

Vladimir Soloviev^{1,2[0000-0002-4945-202X]}, Victoria Solovieva^{3[0000-0002-8090-9569]}, Anna Tuliakova⁴, Alexey Hostryk^{5[0000-0001-6143-6797]} and Lukáš Pichl⁶

¹ Kryvyi Rih State Pedagogical University, 54 Gagarin Ave., Kryvyi Rih, 50086, Ukraine

² The Bohdan Khmelnytsky National University of Cherkasy,

81 Shevchenka Blvd., 18031, Cherkasy, Ukraine

³ State University of Economics and Technology,

16 Medychna Str., Kryvyi Rih, 50005, Ukraine

⁴ Odessa I. I. Mechnikov National University, 2 Dvoryanskaya Str., Odessa, 65082, Ukraine ⁵ Odessa National Economic University, 8 Preobrazhenskaya Str., Odessa, 65082, Ultraine

Ukraine

⁶ International Christian University, 3-10-2 Osawa, Mitaka-shi, Tokyo, 181-8585, Japan vnsoloviev2016@gmail.com, vikasolovieva2027@gmail.com, tuliakovaanna@gmail.com, alexeyGostrik@gmail.com, lukas@icu.ac.jp

Abstract. Based on the network paradigm of complexity in the work, a systematic analysis of the dynamics of the largest stock markets in the world and cryptocurrency market has been carried out. According to the algorithms of the visibility graph and recurrence plot, the daily values of stock and crypto indices are converted into a networks and multiplex networks, the spectral and topological properties of which are sensitive to the critical and crisis phenomena of the studied complex systems. This work is the first to investigate the network properties of the crypto index CCI30 and the multiplex network of key cryptocurrencies. It is shown that some of the spectral and topological characteristics can serve as measures of the complexity of the stock and crypto market, and their specific behaviour in the pre-crisis period is used as indicators-precursors of critical phenomena.

Keywords: crypto index, visibility graph, complexity measures of financial crashes.

1 Introduction

The new interdisciplinary study of complex systems, known as the complex networks theory, laid the foundation for a new network paradigm of synergetic [17]. The complex networks theory studies the characteristics of networks, taking into account not only their topology, but also statistical properties, the distribution of weights of individual nodes and edges, the effects of information dissemination, robustness, etc. [1; 6; 10;

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20; 21; 22; 31]. Complex networks include electrical, transport, information, social, economic, biological, neural and other networks [1; 6; 10; 20; 18; 22; 24; 31]. The network paradigm has become dominant in the study of complex systems since it allows you to enter new quantitative measures of complexity not existing for the time series [3].

Previously, we introduced various quantitative measures of complexity for individual time series [25; 26; 27; 28; 29]. Significant advantage of the introduced measures is their dynamism, that is, the ability to monitor the time of change in the chosen measure and compare with the corresponding dynamics of the output time series. This allowed us to compare the critical changes in the dynamics of the system, which is described by the time series, with the characteristic changes of concrete measures of complexity. It turned out that quantitative measures of complexity respond to critical changes in the dynamics of a complex system, which allows them to be used in the diagnostic process and prediction of future changes. In [25], we introduced network complexity measures and adapted them to study system dynamics. But networks are rarely isolated. Therefore, it is necessary to take into account the interconnection interaction, which can be realized within the framework of different models [4]. In this paper we will consider it by simulating so-called multiplex networks, the features of which are reduced to a fixed number of nodes in each layer, but they are linked by different bonds.

2 Review

Most complex systems inform their structural and dynamic nature by generating a sequence of certain characteristics known as time series. In recent years, interesting algorithms for the transformation of time series into a network have been developed, which allows to extend the range of known characteristics of time series even to network ones. Recently, several approaches have been proposed to transform time sequences into complex network-like mappings. Three main classes can be distinguished. The first is based on the study of the convexity of successive values of the time series and is called visibility graph (VG) [12]. The second analyzes the mutual approximation of different segments of the time sequence and uses the technique of recurrent analysis [9]. The recurrent diagram reflects the existing repetition of phase trajectories in the form of a binary matrix whose elements are units or zeros, depending on whether they are close (recurrent) with given accuracy or not, the selected points of the phase space of the dynamic system. The recurrence diagram is easily transformed into adjacency matrix, on which the spectral and topological characteristics of the graph are calculated [9]. Finally, if the basis of forming the links of the elements of the graph is to put correlation relations between them, we obtain a correlation graph [9]. To construct and analyze the properties of a correlation graph, we must form adjacency matrix from the correlation matrix. To do this, you need to enter a value which, for the correlation field, will serve as the distance between the correlated agents. So, if the correlation coefficient between the two assets is significant, the distance between them is small, and, starting from a certain critical value, assets can be considered bound on

the graph. For an adjacency matrix, this means that they are adjacent to the graph. Otherwise, the assets are not contiguous. In this case, the binding condition of the graph is a prerequisite.

The use of the complexity of recurrent and visibility graph networks to prevent critical and crisis phenomena in stock markets has been considered by us in a recent papers [27; 28]. In this paper, we consider multiplex implementations of these techniques.

The recurrence diagrams for the visualization of phase space recurrences is based on Henri Poincare's idea of the phase space recurrence of dynamical systems. According to Takens's theorem [9], an equivalent phase trajectory that preserves the structure of the original phase trajectory can be recovered from a single observation or time series by the time delay method: $\vec{x}(t) = (u_i, u_{i+\tau}, ..., u_{i+(m-1)\tau})$, where m – embedding dimension, τ – time delay (real time delay is defined as $\tau \Delta t$). The recurrence plot shows the existing repetitions in the form of a binary matrix R, where $R_{i,j} = 1$, if \vec{x}_j it is adjacent to the state \vec{x}_i , and $R_{i,j} = 0$ otherwise. Neighboring (or recurrent) are states \vec{x}_j that fall into a *m*-dimensional region with radius ε and center in \vec{x}_i . It is clear that parameters m, τ and ε are key when conducting recurrent analysis. The recurrence plot is easily transformed into an adjacency matrix, by which the spectral and topological characteristics of the graph are calculated [28].

The algorithm of the VG is realized as follows. Take a time series $Y(t) = [y_1, y_2, ..., y_n]$ of length *N*. Each point in the time series data can be considered as a vertex in an associative network, and the edge connects two vertices if two corresponding data points can "see" each other from the corresponding point of the time series (fig. 1). Formally, two values y_a of the series (at the time t_a) and y_b (at the time t_b) are connected, if for any other value (y_c, t_c) , which is placed between them (that is, $t_a < t_c < t_b$), the condition is satisfied $y_c < y_a + (y_b - y_a)((t_c - t_a)/(t_b - t_a))$. Note that the visibility graph is always connected by definition and also is invariant under affine transformations, due to the mapping method.



Fig. 1. Illustration of constructing the visibility graph (red lines) and the horizontal visibility graph (green lines) [16].

An alternative (and much simpler) algorithm is the horizontal visibility graph (HVG) [16], in which a connection can be established between two data points *a* and b, if one can draw a horizontal line in the time series joining them that does not intersect any intermediate data by the following geometrical criterion: y_a , $y_b > y_c$ for all *c* such that $t_a < t_c < t_b$ (fig. 1).

In multiplex networks, there are two tasks [13]: (1) turn separate time series on the network for each layer; (2) connect the intra-loop networks to each other. The first problem is solved within the framework of the standard algorithms described above. For multiplex networks, the algorithm of the MVG for the three layers is presented in fig. 2.



Fig. 2. Scheme for forming bonds between three layers of the multiplex network [13].

The recurrence multiplex network (MCRP) is formed from recurrence plots of individual layers.

2.1 Spectral and topological graph properties

Spectral theory of graphs is based on algebraic invariants of a graph – its spectra. The spectrum of graph G is the set of eigenvalues of a matrix $S_p(G)$ corresponding to a given graph. For an adjacency matrix A of a graph, there exists a characteristic polynomial $|\lambda I - A|$, which is called the characteristic polynomial of a graph $P_G(\lambda)$. The eigenvalues of the matrix A (the zeros of the polynomial $|\lambda I - A|$) and the spectrum of the matrix A (the set of eigenvalues) are called respectively their eigenvalues and the spectrum of graph G. The eigenvalues of the matrix A satisfy the equality $A\bar{x} = \lambda \bar{x} (\bar{x} - \text{non-zero vector})$. Vectors \bar{x} satisfying this equality are called eigenvectors of matrix A (or graph G) corresponding to their eigenvalues.

Another common type of graph spectrum is the spectrum of the Laplace matrix *L*. The Laplace matrix is used to calculate the tree graphs, as well as to obtain some important spectral characteristics of the graph. In particular, the positive eigenvalues λ_2 is called the index of algebraic connectivity of the graph. This value represents the "force" of the connectivity of the graph component and is used in the analysis of reliability and synchronization of the graph.

Important derivative characteristics are spectral gap, graph energy, spectral moments and spectral radius. The spectral gap is the difference between the largest and the next eigenvalues of the adjacency matrix and characterizes the rate of return of the system to the equilibrium state. The graph energy is the sum of the modules of the eigenvalues of the graph adjacency matrix. The spectral radius is the largest modulus of the eigenvalue of the adjacency matrix. Denote by N_c the value which corresponds to an "average eigenvalue" of the graph adjacency matrix $N_c = -ln(N \sum_{i=1}^{N} e^{\lambda_i})$ and is called natural connectivity.

The *k*-th spectral moment of the adjacency matrix is determined by the expression $m_k(A) = 1/n \sum_{i=1}^n \lambda_i^k$, where λ_i is the eigenvalues of the adjacency matrix, *n* is the vertex of *G*.

Among the topological measures one of the most important is the node degree k – the number of links attached to this node. For non-directed networks, the node's degree k_i is determined by the sum $k_i = \sum_{i=1}^{n} a_{ij}$, where a_{ij} – the elements of the adjacency matrix.

To characterize the "linear size" of the network, useful concepts of mean $\langle l \rangle$ and maximum l_{max} shortest paths. For a connected network of N nodes, the average path length (ApLen) is equal to $\langle l \rangle = 2/((n(N-1))\sum_{i>j} l_{ij})$, where l_{ij} – the length of the

shortest path between the nodes. The diameter of the connected graph is the maximum possible distance between its two vertices, while the minimum possible is the radius of the graph.

If the average length of the shortest path gives an idea of the whole network and is a global characteristic, the next parameter – the clustering coefficient – is a local value and characterizes a separate node. For a given node m, the clustering coefficient C_m is defined as the ratio of the existing number of links between its closest neighbors to the maximum possible number of such relationships $C_m=2E_m/(k_m(k_m-1))$. Here $k_m(k_m-1)/2$ is the maximum number of links between the closest neighbors. The clustering coefficient shows how many of the nearest neighbors of the given node are also the closest neighbors to each other. He characterizes the tendency to form groups of interconnected nodes – clusters. For real-life networks, the high values of the clustering coefficient are high.

Another feature of the node is the between's. It reflects the role of the node in establishing network connections and shows how many shortest paths pass through this node. Node betweenness σ_m is defined as $\sigma_m = \sum_{i \neq j} B(i, m, j)/B(i, j)$, where B(i, j) – the total number of shortest paths between nodes *i* and *j*, B(i, m, j) – the number of shortest paths between *i*, *j* those passing through the node *m*.

One of the main characteristics of the network is the distribution of nodes P(k), which is defined as the probability that the node *i* has a degree $k_i = k$. For most natural and actual artificial networks there is a power distribution $P(k) \sim 1/k^{\gamma}$, $k \neq 0$, $\gamma > 0$.

Also, important topological characteristics are the vertex eccentricity – the largest distance between m and any other vertex, that is, how far the vertex is far from the other

vertices of the graph. The centrality of the vertex measures its relative importance in the graph. At the same time, the farness of a node is defined as the sum of its distances to all other nodes, and its closeness is defined as the backward distance. Thus, the centrality of the node is lower than its total distance to all other nodes.

Another important measure is the link density in the graph, which is defined as the number of links n_e , divided by the expression $n_n(n_n-1)/2$, where n_n is the number of nodes of the graph.

2.2 Multiplex complexity measures

A multilayer/multiplex network is a pair M=(G, C) where $G = \{G_{\alpha}; \alpha \in \{1, ..., M\}\}$ there is a family of graphs (whether directed or not, weighed or not) $G_{\alpha} = (X_{\alpha}, E_{\alpha})$, called layers $C = \{E_{\alpha\beta} \subseteq X_{\alpha} \times X_{\beta}; \alpha, \beta \in \{1, ..., M\}, \alpha \neq \beta\}$. The latter is a set of links between nodes of different layers G_{α} and G_{β} at $\alpha \neq \beta$. Each element E_{α} is intralayer bonds *M* in contrast to the elements of each $E_{\alpha\beta}$ ($\alpha \neq \beta$), called interlayer bonds.

A set of nodes of a layer G_{α} is denoted $X_{\alpha} = \{x_{1}^{\alpha}, \dots, x_{N_{\alpha}}^{\alpha}\}$, and a adjacency matrix as $A^{[\alpha]} = (a_{ij}^{\alpha}) \in \mathbb{R}^{N_{\alpha} \times N_{\alpha}}, a_{ij}^{\alpha} = \begin{cases} 1, (x_{i}^{\alpha}, x_{j}^{\alpha}) \in E_{\alpha}, \text{ for } 1 \leq i, j \leq N_{\alpha} \text{ and } 1 \leq \alpha \leq M. \end{cases}$ For an interlayer adjacency matrix we have $A^{[\alpha,\beta]} = (a_{ij}^{\alpha\beta}) \in \mathbb{R}^{N_{\alpha} \times N_{\alpha}}$, where $a_{ij}^{\alpha\beta} = \begin{cases} 1, (x_{i}^{\alpha}, x_{j}^{\beta}) \in E_{\alpha\beta}, \\ 0 \end{cases}$.

A multiplex network is a partial interlayer case and contains a fixed number of nodes connected by different types of links. Multiplex networks are characterized by correlations of different nature [27], which enable the introduction of additional multiplexes.

Let's evaluate the quantitative overlap between the various layers. The average edge overlap obviously equal $\omega = \sum_i \sum_{j>i} \sum_{\alpha} a_{ij}^{[\alpha]} / M \sum_i \sum_{j>i} (1 - \delta_{0,\sum_i a_{ij}^{[\alpha]}})$ and determines the number of layers in which this bond is present. Its value lies on the interval [1/M, 1] and equals 1/M if the connection (i, j) exists only in one layer, that is, if there is a layer α such that $a_{ij}^{[\alpha]} = 1, a_{ij}^{[\beta]} = 0 \forall \beta \neq \alpha$. If all layers are identical, then $\omega = 1$. Consequently, this measure can serve as a measure of the coherence of the output time series: high values ω indicate a noticeable correlation in the structure of time series.

The total overlap $O^{\alpha\beta}$ between the two layers α and β is defined as the total number of bonds that are shared between the layers α and $\beta : O^{\alpha\beta} = \sum a_{ij}^{\alpha} a_{ij}^{\beta}$, where $\alpha \neq \beta$.

For a multiplex network, the vertex degree k is already a vector $k_i = (k_i^{[1]}, \dots, k_i^{[M]})$, where $k_i^{[\alpha]}$ is the degree of the node in the layer, that is, while the elements of the matrix of adjacency for the layer. Specificity of the vector character of the degree of the peak in multiplex networks allows for the introduction of additional interlayer characteristics. One of these is the overlap of the node's degree $o_i = \sum_{\alpha=1}^{M} k_i^{[\alpha]}$.

The next measure quantitatively describes the interlayer correlations between the degrees of the selected node in two different layers. If, chosen from M the layers of the

pair (α, β) characterized by the distribution of degrees $P(k^{[\alpha]}), P(k^{[\beta]})$, the so-called interlayer mutual information is determined by the formula $I_{\alpha,\beta} = \sum P(k^{[\alpha]}, k^{[\beta]}) \log((P(k^{[\alpha]}, k^{[\beta]}))/(P(k^{[\alpha]})P(k^{[\beta]})))$, where $P(k^{[\alpha]}, k^{[\beta]})$ is the probability of finding a node degree $k^{[\alpha]}$ in a layer α and degree $k^{[\beta]}$ in a layer β . The higher the $I_{\alpha,\beta}$ value, the more correlated are the distributions of the levels of the two layers, and, consequently, the structure of the time series associated with them. We also find the mean value $I_{\alpha,\beta}$ for all possible pairs of layers – the scalar value $< I_{\alpha,\beta} >$ that quantifies the information flow in the system.

The quantity that quantitatively describes the distribution of the node degree *i* between different layers is the entropy of the multiplexed degree $S_i = -\sum_{\alpha=1}^{M} k_i^{[\alpha]} / o_i \ln(k_i^{[\alpha]} / o_i)$. Entropy is zero if all nodes are in the same layer and vice versa, has the maximum value when they are evenly distributed between different layers. That is, the higher the value S_i , the even more links evenly the nodes' connections are distributed between the layers.

A similar magnitude is the multiplex participation coefficient $P_i = M/(M-1) \left[1 - \sum_{\alpha=1}^{M} \left(k_i^{[\alpha]}/o_i\right)^2\right]$. P_i takes values on the interval [0, 1] and determines that homogeneous links of node *i* are distributed among *M* the layers. If all links of the node *i* lie in one layer, $P_i = 0$ and $P_i = 1$ if the node has a precisely defined number of links in each of the *M* layers. Consequently, the larger the coefficient P_i is, the more evenly distributed the participation of the node in the multiplex.

Obviously, the magnitudes S_i and P_i are very similar. We will show that some of these spectral and topological measures serve as measures of complexity of the system, and the dynamics of their changes allows us to build predictors of crisis situations on financial markets.

2.3 Experimental results and their discussion

In our recent work [26] we investigated the multiplex properties of the most capitalized stock indices for the period from 01/01/1983 to 10/01/2019. Here we will add an analysis of their complex network properties, while also preserving the analysis of multiplex properties for a whiter period of time, but including the COVID-19 crisis [23]: 02/01/2004 – 17/08/2020 [34]. In addition, for the first time, we are examining the network complex properties of the CCI30 crypto index and comparing them with the properties of the multiplex network of the 3 most capitalized cryptocurrencies included in the CCI30 index basket. For the crypto market, the period under consideration corresponds to the time the index was observed: from 07/08/2015 to 17/08/2020 [7]. The time series of daily values of stock market indices were selected as databases, which contained significant changes in the indices, and were identified as crisis phenomena [15]. Daily values of cryptocurrency prices for a period comparable to the CCI30 index were borrowed from [33]. Among the set of stock indexes are the following: SP (S&P500) – USA; DAX (DAX PERFORMANCE-INDEX) – Germany; N225 (Nikkei 225) - Japan; HSI (HANG SENG INDEX) - China; GSPTSE (S&P/TSX Composite index) - Canada.

Up to three selected cryptocurrencies include the following: Bitcoin – BTC; Ethereum – ETH; Litecoin – LTC.

Their comparative dynamics on a relative scale is shown in fig. 3.



Fig. 3. The dynamics of the daily values of the selected stock market indices (a) and cryptocurrencies and CCI30 (b).

Despite a slight difference in the time series dynamics, the main trends (both rising and falling – actually crises) are observed for all time series.

Crypto index CCI30 refers to a number of emerging crypto indices [32] similar to many stock market indices. CCI30 is an index that is designed to objectively measure the overall growth, daily and long-term movement of the blockchain sector. This allows you to track 30 cryptocurrencies by market cap. This index serves as a tool for passive investors to participate in this asset class and an industry benchmark for investment managers. The main characteristics of the CCI30 index are: 1) versatility; 2) reproducibility; 3) transparent; 4) provides comprehensive coverage of the entire sector; 5) represents the best possible risk-adjusted performance profile. The CCI30 was launched on Jan 1st, 2017. Its starting value is arbitrarily set at 100 on Jan 1st, 2015. Members are automatically selected from the top 30 cryptocurrencies by adjusted market cap and included in the index. The minimum number of constituents required to obtain statistical significance was set at 30. Because using more components will lead to higher fees without significantly improving performance, and using fewer than thirty components will run the risk of reduced performance, lack of diversification, decreased statistical significance, and wasted opportunities to pick the next leader. To date, having hit the top 30 cryptocurrencies, CCi30 captures approximately 90% of the cryptocurrency market capitalization. With this scope, the index statistically represents the entire cryptocurrency market with a confidence level of 99% and a confidence interval of 1.11. The margin of error of the index value as an indicator of the market is just 1.11%. To calculate the weights for each cryptocurrency, you first need to calculate the adjusted market cap. Market capitalization is not calculated as some instantaneous number – the volatility in the cryptocurrency market is such that it too destabilizes the composition of the index. Instead, the CCI30 uses an exponentially weighted moving average of the market cap. Weighted average market cap helps smooth out volatility to give the most accurate portrait of market cap at any given moment.

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The weight of each constituent cryptocurrency is measured by the square root of its adjusted market capitalization. The square root function was chosen as a hybrid that most accurately weighs the constituents based on the current cryptocurrency market conditions. A simple weighted market cap index would be dominated by the two leading cryptocurrencies, while a slower declining weight, or in a pinch, equal weighting, would give too much weight to the tiny illiquid cryptocurrencies at the bottom of the range. In order to accurately capture market movements, restrictions or minimum values for the weight of cryptocurrencies are not applied. The index is a better investment vehicle than Bitcoin itself, and a much safer approach than trying to pick individual coins. Investing in an index allows you to profit from the unpredictable growth of some cryptocurrencies, while limiting losses associated with the fall of others.

The spectral and topological properties of both stock market indices and the CCI30 index were calculated. The calculations were carried out using the moving window algorithm. In the case of stock indices, the window size was chosen equal to 250 days, and the window offset was equal to 5 days. In the case of a more volatile crypto market, the window size was chosen equal to 100 days.

Figure 4, using only two measures as an example, shows their typical dynamics. It follows from the figure 4 that in the pre-crisis period the system has a higher complexity. In this case, node degree takes maximum values, while the average path length, on the contrary, is minimized. After the crisis, the opposite picture is observed.

Calculations of spectral and topological measures by methods of MVG, MCRP were carried out in the following way. For the selected window, the corresponding graphs were constructed and the spectral, topological and multiplex properties were calculated. Next, the window was shifted step by step, for example, one week (5 trading days) and the procedure repeated until the time series were exhausted. Knowing the time of the onset of the crisis and comparing the time series with the dynamics of a certain indicator, it is possible to investigate its dependence on certain the characteristic changes in the stock market: pre-crisis, crisis and post-crisis periods.

The results of calculations for revived time series of graphs are shown in figures 5-8.





Fig. 4. Window dynamics of spectral k_{max} and topological ApLen complexity measures for the S&P500 and CCI30 indices.



Fig. 5. The entropy of the multiplexed degree and the multiplex participation coefficient calculated for a sliding window (w) of 250 days in increments (Δt) of 5 days. Moments of major stock crises are indicated.



Fig. 6. Nodes degree overlap and the total overlap calculated for a sliding window (w) of 250 days in increments (Δt) of 5 days.

Figures 5-6 show that the pair of parameters S, P in figure 5 is antisymmetric to the pair parameters o, O of figure 6. However, all of them in a characteristic way (decreasing or increasing before the crisis) signal about its possible onset.

Similar calculations were carried out for the CCI30 index (figures 7-8). As in the case of a multiplex visibility graph, multiplex recurrence measures are also informative indicators-predictors of crisis phenomena.

Parameters such as the width of the window w and the step Δt of its displacement along the time series are important. When w is small, the degree of complexity fluctuates noticeably, reacting not only to crises, but also to more or less noticeable fluctuations of the index. On the contrary, with too much window width there is a noticeable smoothing of the appropriate measure and if two crises are at a distance that is smaller w, the indicators of both crises are averaged and less informative. If you choose an oversized parameter Δt , you might miss the actual crisis that distorts the indicator.



Fig. 7. MVG complexity measures: the entropy of the multiplexed degree and the multiplex participation coefficient.



Fig. 8. MVG complexity measures: nodes degree overlaps and the total overlap.

Multiplex networks are actively used to simulate complex networks of different nature: from financial (banks [2], stock market [19], guarantee market [14]) to social [30]. Particular attention should be paid to the work [19], in which the above multiplex measures are analyzed for the subject of correlations with known stock markets crises. Yet there is no systematic analysis of network and multiplex measures and the construction of indicators-predictors of the crisis phenomena in the stock market. Therefore, our studies to some extent fill this gap.

3 Conclusions

We have demonstrated the possibility of studying complex socio-economic systems as part of a network paradigm of complexity. A time series can be represented in an equivalent way - a complex/multiplex network, which has a wide range of characteristics; both spectral and topological, and multiplexed. Examples of known financial crises have shown that most of the network measures can serve as indicators-precursors of crisis phenomena and can be used for possible early prevention of unwanted crises in the financial markets. They are an extension of the already proposed by us and "working" indicators, which use other measures of complexity.

It should be noted that the proposed indicators-precursors do not solve the more general problem of forecasting future values or trends of the stock market. In this way, it is possible to use new approaches or alternative methods based on algorithms of (deep) machine learning [5; 8; 11].

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