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A simple scheme to amplify inter-class discrepancy for improving few-shot fine-grained image classification

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Abstract

Few-shot image classification is a challenging topic in pattern recognition and computer vision. Few-shot fine-grained image classification is even more challenging, due to not only the few shots of labelled samples but also the subtle differences to distinguish subcategories in fine-grained images. A recent method called task discrepancy maximisation (TDM) can be embedded into the feature map reconstruction network (FRN) to generate discriminative features, by preserving the appearance details through reconstructing the query image and then assigning higher weights to more discriminative channels, producing the state-of-the-art performance for few-shot fine-grained image classification. However, due to the small inter-class discrepancy in fine-grained images and the small training set in few-shot learn-

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ing, the training of FRN+TDM can result in excessively flexible boundaries between subcategories and hence overfitting. To resolve this problem, we propose a simple scheme to amplify inter-class discrepancy and thus improve FRN+TDM. To achieve this aim, instead of developing new modules, our scheme only involves two simple amendments to FRN+TDM: relaxing the inter-class score in TDM, and adding a centre loss to FRN. Extensive experiments on five benchmark datasets showcase that, although embarrassingly simple, our scheme is quite effective to improve the performance of few-shot fine-grained image classification. The code is available at <https://github.com/Airgods/AFRN.git>.

Keywords: Few-shot learning, fine-grained image classification, metric-based methods.

1. Introduction

Few-shot fine-grained image classification is a challenging task that draws wide attention in the pattern recognition and computer vision communities. Although deep neural networks learnt from a large amount of labelled training data can provide impressive image classification performances, few-shot learning that trains a model with little labelled data for each class remains difficult. Moreover, the fine-grained setting brings further challenges, as each class is divided to a large number of subcategories, which makes the inter-class discrepancy even smaller and the classification task much harder.

Metric-based methods are effective for few-shot learning [1]. They aim to learn a metric function to measure the similarities/dissimilarities between different classes and assign the test image to the class with the highest similarity

13 or lowest dissimilarity. For example, the prototypical networks (ProtoNet)
14 proposed by Snell et al. [2] adopt the average of features of all images from
15 the same class in the support set as the prototype of that class, and as-
16 sign the query image to the class with the shortest Euclidean distances from
17 the class prototypes. Recent works enhance ProtoNet by generating more
18 representative prototypes [3]. The matching networks (MatchingNet) [4]
19 utilise a bidirectional LSTM network to map the support set and an at-
20 tention mechanism-based LSTM to map the query set, and adopt the cosine
21 similarity as the metric function. In addition to the common metric func-
22 tions, Zhang et al. [5] propose a new metric function EMD, which assigns
23 different weights to different positions of the image and calculates the best
24 matching between the image blocks of the support set and the query set to
25 represent their similarities. To maintain feature discriminability, Nguyen et
26 al. [6] propose the square root of the sum of the Euclidean distance and the
27 norm distance as the metric function. Similarities between images can also
28 be measured via a properly structured neural network [7].

29 However, when the high similarities between subclasses are not carefully
30 considered, metric-based methods can fail to classify fine-grained images.
31 Thus it is crucial to extract features with strong discriminative power to
32 distinguish the ultra-fine differences between subclasses. Li et al. intro-
33 duce the bi-similarity network (BSNet) with two similarity metrics to learn
34 such discriminative features [8]. Huang et al. propose the low-rank pairwise
35 aligned bilinear network (LRPABN), which utilises bilinear pooling opera-
36 tions to distinguish support and query images [9]. Huang et al. also propose
37 the targeted alignment network (TOAN), which can increase the inter-class

38 variation by extracting discriminative fine-grained features while reducing
 39 intra-class variation by matching support and query features [10].

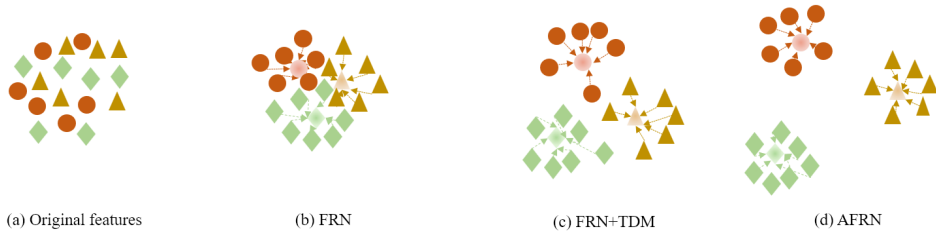


Figure 1: An illustration of the motivation of the adaptive feature map reconstruction network (AFRN). The solid circles, triangles and diamonds represent the instances from three classes, respectively, and the transparent circle, triangle and diamond represent the corresponding prototypes of the three classes, respectively. In (a), we depict a challenging classification task, with severe overlapping between the three classes in the original features space. This challenge is partially resolved by FRN in (b), because the appearance details of images are well preserved by reconstruction, which potentially makes the embedded features more discriminative. In (c), TDM is incorporated to FRN to assign high weights to channels with strong discriminative abilities, and thus the classes become more separable. Finally, in (d), AFRN further improves FRN+TDM by amplifying the inter-class discrepancy, and thus the three classes can be more easily distinguished.

40 There is a problem in many previous metric-based learning algorithms
 41 that the input to the metric function has to be reshaped to vectors, resulting
 42 in deficient spatial information. To resolve this problem, Wertheimer et
 43 al. [11] propose a novel metric-based classification mechanism, feature map
 44 reconstruction networks (FRN), for few-shot learning. FRN predicts the
 45 membership of the query image by reconstructing the query feature map
 46 via the pooled support features of each class. The idea behind FRN is that
 47 the query feature map is expected to be well reconstructed by the support

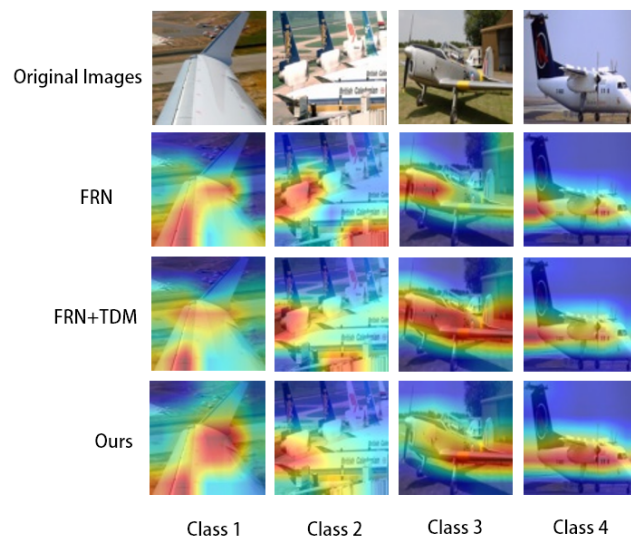


Figure 2: Examples of the features captured by FRN, FRN+TDM and AFRN on four subclasses of airplanes. Apparently, FRN focuses on the objects as well as the nuisance background. Involving TDM in FRN makes the features more discriminative and the focus on background is reduced slightly. In comparison, our AFRN can identify the most discriminative features to distinguish the subclasses with the least focus on the background.

48 features from the correct class with the smallest reconstruction error. Hence,
49 through the reconstruction process, FRN can well preserve the appearance
50 details of the images.

51 However, in FRN, all channels are treated equally with the same weights,
52 without stressing the different importance of different channels. Hence, Lee
53 et al. [12] propose the task discrepancy maximisation (TDM) module to
54 identify channels with high discriminative power and assign higher weights
55 to these channels to improve the classification results of few-shot methods,
56 such as FRN, for fine-grained images. TDM produces channel weights for
57 both support and query sets via the support attention module (SAM) and
58 the query attention module (QAM), respectively. SAM provides class-wise
59 channel weights to highlight the discriminative channels to distinguish be-
60 tween classes, while QAM provides object-wise channel weights to focus more
61 on the object-relevant channels. Lee et al. [12] demonstrate that by incorpo-
62 rating TDM to FRN, namely FRN+TDM, a state-of-the-art performance of
63 few-shot fine-grained image classification can be achieved.

64 However, due to the small inter-class discrepancy omnipresent in fine-
65 grained images and the small training set in the setting of few-shot learning,
66 FRN+TDM can produce excessively flexible boundaries between subcate-
67 gories and hence overfitting. To resolve this problem, we propose a simple
68 scheme to amplify inter-class discrepancy and thus improve FRN+TDM. To
69 this end, instead of developing new modules to further enhance the extraction
70 of discriminative features, our scheme only involves two simple amendments
71 to FRN+TDM: relaxing the inter-class score in TDM, and adding a centre
72 loss to FRN. We name the network incorporating our scheme to FRN+TDM

73 the adaptive feature map reconstruction network (AFRN).

74 The centre loss [13] aims to achieve intra-class compactness by penalising
 75 the distance between the learnt features and their corresponding class
 76 centres, which is vital to distinguish subclasses with high similarity normally
 77 occurring in fine-grained image classification. In Figure 1, we illustrate
 78 the motivation of AFRN by a challenging classification of three overlapping
 79 classes, which is typical in fine-grained image classification with small inter-
 80 class discrepancy. By involving the centre loss in AFRN, we expect that
 81 the three classes can be intra-class more compact and thus inter-class more
 82 separated to make the classification easier. Moreover, in Figure 2, we demon-
 83 strate one real-data example of the discriminative features extracted by FRN,
 84 FRN+TDM and AFRN on four subclasses of airplanes. The original FRN
 85 focuses on the airplanes as well as the nuisance backgrounds; incorporating
 86 TDM can improve this situation with less focus on the backgrounds; while,
 87 in comparison, AFRN can identify the most discriminative features with the
 88 least focus on the backgrounds. For instance, in class 2, the background in
 89 the lower right corner is least highlighted in our method.

90 More importantly, we observe that FRN+TDM can produce excessively
 91 flexible boundaries between subcategories and thus overfitting, as the inter-
 92 class score in TDM to measure the discrepancy between classes is the Eu-
 93 clidean distance between one class and its *nearest* class. Such an inter-class
 94 score can result in extremely flexible classification boundaries for fine-grained
 95 images and thus overfitting to the seen classes in the training set. In few-shot
 96 fine-grained learning, this problem is severer, because in the test phase, few-
 97 shot learning aims to classify the novel set with completely different classes

98 from those in the training set. Thus we propose to relax the inter-class score
99 in TDM simply to the Euclidean distance between one class and its *furthest*
100 class, to mitigate the potential overfitting to a large extent. This amendment
101 makes the original TDM module a relaxed TDM module.

102 In summary, the main contributions of our work are as follows.

- 103 • We propose AFRN, a simple scheme to amplify inter-class discrepancy
104 and thus improve the few-shot fine-grained image classification. Our
105 scheme only involves two simple amendments to FRN+TDM: relaxing
106 the inter-class score in TDM, and adding a centre loss to FRN.
- 107 • By relaxing the inter-class score in TDM, we are able to remarkably
108 mitigate the negative impact, from the overfitting to the seen training
109 set of fine-grained subclasses, on the inference of unseen novel classes
110 in the few-shot learning setting.
- 111 • By incorporating the guidance of the centre loss to FRN, we are able to
112 enhance the discriminative power of the learnt features for fine-grained
113 image classification, through enlarging the omnipresent subtle distances
114 between fine-grained subclasses.
- 115 • The experiments on five benchmark fine-grained datasets demonstrate
116 that our scheme, although very simple, is quite effective to improve the
117 performance of few-shot fine-grained image classification.

118 The rest of the paper is organised as follows. In section 2, we discuss
119 the literature that is closely related to our work. The technical details of
120 FRN+TDM and AFRN are presented in section 3. In section 4, we demon-
121 strate the superior classification performances of AFRN through extensive

122 experimental results and ablation studies. Lastly, we draw conclusions in
123 section 5.

124 2. Related Work

125 2.1. Metric-based few-shot methods for image classification

126 Metric-based few-shot methods aim to learn discriminative feature em-
127 beddings that can be well generalized to new classes based on a predefined or
128 a learnt distance metric, such as Euclidean distance [2], cosine distance [14],
129 hyperbolic distance [15], or distance parameterized by neural networks [16].
130 MatchingNet [4] adopts the cosine similarity to assign the label of the query
131 image. ProtoNet [2] calculates prototypes as the average features of each
132 class in the support set and assign the query image to the nearest class
133 prototype by Euclidean distance. Instead of using a predefined metric, Rela-
134 tionNet [16, 17] utilises a neural network to compute the nonlinear similar-
135 ities between different samples. Moreover, Satorras and Estrach propose to
136 utilise graph neural networks to measure the similarities between images [18].
137 A large amount of work has also been done to extend the metric-based meth-
138 ods for fine-grained images. For example, BSNet involves two similarity met-
139 rics to learn discriminative features [8] and LRPABN adopts bilinear pooling
140 operations [9].

141 2.2. Feature alignment-based few-shot methods for image classification

142 Feature alignment methods usually aim to align the object positions
143 between the support and query sets to improve the classification perfor-
144 mance [19]. CrossTransformers (CTX) [20] utilises the transformer-based

145 network to explore the spatially-correlated features and calculate the sim-
 146 ilarity between two images. A more recent transformer-based method is
 147 QSFormer [21], which effectively learns consistent representations of the sup-
 148 port and query sets via the global sample transformer and the local patch
 149 transformer. Dynamic meta-filer (DMF) [22] considers both channel-wise
 150 and spatial-wise alignments by neural ordinary differential equation. Re-
 151 lational embedding network (RENet) utilises the self-correlational repre-
 152 sentation (SCR) module and the cross-correlational attention (CCA) mod-
 153 ule, where the SCR module transforms the basic feature maps into self-
 154 correlational tensors and extracts structural patterns, while the CCA module
 155 calculates the cross-correlations between images and generates common at-
 156 tention between them. FRN [11] aligns the features maps of the query image
 157 and the support set via reconstructing the query image based on the pooled
 158 support features, where the ridge regression-based reconstruction with close-
 159 form solutions makes the process efficient. Besides the L_2 norm adopted
 160 in FRN, Sun et al. [23] propose to utilise the $L_{2,1}$ norm for feature recon-
 161 struction. To alleviate overfitting of the reconstruction-based methods, Li et
 162 al. [24] propose the self-reconstruction network that can diversify the query
 163 features by reconstructing the query features by themselves.

164 3. Methodology

165 3.1. Problem definition

166 Few-shot learning aims to learn discriminative knowledge from a small
 167 amount of labelled data to classify test instances from new tasks. In few-
 168 shot learning, the dataset is usually divided into a base set \mathcal{D}_B , a validation

169 set \mathcal{D}_V and a novel set \mathcal{D}_N , where the classes of the three subsets do not
 170 intersect. Few-shot learning learns from the tasks on \mathcal{D}_B to classify instances
 171 of new tasks on \mathcal{D}_N . The instances in \mathcal{D}_V assist to find the best model during
 172 the training process. In this paper, we follow the classic setting of N -way
 173 K -shot, i.e. the model is trained by the support set, $\mathcal{S} = \{\mathbf{x}_i, y_i\}_{i=1}^{N \times K}$, of N
 174 classes with K instances each class, and evaluated on the query set of the
 175 same classes in \mathcal{S} , $\mathcal{Q} = \{\mathbf{x}_j, y_j\}_j^{N \times q}$, of N classes with q instances each class.
 176 The classification performance of the trained model is finally tested on \mathcal{D}_N
 177 with its average classification accuracy as the performance measure.

178 3.2. FRN+TDM

179 In metric-based few-shot learning methods, reshaping feature maps to
 180 feature vectors as input to metric function can lead to loss of spatial details.
 181 FRN [11] aims to resolve this problem by reconstructing every location of the
 182 query feature map by the pooled support features from each class through
 183 ridge regression. The class membership of the query instance is then assigned
 184 based on the reconstruction error. However, in FRN, all channels are treated
 185 equally with the same weights, which cannot stress the regions with high
 186 discriminative abilities. To identify the discriminative regions, the TDM
 187 module can be embedded in the FRN framework.

188 Specifically, TDM [12] takes the features extracted from the embedding
 189 module to calculate the task-wise channel weight vector β_n of the n th class
 190 as a linear combination of the support weight vector β_n^S and the query weight
 191 vector β^Q :

$$\beta_n = \alpha \beta_n^S + (1 - \alpha) \beta^Q \in \mathbb{R}^C, \quad (1)$$

192 where $\alpha \in [0, 1]$ is a hyper-parameter. β_n^S and β^Q are obtained from the
 193 support attention module (SAM) and the query attention module (QAM),
 194 respectively, based on the task-wise intra-class scores $\mathbf{r}_n^{\text{intra}}$ and inter-class
 195 scores $\mathbf{r}_n^{\text{inter}}$.

196 The input to SAM is the prototype of each class $\mathcal{P}_n \in \mathbb{R}^{H \times W \times C}$, i.e. the
 197 average of all support set instances in the n th class. The c th element of $\mathbf{r}_n^{\text{intra}}$
 198 is then calculated as

$$r_{n,c}^{\text{intra}} = \frac{1}{H \times W} \|\mathcal{P}_{n,c} - \mathbf{M}_n\|_2^2, \quad (2)$$

199 where H and W are the height and width of the feature maps, C is the
 200 number of channels, $\mathcal{P}_{n,c} \in \mathbb{R}^{H \times W}$ is the c th channel of the n th prototype and
 201 $\mathbf{M}_n \in \mathbb{R}^{H \times W}$ is the average of the channels in \mathcal{P}_n , i.e. $\mathbf{M}_n = \frac{1}{C} \sum_{c=1}^C \mathcal{P}_{n,c}$.
 202 Thus $\mathbf{r}_n^{\text{intra}}$ measures the dispersion of the channels in the prototype of each
 203 class. On the contrary, the c th element of $\mathbf{r}_n^{\text{inter}}$ involves information from
 204 different classes:

$$r_{n,c}^{\text{inter}} = \frac{1}{H \times W} \min_{1 \leq l \leq N, n \neq l} \|\mathcal{P}_{n,c} - \mathbf{M}_l\|_2^2, \quad (3)$$

205 where \mathbf{M}_l denotes the mean spatial features of the l th class. It is clear
 206 that $r_{n,c}^{\text{inter}}$ measures the difference between each channel and its closest mean
 207 spatial features of a different class. Finally, we obtain β_n^S as

$$\beta_n^S = \eta(g^{\text{inter}}(\mathbf{r}_n^{\text{inter}})) + (1 - \eta)(g^{\text{intra}}(\mathbf{r}_n^{\text{intra}})), \quad (4)$$

208 where g^{inter} and g^{intra} are fully-connected blocks and $\eta \in [0, 1]$. We adopt the
 209 same structure for g as in [12].

210 Since the labels of query images are unknown, only the intra-class score

211 is involved in QAM:

$$r_{Q,c}^{\text{intra}} = \frac{1}{H \times W} \|\mathcal{P}_{Q,c} - \mathbf{M}_Q\|_2^2, \quad (5)$$

212 where $\mathcal{P}_{Q,c}$ is the c th channel of the query feature maps and \mathbf{M}_Q is the mean
213 of all channels of \mathcal{P}_Q . Then, β^Q is calculated as

$$\beta^Q = g^Q(\mathbf{r}_Q^{\text{intra}}), \quad (6)$$

214 where g^Q is a fully-connected block with the same structure as g^{inter} and g^{intra} .
215 By substituting equation(4) and equation(6) to equation(1), we obtain the
216 task-wise weights β_n .

217 In FRN+TDM, suppose the pooled support features of the n th class is
218 $\mathbf{S}_n \in \mathbb{R}^{(K \times H \times W) \times C}$ while the the query features are $\mathbf{Q} \in \mathbb{R}^{(H \times W) \times C}$. \mathbf{Q} is
219 reconstructed by each \mathbf{S}_n via ridge regression:

$$\hat{\mathbf{W}} = \underset{\mathbf{W}}{\operatorname{argmin}} \|\mathbf{Q} - \mathbf{W}\mathbf{S}_n\|_2^2 + \lambda \|\mathbf{W}\|_2^2, \quad (7)$$

220 where $\mathbf{W} \in \mathbb{R}^{(H \times W) \times (K \times H \times W)}$ is the weight matrix and λ is a non-negative
221 value that controls the contribution of the ridge penalty. The reconstructed
222 query image by the n th class is calculated as

$$\hat{\mathbf{Q}}_n = \hat{\mathbf{W}}\mathbf{S}_n. \quad (8)$$

Then, the task-wise weight vector β_n is applied to the original and the
reconstructed query feature maps to re-weight the channels:

$$\begin{aligned} \mathbf{Q}_n^r &= (\mathbf{1}_{H \times W} \beta_n^T) \odot \mathbf{Q}, \\ \hat{\mathbf{Q}}_n^r &= (\mathbf{1}_{H \times W} \beta_n^T) \odot \hat{\mathbf{Q}}_n, \end{aligned} \quad (9)$$

223 where $\mathbf{1}_{H \times W}$ is a vector of $H \times W$ 1s and \odot is the element-wised Hadamard
 224 product.

225 Lastly, to assign the class membership of the j th query image, we calculate
 226 its probability of belonging to the n th class as

$$P(\hat{y}_j = n | \mathbf{x}_j) = \frac{e^{-\gamma d(\mathbf{Q}_{n,j}^r, \hat{\mathbf{Q}}_{n,j}^r)}}{\sum_{n' \in [1, N]} e^{-\gamma d(\mathbf{Q}_{n',j}^r, \hat{\mathbf{Q}}_{n',j}^r)}}, \quad (10)$$

227 where $d(\mathbf{Q}_n^r, \hat{\mathbf{Q}}_n^r) = \frac{1}{H \times W} \|\mathbf{Q}_n^r - \hat{\mathbf{Q}}_n^r\|_2^2$ and γ is a non-negative parameter.

The training process of FRN+TDM is guided by the cross-entropy loss and the auxiliary loss in FRN:

$$\begin{aligned} L_{FRN} &= L_{CE} + L_{AUX} \\ &= - \sum_{j=1}^{N_q} \log(P(\hat{y}_j = y_j | \mathbf{x}_j)) \\ &\quad + \sum_{n \in [1, N]} \sum_{n' \in [1, N], n' \neq n} \|\hat{\mathbf{S}}_n (\hat{\mathbf{S}}_{n'})^T\|^2, \end{aligned} \quad (11)$$

228 where $\hat{\mathbf{S}}_n$ is the row-normalised \mathbf{S}_n .

229 3.3. Adaptive feature map reconstruction network (AFRN)

230 Although FRN+TDM has achieved a state-of-the-art performance in few-
 231 shot fine-grained image classification, due to the small inter-class discrepancy
 232 omnipresent in fine-grained images and the small training set in the setting
 233 of few-shot learning, the training of FRN+TDM can still result in excessively
 234 flexible boundaries between subcategories and hence overfitting to the seen
 235 subclasses in the training set. To mitigate this issue, we propose a simple
 236 scheme to amplify inter-class discrepancy and thus improve FRN+TDM.
 237 Our scheme only involves two simple amendments to FRN+TDM: relaxing

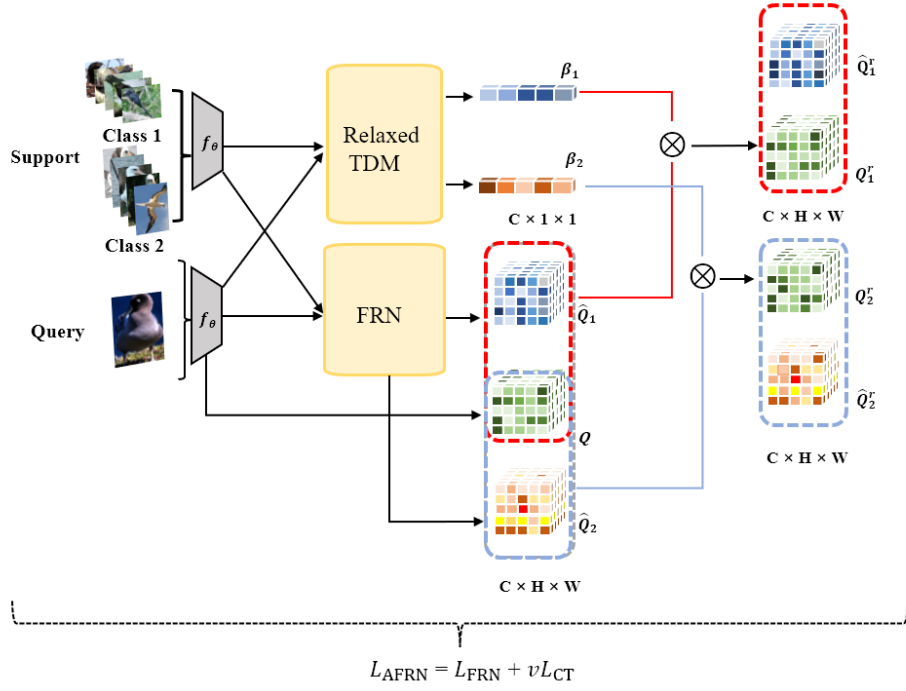


Figure 3: The structure of AFRN with an example of 2-way 5-shot classification. The embedded features of the support set and the query set are input to the FRN and the relaxed TDM modules. The FRN module reconstructs the query feature map by the pooled support features of each class and output the reconstructed query feature maps \hat{Q}_1 and \hat{Q}_2 . The relaxed TDM module produce the task-wise channel weights β_1 and β_2 . Then, the original query feature map Q and the reconstructed \hat{Q}_1 are re-weighted by β_1 to obtain Q_1^r and \hat{Q}_1^r . Similarly, Q and \hat{Q}_2 are re-weighted by β_2 to obtain Q_2^r and \hat{Q}_2^r . Lastly, the two pairs of re-weighted query features are used to obtain probabilities in equation(10) to assign the membership of the query image.

238 the inter-class score in TDM, and adding a centre loss to FRN. We call the
 239 network incorporating our scheme to FRN+TDM the adaptive feature map
 240 reconstruction network (AFRN). The structure of AFRN is illustrated in
 241 Figure 3.

242 3.3.1. Relaxing inter-class score in TDM

243 In equation(3), $r_{n,c}^{\text{inter}}$ measures the minimum distance between each chan-
 244 nel and its closest mean spatial features of a different class. Therefore, the
 245 classes that are mostly difficult to distinguish are specifically considered.
 246 However, this may lead to extremely flexible classification boundaries in the
 247 setting of fine-grained image classification, which is even severer in the few-
 248 shot setting where the classes in the base set and the novel set are not the
 249 same, due to the overfitting to the seen subclasses in the base set. To miti-
 250 gate this problem, we propose the relaxed TDM by revising the calculation
 251 of $r_{n,c}^{\text{inter}}$ in equation (3) as

$$r_{n,c}^{\text{inter}} = \frac{1}{H \times W} \max_{1 \leq l \leq N, n \neq l} \|\mathcal{P}_{n,c} - \mathbf{M}_l\|_2^2. \quad (12)$$

252 In this way, $r_{n,c}^{\text{inter}}$ measures the differences between classes that are less dif-
 253 ficult to distinguish, which makes the classification boundaries less flexible
 254 and thus mitigates the overfitting to a large extent.

255 3.3.2. Adding centre loss to FRN

256 The centre loss L_{CT} measures the intra-class variation of each class, which
 257 is calculated as

$$L_{CT} = \sum_{j=1}^{Nq} \|\mathbf{Q}_j - \mathbf{C}_{y_j}\|_2^2, \quad (13)$$

258 where \mathbf{C}_{y_j} denotes the centre of the y_j th class, and \mathbf{Q}_j represents the feature
 259 of the j th query. To effectively update the centre, we compute the centre as
 260 the average of the query samples in one task.

261 Hence, the total loss function of AFRN is a simple amendment to that of
 262 FRN in equation (11):

$$L_{AFRN} = L_{FRN} + \nu L_{CT}. \quad (14)$$

263 4. Experiments

264 In this section, we empirically demonstrate the superior classification per-
 265 formance of AFRN on five fine-grained image datasets, by comparing it with
 266 eight state-of-the-art methods: MatchingNet [4], ProtoNet [2], CTX [20],
 267 DeepEMD [5], RENet [25], MixFSL [26], FRN [11] and FRN+TDM [12].

268 4.1. Datasets

269 We choose five publicly-available benchmark datasets for few-shot image
 270 classification, namely CUB-200-2011 [27], aircraft [28], Oxford flowers [29],
 271 Stanford cars [30] and Stanford dogs [31]. We name these datasets CUB,
 272 aircraft, flowers, cars and dogs for short hereafter.

273 The CUB dataset contains 200 species of birds, with a total of 11,788
 274 images. We randomly divide the 200 categories into the training, validation
 275 and test sets, each consisting of 100, 50 and 50 categories, respectively.

276 The aircraft dataset has 100 classes of aircrafts, with a total of 10,000
 277 images. We randomly divide the dataset into the training set with 50 classes,
 278 the validation set with 25 classes and the test set with 25 classes.

279 The flowers dataset consists of 102 categories of flowers with 8,189 images.
280 Each type of flower consists of 40 to 258 images, mainly featuring common
281 British flowers. We randomly select 51 classes as the training set, 26 classes
282 as the validation set, and 25 classes as the test set.

283 The cars dataset includes 196 classes of cars, with a total of 16,185 images.
284 We randomly divide the dataset into the training set with 130 classes, the
285 validation set with 17 classes and the test set with 49 classes.

286 The dogs dataset contains 120 breeds of dogs, with a total of 20,580
287 images. We randomly divide the 120 categories into the training set with 60
288 categories, the validation set with 30 categories and the testing set with 30
289 categories.

290 *4.2. Implementation details*

291 We adopt ResNet-12 as the backbone with the same implementation de-
292 tails as in [28, 32, 33]. The ResNet-12 backbone consists of 4 residual blocks,
293 and each residual block has 3 convolutional layers. We adopt the leaky ReLU
294 with $\alpha = 0.1$ and 2×2 max pooling. We also adopt the deep block from the
295 original implementation [32, 28, 33], so the output size of each residual block
296 is 64, 160, 320 and 640. Therefore, the shape of the output feature map of
297 an input image of size 84×84 is $640 \times 5 \times 5$. During the training process, we
298 implement the standard data augmentation step, including random cropping,
299 horizontal flipping and color jittering, as in [28, 5, 34, 35].

300 Following [14, 33], we train ResNet-12 for 1,200 epochs and reduce the
301 learning rate proportionally at the 400th and 800th epochs. We use the
302 validation set to select the best performing model during the training process
303 and validate every 20 epochs. We train the models with the 10-way 5-shot

304 setting and test the models with the 5-way 1-shot and 5-way 5-shot setting.

305 For AFRN, we follow TDM [12] to set $\alpha = \eta = 0.5$, and set $\nu = 0.05$. In
306 section 4.5, we will show the robustness of ν .

307 AFRN and FRN+TDM have the same amount of parameters and they
308 have the same FLOPs. For the 5-way 1-shot task with 16 query images, their
309 FLOPs is 299.6G per task while for the 5-way 5-shot setting with 16 query
310 images, their FLOPs is 370G per task.

Table 1: 5-way few-shot classification accuracies on the CUB, aircraft, flowers, cars and dogs datasets with the ResNet-12 backbone. Methods labeled by † denote our implementations. The best classification accuracies are labelled in bold fonts.

Method	CUB		Aircraft		Flowers		Cars		Dogs	
	1-shot	5-shot	1-shot	5-shot	1-shot	5-shot	1-shot	5-shot	1-shot	5-shot
MatchingNet[4] †	71.87±0.24	85.08±0.24	56.74±0.87	73.75±0.69	71.89±0.90	85.46±0.59	45.29±0.82	64.00±0.74	66.48±0.88	79.57±0.63
ProtoNet[2] †	81.02±0.20	91.93±0.11	46.68±0.81	71.27±0.27	75.41±0.22	89.46±0.14	82.29±0.20	93.11±0.10	73.81±0.21	87.39±0.12
CTX[20] †	80.39±0.20	91.01±0.11	65.60±0.25	80.20±0.25	-	-	85.03±0.19	92.63±0.11	73.22±0.22	85.90±0.13
DeepEMD[5] †	75.59±0.30	88.23±0.18	-	-	70.00±0.35	83.63±0.26	73.30±0.29	88.37±0.17	70.38±0.30	85.24±0.18
RENet[25] †	77.45±0.45	90.50±0.26	59.16±0.47	76.48±0.37	79.91±0.42	92.33±0.22	79.66±0.44	91.95±0.22	71.69±0.47	85.60±0.30
MixFSL[26] †	64.53±0.92	80.67±0.64	60.55±0.86	77.57±0.69	72.60±0.91	86.52±0.65	58.15±0.87	80.54±0.63	67.26±0.90	82.05±0.56
FRN[11] †	82.33±0.19	92.02±0.11	70.26±0.22	83.58±0.14	81.68±0.20	92.61±0.11	86.59±0.18	95.01±0.08	76.49±0.21	88.22±0.12
FRN+TDM[12] †	83.31±0.19	92.70±0.10	70.61±0.21	84.53±0.13	82.95±0.19	93.61±0.10	89.38±0.16	96.98±0.06	76.67±0.21	88.53±0.12
Ours	83.95±0.18	93.17±0.10	72.19±0.21	85.59±0.13	83.59±0.19	94.05±0.09	89.27±0.16	96.89±0.06	77.01±0.21	88.60±0.12

Table 2: The results of the one-sided paired t -test of comparing the classification accuracies of our method with those of the state-of-the-art methods in Table 1. The null hypothesis H_0 is $\mu_{\text{AFRN}} < \mu_m$, where μ is the mean classification accuracy and $m \in \{\text{MatchingNet, ProtoNet, CTX, DeepEMD, RENet, MixFSL, FRN, FRN+TDM}\}$.

Ours vs.	MatchingNet	ProtoNet	CTX	DeepEMD	RENet	MixFSL	FRN	FRN+TDM
p value	1×10^{-3}	7×10^{-3}	3.9×10^{-5}	2.8×10^{-4}	2.8×10^{-4}	1.4×10^{-4}	3.3×10^{-5}	7×10^{-3}
Reject at 1% level	✓	✓	✓	✓	✓	✓	✓	✓

311 4.3. Comparison with the state-of-the-art methods

312 We report the classification accuracies of AFRN and the eight state-of-
313 the-art methods on five fine-grained image datasets in Table 1. Obviously,

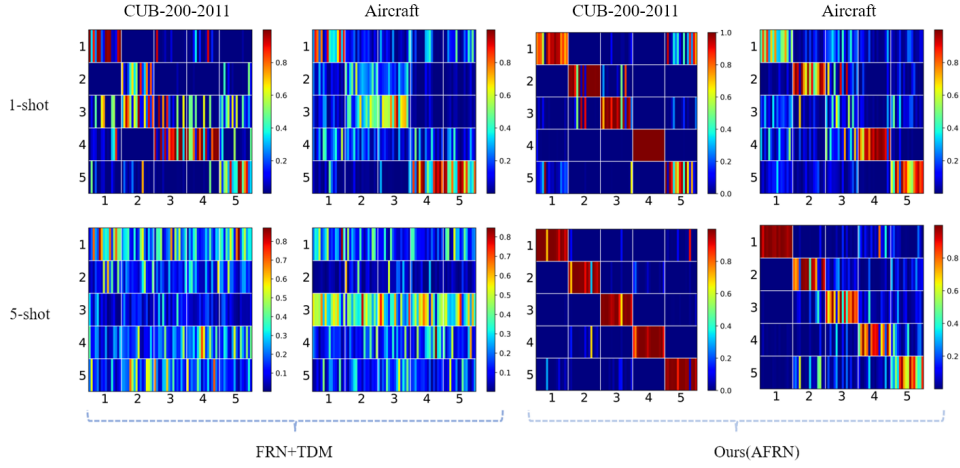


Figure 4: The visualisations of the confusion matrices of AFRN and FRN+TDM on the CUB and aircraft datasets under the 5-way 1-shot and 5-way 5-shot settings.

Table 3: The ablation study on the relaxed TDM module and the centre loss.

	Relaxed TDM	Centre loss	CUB		Aircraft	
			1-shot	5-shot	1-shot	5-shot
(a)	-	-	83.31±0.19	92.70±0.10	70.61±0.21	84.53±0.13
(b)	✓	-	83.73±0.12	92.86±0.10	71.59±0.22	85.06±0.13
(c)	-	✓	83.77±0.18	93.09±0.10	71.05±0.21	84.58±0.13
(d)	✓	✓	83.95±0.18	93.17±0.10	72.19±0.21	85.59±0.13

314 our method can beat all state-of-the-art methods on the CUB, aircraft, flow-
 315 ers and dogs dataset, while providing competitive classification results with
 316 FRN+TDM on the cars dataset. This demonstrates the effectiveness of in-
 317 volving the centre loss and the relaxed TDM module. To have a deep insight
 318 to the results, we compare the visualisations of the confusion matrices of
 319 AFRN and FRN+TDM in Figure 4 on the CUB and aircraft datasets. It is
 320 clear that AFRN is better than FRN+TDM on the two datasets with more
 321 deep red stripes or higher values on the diagonals. To confirm that AFRN is
 322 significantly better than the state-of-the-art methods, we perform one-sided
 323 paired t -test to compare the classification accuracies of AFRN and those of
 324 other methods in Table 1, with a null hypothesis H_0 of $\mu_{AFRN} < \mu_m$, where μ
 325 is the mean classification accuracy and $m \in \{\text{MatchingNet, ProtoNet, CTX,}$
 326 $\text{DeepEMD, RENet, MixFSL, FRN, FRN+TDM}\}$. H_0 can be rejected at 1%
 327 level for all methods compared, suggesting that the classification accuracy of
 328 AFRN is significantly better than those of other methods.

329 4.4. Ablation studies

330 Here we explore the impacts of the relaxed TDM module and the centre
 331 loss on the classification performance and report the results on the CUB and
 332 aircraft datasets in Table 3. For the relaxed TDM column, ‘-’ represents
 333 adopting the original TDM module while ‘✓’ is for the proposed relaxed
 334 TDM module. For the centre loss column, ‘-’ is to train the model by the
 335 original FRN loss in (11) while ‘✓’ represents training the model by the
 336 AFRN loss in (14). Thus, scenario-(a) corresponds to FRN+TDM while
 337 scenario-(d) represents AFRN. Clearly, the classification accuracy of TDM
 338 can be raised by only modifying the inter-class score via the relaxed TDM

339 in scenario-(b). It is worth noting that, for the 1-shot classification of the
 340 aircraft dataset, the accuracy is improved greatly by almost 1%, suggesting
 341 that the subcategories of aircraft are highly similar and the relaxed score is
 342 required to reduce potential overfitting. In scenario-(c), when we only involve
 343 the additional centre loss, the improvement is more substantial for the CUB
 344 dataset, suggesting that the variation within each subcategory of the CUB
 345 dataset is relatively large and thus making intra-class variation smaller via
 346 centre loss is beneficial. Finally, utilising the relaxed TDM module as well
 347 as the centre loss can provide the best classification accuracies.

Table 4: The effect of ν in (14) of the AFRN loss.

ν	CUB		Flowers	
	1-shot	5-shot	1-shot	5-shot
0.5	83.22±0.19	92.75±0.10	82.75±0.19	93.46±0.10
0.05	83.95±0.18	93.17±0.10	83.59±0.19	94.05±0.09
0.005	83.69±0.18	93.07±0.10	82.35±0.20	93.22±0.10

348 4.5. The effect of ν in (14)

349 In this section, we present the effect of ν in (14), i.e. the parameter con-
 350 trolling the contribution of the centre loss, on the classification performance.
 351 The classification accuracies of the CUB and flowers datasets for three values
 352 of ν , 0.5, 0.05 and 0.005, are summarised in Table 4. It shows that 0.05 is a
 353 proper choice. In addition, the accuracies of using the three values of ν are
 354 all higher than or competitive with FRN+TDM.

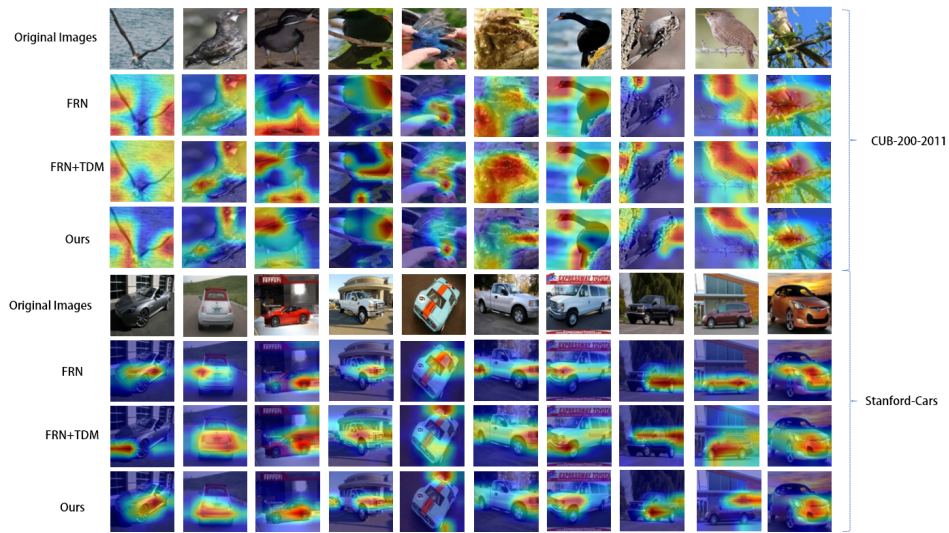


Figure 5: The visualisation of the discriminative features extracted by FRN, FRN+TDM and AFRN ('Ours') on the CUB and cars datasets. AFRN focuses on the most discriminative regions compared with FRN and FRN+TDM.

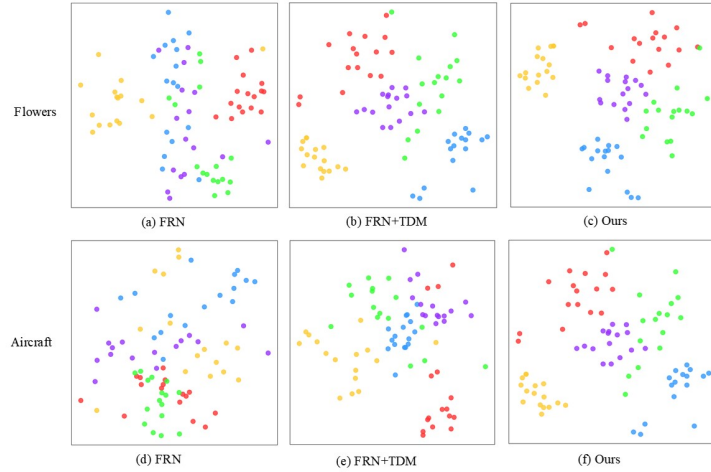


Figure 6: The visualisation of the feature embeddings of FRN, FRN+TDM and AFRN (‘Ours’) on the flowers and aircraft datasets. AFRN can provide the best separation of different classes.

355 4.6. The visual comparisons of FRN, FRN+TDM and AFRN

356 4.6.1. Visualisation of discriminative features

357 To demonstrate that AFRN can focus on the most discriminative regions
 358 for classification, we visually compare the discriminative regions identified by
 359 FRN, FRN+TDM and AFRN, following the Grad-CAM technology [36] in
 360 Figure 5. For the CUB and cars datasets, we randomly select 10 images for
 361 visualisation. We can observe that FRN tends to focus on both the objects
 362 and irrelevant backgrounds. FRN+TDM can improve this by identifying
 363 smaller discriminative regions, while AFRN can usually make the areas even
 364 smaller by focusing on the highly discriminative ones.

365 *4.6.2. Visualisation of feature embeddings*

366 To further show that AFRN can amplify the inter-class discrepancy, we
 367 visualise the feature embeddings learnt by FRN, FRN+TDM and AFRN
 368 via t -distributed stochastic neighbour embedding (t -SNE) [37] in Figure 6.
 369 The results of the flowers and aircraft datasets are presented in the first and
 370 second rows in Figure 6, respectively. For each dataset, we randomly select
 371 five classes with 16 test samples each and label them by different colours. The
 372 five classes are severely mixed in FRN while better separated in FRN+TDM.
 373 Obviously, the best separation of the classes is achieved by FRN: the inter-
 374 class discrepancy is amplified, which also supports our motivation in Figure 1.

375 *4.7. Discussion*

Table 5: The classification accuracies of FRN, FRN+TDM and AFRN (‘Ours’) on two coarse-grained datasets, mini-ImageNet and FC100, with the ResNet-12 backbone. The best classification accuracies are labelled in bold fonts.

	mini-ImageNet		FC100	
	1-shot	5-shot	1-shot	5-shot
FRN	63.26±0.21	77.68±0.15	40.31±0.17	55.34±0.17
FRN+TDM	62.18±0.20	78.41±0.15	39.84±0.17	54.16±0.17
Ours	62.78±0.20	78.60±0.15	40.09±0.18	54.38±0.18

376 In this section, we further test the ability of AFRN to classify coarse-
 377 grained data, where larger categories or super-categories with large intra-
 378 class variations are considered. We adopt two benchmark coarse-grained
 379 datasets, the mini-ImageNet dataset [4] and the FC100 dataset [38]. The
 380 mini-ImageNet dataset contains 60,000 images distributed evenly over 100
 381 classes. We randomly divide the dataset to a training set with 64 classes,

382 a validation set with 16 classes and a test set with 20 classes. The FC100
 383 dataset has 100 object categories which are merged to 20 super-categories.
 384 We randomly divide it to a training set with 12 super-categories containing
 385 60 object categories, a validation set with 4 super-categories containing 20
 386 object categories and a test set with 4 super-categories containing 20 object
 387 categories.

388 The classification accuracies of FRN, FRN+TDM and AFRN on coarse-
 389 grained datasets are reported in Table 5. Clearly, the original FRN dominates
 390 FRN+TDM and AFRN in most scenarios, except for the classification of 5-
 391 shot mini-ImageNet. However, we note that AFRN performs slightly better
 392 than FRN+TDM in all cases, which demonstrate that the two amendments
 393 also work on coarse-grained data, but not effective enough to beat the original
 394 FRN. One explanation to this result is that TDM or relaxed TDM put too
 395 much attention on few channels while ignore information from other channels
 396 that may be valuable for coarse-grained data. Thus, they perform worse than
 397 the original FRN when all channels are considered equally.

398 5. Conclusions

399 In this paper, we propose AFRN, a simple scheme to amplify the inter-
 400 class discrepancy and thus improve the classification performance of FRN+TDM
 401 on few-shot fine-grained images. To mitigate the potential overfitting to the
 402 seen subclasses, we propose to relax the inter-class score in TDM. To enlarge
 403 the subtle differences between the subclasses of fine-grained images, we pro-
 404 pose to incorporate the centre loss to FRN. Extensive experiments on five
 405 fine-grained datasets showcase that our scheme can produce the state-of-the-

406 art performance, verified by statistical tests. Results in ablation study also
407 reveal the effectiveness of each amendment. Moreover, we note one limitation
408 of our method on classifying coarse-grained data, which we identify as our
409 future work.

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- We propose AFRN, a simple scheme to amplify inter-class discrepancy.
- We relax the inter-class score in TDM to mitigate the negative impact of overfitting.
- We incorporate the guidance of the centre loss to FRN to enhance the discriminative power of learnt features.
- The experimental results demonstrate that our scheme is simple yet effective to improve the few-shot classification performance.

Journal Pre-proof

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Declaration of interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

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