## A consumer scalable anonymity payment scheme with role based access control

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#### **Abstract**

#### 1 Introduction

This paper proposes a secure, scalable anonymity and practical payment protocol for Internet purchases, and uses role based access control (RBAC) to manage the new payment scheme. The protocol uses electronic cash for payment transactions. In this new protocol, from the viewpoint of banks, consumers can improve anonymity if they are worried about disclosure of their identities. An agent provides a higher anonymous certificate and improves the security of the consumers. The agent will certify re-encrypted data after verifying the validity of the content from consumers, but with no private information of the consumers required. With this new method, each consumer can get the required anonymity level, depending on the available time, computation and cost.

We also analyse how to prevent a consumer from spending a coin more than once. Furthermore, we use RBAC to manage the new payment scheme. Each user may be assigned one or more roles, and each role can be assigned one or more privileges that are permitted to users in that role. Security administration with RBAC consists of determining operations that must be executed by persons in particular jobs, and assigning employees to proper roles. RBAC can improve system security and reduce conflicts of different roles. The complexities with RBAC can be decreased by mutually exclusive roles and role hierarchies.

**Keywords**: Electronic-cash, Anonymity, Traceability, Hash function.

Recent advances in the Internet and WWW have enabled rapid development in e-commerce. More and more businesses begin to develop or adopt e-commerce systems to support their selling/business activities. While this brings convenience for both consumers and vendors, many consumers have concerns about security and their private information when purchasing over the Internet, especially with electronic payment or e-cash payment. Consumers often prefer to have some degree of anonymity when shopping over the Internet. There are a number of proposals for electronic cash systems. All of them lack flexibility in anonymity. David Chaum [5] first proposed an online payment system that guarantees receiving valid coins. This system provides some anonymity against a collaboration between shops and banks. However, users have no flexible anonymity and banks have to keep a very big database for users and coins. Another on-line Cyber-Coin (http://www.cybercash.com) approach allows clients to make payments by signing fund transfer requests to merchants. The merchants submit the signed requests to the bank for authorization of the payments. The CyberCoin protocol is not fully anonymous since it allows the issuing bank to track every purchase. Furthermore, the scalability of the CyberCoin protocol is questionable since it relies on the availability of a single on-line bank. NetBill [8] extends the above payment mechanism by supporting goods atomicity and certified delivery. The drawbacks of NetBill protocol are the addition of extra messages and the significant increase in the amount of encryption used. The most sophisticated protocol is the SET protocol [15], which was designed to facilitate credit card transactions over the Internet. SET security comes at a considerable computation and communication cost. SET, unlike other simpler on-line protocols, does not offer full anonymity, non-repudiation or certified delivery.

Systems mentioned above are on-line payment systems. They need sophisticated cryptographic functions for each coin, and require additional computational resources for the bank to validate the purchases. Forcing the bank to be online at payment is a very strict requirement. On-line payment systems protect the merchant and the bank against customer fraud, since every payment needs to be approved by the customer's bank. This will increase the computation cost, proportional to the size of the database of spent coins. If a large number of people start using the system, the size of this database could become very large and unmanageable. Keeping a database of the coins ever spent in the system is not a scalable solution. Digicash plans to use multiple banks each minting and managing their own currency with inter-bank clearing to handle the problems of scalability. It seems likely that the host bank machine has an internal scalable structure so that it can be set up not only for a 10,000 user bank, but also for a 1,000,000 user bank. Under the circumstances, the task of maintaining and querying a database of spent coins is probably beyond today's state-of-the-art database systems.

In an off-line protocol, the merchant verifies the payment using cryptographic techniques, and commits the payment to the payment authority later in an off-line batch process. Off-line payment systems were designed to lower the cost of transactions due to the delay in verifying batch processes. Off-line payment systems, however, suffer from the potential of double spending, whereby the electronic currency might be duplicated and spent repeatedly.

The first off-line anonymous electronic cash was introduced by Chaum, Fiat and Naor [7]. The security of their scheme relied on some restricted assumptions such as requiring a function which is similar to random oracle and maps from the second argument onto a special range. There is also no formal proof attempted. Although hardly practical, their system demonstrated how off-line e-cash can be constructed and laid the foundation for more secure and efficient schemes. In 1995, Chan, Frankel and Tsiounis [4] presented a provable secure off-line e-cash scheme that relied only on the security of RSA [19]. This scheme extended the work of Franklin and Yung [13] who aimed to achieve provable security without the use of general computation protocols. The anonymity of consumers is based on the security of RSA and it cannot be changed dynamically after the system is established. NetCents [18] proposed a lightweight, flexible and secure protocol for micropayments of electronic commerce over the Internet. This protocol is designed only to support purchases ranging in value from a fraction of a penny and up. In 2000, David Pointcheval [17] presented a payment scheme in which the consumer's

identity can be found any time by a certification authority. So the privacy of a consumer cannot be protected.

Recently, role based access control (RBAC) has been widely used in database system management and operating system products. In 1993, the National Institute of Standards and Technology (NIST) developed prototype implementations, sponsored external research [10], and published formal RBAC models [11, 14]. Since then, many RBAC practical applications have been implemented [1, 12, 21], because RBAC has many advantages such as reducing administration cost and complexity.

Moreover, as mentioned above, the on-line e-cash payments need more computing resources. Most of the previously designed off-line schemes are only for micropayments. They rely on the heuristic proofs of security and therefore do not formally prevent fraud and counterfeit money. Under these conditions, most on-line and off-line payment schemes do not provide efficient anonymity for consumers. Furthermore, there has been little research done on the usage of RBAC in payment scheme management. Hence, a new payment scheme for the purchases over the Internet with untraceability, flexible anonymity and RBAC management will be very useful and very important.

In this paper, we analyse electronic-payment model first, then propose a new off-line electronic cash scheme, in which the anonymity of consumers is scalable and can be done by consumers themselves. Consumers can get the required anonymity without showing their identities to any third party. Furthermore, to reduce administration cost and complexity and to improve the security of management, we will analyse how to use RBAC to manage the new payment scheme. This is truly anonymous for legal consumers and it can trace consumers' identities for double spending.

The paper is organized as follows. In the following section, some basic definitions and simple examples are reviewed. The payment model and the anonymity provider agent are described in section 3. The design of a new offline electronic cash scheme and its complexity are detailed in section 4 and the security analysis of the scheme and RBAC management such as the relationship of roles are presented in section 5. An example of the new e-cash scheme and how to use it for Internet purchases are given in section 6. Conclusions are included in section 7.

## 2 Some Basic Definitions

## 2.1 Hash functions

H(x) is a hash function. For a given value W it is computationally hard to find a x such that H(x) = W, i.e. collisions are hard to find, where x might be a vector.

Hash function is a major building block for several cryptographic protocols, including pseudorandom generators

[2], digital signatures [3], and message authentication.

## 2.2 DLA and ElGamal encryption system

Discrete Logarithm Assumption ( DLA ) is an assumption that the discrete logarithm problem is believed to be difficult.

The discrete logarithm problem is as follows: given an element g in a group G of order t, and another element y of G, find x, where 0 < x < t - 1, such that y is the result of multiplying g with itself x times. In some groups there exist elements that can generate all the elements of G by exponentiation (i.e. applying the group operation repeatedly) with all the integers from 0 to t - 1. When this occurs, the element is called a generator and the group is called cyclic. Rivest [20] has analyzed the expected time to solve the discrete logarithm problem both in terms of computing power and cost.

For this reason, it has been used for the basis of several public-key cryptosystems, including the famous ElGamal encryption system. ElGamal encryption system [9] is a public key encryption scheme which provides semantic security. Let us briefly recall it.

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step 1. The system needs a group G of order q, and a generator g. The secret key is an element X \in Z_q = \{0,1,...,q-1\} and the public key is Y = g^X. step 2. For any message m \in G, the ciphertext of m is c = (g^r, Y^r m), for a random r \in Z_q - \{0\}. step 3. For any ciphertext c = (a,b), the message m can be retrieved by m = b/a^X.
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## ElGamal encryption scheme

# 2.3 Undeniable signature scheme and Schnorr signature scheme

The undeniable signature scheme, devised by Chaum and van Antwerpen [6], is a non-self-authenticating signature schemes, where signatures can only be verified with the signer's consent. However, if a signature is only verifiable with the aid of a signer, a dishonest signer may refuse to authenticate a genuine document. Undeniable signatures solve this problem by adding a new component called the disavowal protocol in addition to the normal components of signature and verification.

An undeniable proof scheme consists of the following algorithms:

- 1. The key generation algorithm K which outputs random pairs of secret and public keys (sk, pk).
- 2. The proof algorithm P(sk,m) which inputs a message m, returns an "undeniable signature" S on m.

However this proof "S" does not convince anybody by itself. To be convinced of the validity of the pair (m, S), relative to the public key pk, one has to interact with the owner of the secret key sk.

- 3. The confirmation process confirms (sk, pk, m, S), which is an interactive protocol between the signer and the verifier, where the prover (the signer) tries to convince the validity of the pair (m, S).
- 4. The disavowal process is an interactive protocol between the signer and the verifier, where the prover (the signer) tries to prove that the pair (m, S) is not valid (i.e. has not been produced by him).

Schnorr proposed an undeniable signature scheme in 1991 [22]. We simply recall it.

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The system needs primes p and q such that q is divided by (p-1), i.e. q|(p-1), g \in Z_p with order q, i.e. g^0 = 1 (modp), g \ne 1. A consumer generates by himself a private key s which is a random number in Z_q. The corresponding public key v is the number v = g^{-s} (modp). To sign message m with the private key s the consumer performs the following steps:

1. Computes x = g^n (modp), where r \in Z_q is a random number.

2. Computes y = r + se(modq) and output the signature y = r + se(modq) and output the signature y = r + se(modq) and output the public key y = r + se(modq) and checks y = r + se(modq).
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#### Schnorr signature scheme

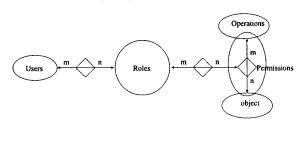
#### 2.4 Role based access control

RBAC is described in terms of individual users being associated with roles as well as roles being associated with permissions (Each permission is a pair of objects and operations). As such, a role is used to associate with uses and permissions. A user in this model is a human being. A role is a job function or job title within the organization associated with the authority and responsibility.

A permission is an approval of a particular operation to be performed on one or more objects. The relationship between roles and permissions is shown in Figure 1, arrows indicate a many to many relationship (i.e. a permission can be associated with one or more roles, and a role can be associated with one or more permissions). The RBAC security model has two components:  $MC_0$  and  $MC_1$ . Model component  $MC_0$ , called the RBAC authorization database model, defines the RBAC security properties for authorization of static roles. Static properties of a RBAC authorization database include role hierarchy, inheritance, cardinality, and static separation of duty.  $MC_1$  called the RBAC activation model, defines the RBAC security properties for dynamic activation of roles. Dynamic properties include role activation, permission execution, dynamic separation of duties, and object access. In particular, the RBAC model supports the specification of:

- a. User/role associations; the constraints specifying user authorizations to perform roles,
- b. Role hierarchies; the constraints specifying which role may inherit all of the permissions of another role,
- c. Duty separation constraints; these are role/role associations indicating conflict of interest:

- c1. Static separated duty (SSD); a constraint specifying that a user cannot be authorized for two different roles,
- c2. Dynamic separated duty (DSD); a constraint specifying that a user can be authorized for two different roles but cannot act simultaneously in both,
- d. Cardinality; the maximum number of users allowed, i.e. how many users can be authorized for any particular role (role cardinality), e.g., only one manager.



Indicates many to many relationships

Figure 1. RBAC relationship

We note that properties a and d depend on how a system is implemented, and they can be decided after the system has been designed. However, properties b and c have to be decided when a system is designed. This is because permissions of different roles may be in conflict compromizing the security of the system. Therefore, this paper will focus on relationships of roles such as Role hierarchies, SSD and DSD.

## 3 Basic model and new payment model

We will show the basic payment model and then discuss the new payment model in this section.

## 3.1 Basic payment model

Electronic cash has sparked wide interest among cryptographers ([20, 25, 16], etc.). In its simplest form, an ecash system consists of three parts (a bank B, a consumer U and a shop S) and three main procedures as shown in Figure 2 (withdrawal, payment and deposit). In a coin's life-cycle, the consumer U first performs an account establishment protocol to open an account with the bank B.

The consumers and the shops maintain an account with the bank, while

- U withdraws electronic coins from his account, by performing a withdrawal protocol with the bank B over an authenticated channel.
- 2. *U* spends a coin by participating in a payment protocol with a shop *S* over an anonymous channel, and

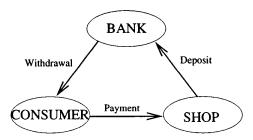


Figure 2. Basic electronic cash system

3. S performs a deposit protocol with the bank B, to deposit the consumer's coin into his account.

The system is *off-line* if the shop S does not communicate with the bank B during payment. It is untraceable if there is no p.p.t. TM (probabilistic polynomial-time Turing Machine) that can identify a coin's origin even if one has all the information of withdrawal, payment and deposit transactions. It is anonymous if the bank B, in collaboration with the shop S, cannot trace the coin to the consumer. However, in the absence of tamper-proof hardware, electronic coins can be copied and spent multiple times by the consumer U. This has been traditionally referred to as double-spending. In on-line e-cash, double-spending is prevented by having the bank check if the coin has been deposited before. In offline e-cash, however, this solution is not possible; instead, as proposed by Chaum, Fiat and Naor [7], the system guarantees that if a coin is double-spent the consumer's identity is revealed with overwhelming probability.

There are also three additional processes such as the bank setup, the shop setup, and the consumer setup (account opening). They describe the system initialization, namely creation and posting of public keys and opening of bank accounts. Although they are certainly parts of a complete system, these are often omitted as their functionalities can be easily inferred from the description of the three main procedures. For clarity we will only describe the bank setup and the consumer setup (because the shop setup is as similar as the consumer setup) for the new scheme in the next section.

Besides the basic participants, a third party named Anonymity Provider (AP) agent will be involved in the scheme. The AP agent will help the consumer to get the required anonymity but will not be involved in the purchase process. The new model can be shown in Figure 3. The AP agent gives a certificate to the consumer when s/he needs a higher level of anonymity.

## 3.2 Anonymity Provider Agent

Here we explain what is an AP agent. Assuming a consumer owns a valid coin  $c=\varphi(pk_B,pk_u,y)$  with its certificate  $Cert_c$ , which guarantees correct withdrawal

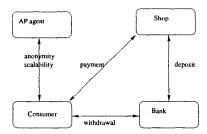


Figure 3. New electronic cash model

from the bank. Where  $\varphi(pk_B,pk_u,y)$  is a function on the public keys of the bank, the user and a variable y, i.e.  $(pk_B,pk_u,y)$ . Whether a coin is valid or not depends on its certificate. Therefore the bank can revoke the anonymity of the consumer if it finds a consumer who spends a coin twice. After the following processes with the AP agent, the consumer owns a new valid coin,  $c' = \varphi(pk_B, pk_u, y + t)$  with its certificate  $Cert_{c'}$ .

- 1. The consumer re-encrypts the coin c into  $c' = \varphi(pk_B, pk_u, y + t)$ .
- 2. The consumer provides an undeniable signature S, using c as a public key associated with the secret key  $sk_u$  of the user, of the equivalence between c and c'. This equivalence is guaranteed by the variable t.
- 3. The consumer confirms the validity of this signature S to the AP agent.
- 4. The AP agent certifies the new coin c' and sends  $Cert_{c'}$  to the consumer.

Indeed, after steps 2 and 3, the AP is convinced that the conversion has been performed by the owner of the coin c; c' is equivalent to c. The owner of c will not be able to deny S (the relation between c and c'). The AP agent should be an electronic notarized participant in the system. It does not need to know any private information about consumers, only verifies the information of consumers.

#### 3.3 Proof of ownership of a coin

This subsection will show how users prove the ownership of a coin. Let us assume that Y is the public key of the bank, and  $I=g^{x_u}$  the identity of a consumer. H(x,y) is a hash function. A coin is the encryption of I:  $c=(a=g^r,b=Y^rI^s)$  which is afterwards certified by the bank, where r,s are random numbers. With the certificate of the bank, one knows that the encryption is valid. Therefore, in order to prove his ownership, the consumer has just to convince of his knowledge of  $(x_u,r,s)$  such that  $b=Y^rI^s$ . This can be expressed as follows.

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1. Consumers choose random k \in Z_p, then compute t = Y^k g^s \pmod{p} and e = H(m,t) where m is a mixed message of c, current time etc, 2. Then compute u = k - re(mod \, p), \, v = s - x_u \, e(mod \, p), and t_1 = g^{(s-1)x_u \, e} (mod \, p), 3. The signature finally consists of (e, u, v, t_1), 4. In order to verify it, one has just to compute t' = Y^u \, g^v \, b^e and check whether t' = tt_1 and e = H(m, t'/t_1).
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#### Proof of validity of a coin $c = Y^r I^s$

Then, a scrambled coin is simply got by multiplying both parts of the old one by respective bases, g and Y, put at a same random exponent  $\rho$ :

$$c' = (a' = g^{\rho}a, b' = Y^{\rho}b) = (g^{r+\rho}, Y^{r+\rho}I^s).$$

Then, if the owner of the old coin has certified the message  $m' = h^{\rho}$ , equivalence of both coins can be proven with the proof of equivalence of three discrete logarithms:

$$log_h m' = log_q(a'/a) = log_Y(b'/b)$$

where h is a public variable.

## 4 Self-scalable anonymity payment scheme

In this section, we propose an anonymity self-scalable payment scheme. The new payment scheme has two main features, the first is that a consumer can have a higher level of anonymity by himself, the second is that the identity of a consumer can not be traced unless the consumer spends the same coin twice.

Our scheme includes two basic processes in system initialization (bank setup and consumer setup) and three main protocols: a new withdrawal protocol with which U withdraws electronic coins from B while his account is debited, a new payment protocol with which U pays the coin to S, and a new deposit protocol with which S deposits the coin to S and has his account credited. If a consumer wants to get a higher level of anonymity after getting a coin from the bank (withdrawal), s/he can contact the AP agent.

## 4.1 System Initialization

The bank setup and the consumer setup are described as follows, and the details of the shop setup are omitted (because the shop setup is similar to the consumer setup).

**Bank setup**: (performed once by B)

Primes p and q are chosen such that  $|p-1|=\delta+k$  for a specified constant  $\delta$ , and  $p=\gamma q+1$ , for a specified small integer  $\gamma$ . Then a unique subgroup  $G_q$  of prime order q of the multiplicative group  $Z_p$  and generator q of  $G_q$  are defined. Secret key  $x_B \in_R Z_q$  for a denomination is created, where  $a \in_R A$  means that the element a is selected randomly from the set A with uniform distribution. Hash function H from a

family of collision intractable hash function is also defined. B publishes p, q, g, H and its public keys  $Y = g^{x_B} \pmod{p}$ .

The secret key  $x_B$  is safe under the DLA. The hash function will be used in payment transactions.

**Consumer setup**: (performed for each consumer U) The bank B associates the consumer U with  $I=g^{x_u} \pmod{p}$  where  $x_u \in G_q$  is the secret key of the consumer and is generated by U.

In system initialization, the communication complexity is O(1) for the consumer only sends its account I of length l bits to the bank, and the computation complexity is O(1). It requires only two exponentiations  $g^{x_B}$  and  $g^{x_u}$ .

After the consumer's account and the shop's account opening, we can describe the new payment scheme.

## 4.2 New off-line payment scheme

We now describe the new anonymity scalable electronic cash scheme which includes withdrawal, payment and deposit.

**Withdrawal**: As usual, an anonymous coin is a certified message, which embeds the public key of a consumer. In our scheme, the message is an encryption of this consumer's public key, using the public key Y of the bank.

Instead of using intricate zero-knowledge proofs to convince the bank of the validity of the encryption, the consumer shows some information to the bank including a signature. So the bank certifies the encryption with full confidence.

The consumer  $I=g^{x_u}$  constructs a coin  $c=(a=g^r,b=Y^rI^s)$  using the public key Y of the bank, where s is a secret key of the coin, which is kept by the consumer and r is a random number in  $Z_q$ . She/He also signs c together with the date, using his private key  $x_u$  and a Schnorr signature. She/He sends both to the bank together with r,I. Then the bank can check the correct encryption. With the signature of the coin and the date, only the legitimate consumer could have done it. After having modified the consumer's account, the bank sends back a certificate  $Cert_c$ . The consumer just has to remember  $(r,s,Cert_c)$ .

Anonymity scalability: The consumer can use the coin now without a higher anonymity since the bank can easily trace any transaction performed through the coin. This is because some information of the consumer such as I,  $Cert_c$  has been known by the bank. To solve this problem, an AP agent is established to help the consumer to make a higher level of anonymity: the consumer can derive a new encryption of his identity in an indistinguishable way. However, the consumer will need a new certificate for a new issued ciphertext. The AP agent can provide this new certificate. Before certifying, the consumer requires both the previous

coin  $(c, Cert_c)$  and the proof of equivalence between the two ciphertexts. Details are described below.

The consumer contacts the AP agent if s/he needs to get a higher level of anonymity. The consumer chooses a random  $\rho$  and re-encrypts the coin:

$$c' = (a' = q^{\rho}a, b' = Y^{\rho}b).$$

- 1. The consumer generates a Schnorr signature S on  $m=h^{\rho}$  using the secret key  $x_u$  as shown in subsection 2.3. Because of S, the consumer will not be able to deny his knowledge of  $\rho$  later. Furthermore, nobody can impersonate the consumer at this step, since the discrete logarithm  $x_u$  of I is required to produce a valid signature. So there is no existential forgery.
- 2. The consumer also provides a designated -verifier proof of equality of discrete logarithms

$$log_h m = log_q(a'/a) = log_Y(b'/b). \tag{1}$$

- 3. The consumer finally sends c, c', S, m to the AP agent.
- The AP agent checks the certificate Cert<sub>c</sub> on c, the validity of the signature S on the message m, then certifies c' and sends back a certificate Cert<sub>c'</sub> to the consumer

After these processes the consumer gets a new certified coin  $c' = (a' = g^{\rho}a, b' = Y^{\rho}b)$  and a new certification  $Cert_{c'}$  which is now strongly anonymous from the point of view of the bank. The AP agent has to keep (c, c', m, S) to be able to prove the link between c and c', with the help of the consumer.

In the withdrawal process, the communication complexity is O(1) since the consumer sends c, I and a signature to the bank and the bank returns  $Cert_c$  to the consumer, twelve exponentiations are required in the withdrawal and anonymity providing process.

Following the process, the AP agent can also give many smaller new coins for an old one since the amount of new one can be embedded in the certificate  $Cert_{c'}$ .

**Payment:** (performed between the consumer and the shop over an anonymous channel)

When a consumer possesses a coin, s/he can simply spend it at shops: proves the knowledge of the secret key  $(x_u, s)$  associated with the coin c or c'. This proof is a signature  $S = (e, u, v, t_1)$  of the new certificate  $Cert_{c'}$ , purchase, date, etc with the secret key  $(x_u, s)$  associated to the coin to the receiver (which is later forwarded to the bank).

In payment transactions, the communication complexity is O(1) for the consumer sending c and a signature  $S=(e,u,v,t_1)$  to the shop. There are six exponentiations for the signature.

Deposit: (The receiver deposits a coin to a bank)

Since the system is off-line, the shop will send the payment transcript to the bank B later. The transcript consists of the coin c or c' (if the consumer applied a higher level of anonymity), the signature and the date/time of the transaction. The bank will verify the correctness of payment and credit the coin into shop's account.

In the deposit, the communication complexity is O(1) because the shop sends the consumer's response c, and signature S=(e,u,v) to the bank. The computation complexity is O(1), since it only verifies whether c or c' was used before or not.

Untracebility: The receiver (shop) deposits the coin into its bank's account with a transcript of the payment. If the consumer uses the same coin c twice, then the consumer will be traced: two different receivers will send the same coin c to the bank. The bank can easily search its records to ensure that c has not been used before. If the consumer uses c twice, then the bank has two different signatures. Thus, the bank can isolate the consumer and trace the payment to the consumer's account I.

In the process of the new scheme, the communication complexity is O(1), the required exponentiations are eighteen which is less than that in [17].

## 5 Security Analysis

We analyze the security of the system from two perspectives. One is from the skill of the system itself, another is from its management. We first start with the skill of the payment scheme.

## 5.1 Payment scheme security

An off-line e-cash scheme is secure [13] if the following requirements are satisfied:

- 1. *Unreusable*: If any consumer uses the same coin twice, the identity of the consumer can be computed.
- Unexpandable: With any number of the customer's valid withdrawal, payment and deposit protocols, no p.p.t. (Probabilistic polynomial time) Turing Machine can compute a legal consumer's identity.
- Unforgeable: With any number of the customer's withdrawal, payment and deposit, no p.p.t. Turing Machine can compute a single valid coin.
- Untraceable: With n withdrawal processes, no p.p.t.
   Turing Machine can compute (n + 1)th distinct and
  valid coin.

The security in the e-cash scheme is based on the hardness of Discrete Logarithms [26] and hash functions. The system preserves the above four requirements.

Unreusable: When a consumer spends a coin, s/he hands over the coin together with a signature  $S=(e,u,v,t_1)$  to a shop. If the consumer uses a coin twice, then we have two signatures  $S_1=(e_1,u_1,v_1,t_{11})$  and  $S_2=(e_2,u_2,v_2,t_{12})$ , where

$$u_1 = k_1 - re_1(modq), \ v_1 = s - x_u e_1(modq).$$

$$u_2 = k_2 - re_2(modq), v_2 = s - x_u e_2(modq).$$

Then  $(v_2 - v_1)/(e_1 - e_2) = x_u$ , this is the secret key of the consumer I. So, a coin in the new scheme cannot be reused.

Untraceable: When a consumer constructs a coin, s/he uses the secret keys  $x_u$  and s, both of which are not shown to any other parts in the purchase process. So no one can trace the consumer and the coin.

Unforgeable: We first discuss whether the bank and the AP agent can forge a valid coin or not. To produce a valid coin, the first requirement is making a encryption  $c=(a=g^r,b=Y^rI^s)$  of I, the second requirement is using the secret key  $x_u$  of the consumer to sign a Schnorr signature of c together with the current time. The bank can do the first step but can not do the second step since it does not know the secret key  $x_u$ . This means the bank can not forge a valid coin. Similarly, the AP agent can not forge a valid coin either. It should be noted that even though both the bank and the AP agent know a valid coin, they still can not use it. This is because there is a signature in payment process which can only be done by the user.

As already seen, the secret key  $x_u$  of a consumer is never revealed, only used in some signatures. A consumer is therefore protected against any impersonation, even from a collusion of the bank, the AP agent, and the shop. Only the consumer can construct a valid coin since there is a undeniable signature embedded in the coin. To prevent the bank from framing the consumer as a multiple spender in the scheme, we use digital signature  $I^s$  for s which is known only by the consumer. Then the system is unforgeable.

Unexpandable: For a legal consumer and a valid coin, the secret key  $x_u$  and the random number s are never shown to others at anytime. Furthermore, usually, the random number s will be changed for different coins. With n withdrawal proceedings, the random number s will be changed n times. Then, no one can compute (n+1)th distinct and valid coins even they see n proceeding withdrawals.

## 5.2 RBAC management

In this section, we will analyze the security of the system from the management viewpoint, and then we will see how to use RBAC to manage the new scheme.

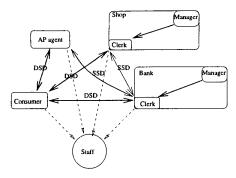


Figure 4. The relationships of the roles in the new scheme

With RBAC, users cannot associate with permissions directly. Permissions must be authorized for roles, and roles must be authorized for users. In RBAC administration, two different types of associations must be managed, i.e. associations between users and roles, and associations between roles and permissions. When a user's job position changes, only the user/role associations change. If the job position is represented by a single role, then when a user's job position changes, only two user/role associations need to be changed: remove the association between the user and the user's current role, and add an association between the user and the user's new role. There are three advantages of RBAC management. Firstly, it will be much easier to manage a system with the use of RBAC. Secondly, RBAC can reduce administration cost and complexity [21]. Thirdly, RBAC is better than ACL (access control list) because ACLs only support the specification of user/permission and group/permission relationships, but the RBAC model supports the specification of user/role and role/role permission relationships.

As we mentioned in subsection 2.4, relationships of roles such as Role hierarchies, SSD and DSD have to be decided when a system is designed. Some relationships like cardinality, the maximum number of users etc, can be decided when the system is in operation.

Now we consider the RBAC management of the new payment scheme. There are four major roles in the system, the AP agent, the consumer, the bank and the shop. The bank and the shop, should be companies comprising many participants. We will not discuss the relationships of all the participants in these companies since they are beyond this paper. We will only consider a manager role in the shop and the bank separately. In Figure 4, there are some dotted lines from four components to staff since all components should be staff. In a shop, the work of a clerk can be decided by the manager, so the manger inherits the clerk, e.g.  $clerk \prec manager$ . The relationship of the clerk and the

manager in the bank is similar to that in the shop.

The AP agent, the shop and the bank have DSD relationships with the consumer. This is because everyone in these three companies can be a consumer, but cannot act at the same time. Then staff in these three companies have to first log out if they want to register as consumers. For example, A consumer, is a staff member of the AP agent, can ask the AP agent to help him to get a higher anonymity. But as a consumer, since the shop and the bank need to check the new coin's certificate  $Cert_{c'}$  and signature, s/he cannot give herself/himself a new certificate  $Cert_{c'}$  of a coin when s/he works for the AP agent. Another staff member of the AP agent can help this person. The AP agent has an SSD relationship with the bank. This is because the duty of the AP agent is to help a consumer to get a higher anonymity. The bank knows the old coin  $c = (q^r, Y^r I^s)$  and its certificate  $Cert_c$ . The AP agent sends the new certificate  $Cert_{c'}$  of the new coin  $c' = (g^{r+\rho}, Y^{r+\rho}I^s)$  to the consumer. The bank will know the new certificate  $Cert_{c'}$  when the AP agent and the bank are authorized by a staff member common in both. If so, the consumer cannot get a required anonymous coin. The shop also has an SSD relationship with the bank since the bank verifies the payment as well as depositing the coin to the shop's account.

## 6 An example and implementations

In this section, we will give a simple example and analyse two different purchase procedures. We will show how to use the new e-cash for Internet purchases and how to get some smaller coins from the AP agent. As a result, we will see the efficiency of the payment protocol.

## 6.1 An example

This example will show the main steps in the e-cash scheme. We omit the details of two undeniable signatures in withdrawal and scalable anonymity process, because they are only used for verifying the user. For simplicity, module 47 which has been used in the computation below is omitted in the expression.

## Bank setup

Suppose  $(p,q,\gamma,k)=(47,23,2,4)$ , then  $G_q=\{0,1,2,...,22\}$  is a subgroup of order 23. g=3 is a generator of  $G_q$ . The bank's secret key  $x_B=4$  and hash function  $H(x,y)=3^x*5^y$ . The bank publishes H(x,y) and  $\{p,q,g\}=\{47,23,3\}$ . The public key of the bank is  $Y=g^{x_B}=34$ .

#### User setup

We assume the secret of a user is  $x_u = 7$  and the user sends  $I = g^{x_u} = 32$  to the bank. After checking some things like social security card or drive license, the bank authorizes the user (consumer) with I.

After the bank setup and the user setup, the user can do purchase.

#### Withdrawal

The user chooses (r,s)=(2,3) and computes  $c=(g^r,Y^rI^s)=(9,2)$ , then signs a Schnorr signature S for the message m=(c,t), where t is the current time. The user sends c=(9,2) and S to the bank, the latter sends back a certificate  $Cert_c$ .

The user contacts the AP agent if s/he needs a high level of anonymity, or uses the coin in a shop directly (See Payment). The user and the AP agent follow the processes below. We suppose h=37 is a public number.

### Anonymity scalability

The user re-encrypts the coin c, chooses  $\rho=4$  and computes  $c'=(a'=g^{\rho}a,b'=Y^{\rho}b)=(24,14)$  and signs a Schnorr signature S on  $m=h^{\rho}=36$ . Finally, the user sends (c,c',S,m) to the AP agent. The latter verifies the Schnorr signature S and the equation (1), and sends a certificate  $Cert_{c'}$  to the user if they are correct.

Since the new coin c'=(24,14) and its certificate  $Cert_{c'}$  has no relationship with the bank, the user has a high anonymity.

## **Payment**

The user signs a signature  $S=(e,u,v,t_1)$  of a message m which includes c',  $Cert_{c'}$  and purchase time etc to prove the ownership of the new coin. For convenience, we assume m=11. The user chooses k=5 then computes  $t=Y^kg^s=19, e=H(m,t)=40, u=18, v=5, t_1=28$ .

The shop computes t'=15 who is convinced that the user is the owner of the coin if the equation of  $t'=tt_1$  and the signature S are successful. She/He does not know who is the user.

#### **Deposit**

The bank will put the money into the shop's account when the checking of the coin C'=(24,14) and the signature  $S=(e,u,v,t_1)=(40,18,5,28)$  are correct. The shop can also see that the money in his account is added.

#### **6.2** Purchase procedures

#### Purchase procedure 1

In purchase procedure 1 a consumer decides how much money should be paid to the shop, withdraws the money from the bank, and pays it to the shop.

- 1. Consumer to shop: The consumer wants to buy some goods in a shop, so contacts the shop for the price.
- Consumer to bank: The consumer gets the money from the bank, the amount being embedded in the signature.

- Anonymity scalability: If the consumer wants to maintain higher level of anonymity, s/he can ask the AP agent to certify a new coin which can be then used in the shop.
- 4. *Consumer to shop*: The consumer proves to the shop that s/he is the owner of the money, and pays it to the shop. Then the shop sends the goods to the consumer.
- 5. Shop to bank: The shop deposits the e-cash in the bank. The bank checks the validation and that there is no double spending of the coin. The bank transfers the money to the shop's account.

## Purchase procedure 2

In purchase procedure 2 is that: the consumer does not have to ask the bank to send money since the consumer already has enough e-cash in his "wallet". All needs to do is to get some smaller e-cash from the AP agent to pay the shop.

There are 4 steps in the purchase procedure 2. They are: (1) consumer to shop; (2) consumer to AP agent; (3) consumer to shop again and (4) shop to bank. Step 2, consumer to AP agent is different from the step 3 in procedure 1 and another three steps are similar to that in procedure 1. Therefore we will focus only on step 2 consumer to AP agent. It should be noted that electronic-cash is a digital message and a certification. We say that the AP agent can provide certificates of coins then provide a service in changing small coin.

Consumer to AP agent: The consumer advises the AP agent of the amount of money to pay the shop from his wallet. She/He can ask the AP agent to make some smaller coins. By doing this, the consumer can also get a higher level of anonymity. After checking the old money sent by the consumer, the AP agent creates some new coins of an equivalent value to the original coin. One of these new coins can be used in the shop.

We have already seen that the consumer can keep money in his wallet or get money from the bank. In both purchase procedures 1 and 2 most computations are done by the consumers, so the system is very convenient for Internet purchases.

## 7 Conclusions

In this paper, a new electronic cash scheme is designed to provide different degree of anonymity for consumers. Consumers can decide the levels of anonymity. They can have a low level of anonymity if they want to spend coins directly after withdrawing them from the bank. Consumers can acheive a higher level of anonymity through the AP agent without revealing their private information and are more secure in relation to the bank because the new certificate of a

coin comes from the AP agent who is not involved in the payment process. This system does not need a trusted party to manage consumers' identities. It is an off-line scheme with low communication and computation. With its scalable anonymity, the new payment protocol can effectively prevent eavesdropping, tampering and impersonation. Finally, we have discussed how to use RBAC to manage the new payment scheme.

## References

- [1] Barkley J. F., Beznosov K. and Uppal J. Supporting relationships in access control using role based access control. In *Third ACM Workshop on RoleBased Access Control*, pages 55–65, October, 1999.
- [2] Bellare M., Goldreich O., and Krawczyk H. Stateless evaluation of pseudorandom functions: Security beyond the birth-day barrier. In Advances in Cryptology Crypto 99, volume 1666 of Lectures Notes in Computer Science. Springer-Verlag, 1999.
- [3] Canetti R., Goldreich O., and Halevi S. The random oracle methodology. In *Proceedings of the 30th ACM STOC '98*, pages 209–218. IEEE, 1998.
- [4] Chan A., Frankel Y., and Tsiounis Y. An efficient off-line electronic cash scheme as secure as RSA. Research report nu-ccs-96-03, Northeastern University, Boston, Massachussets. 1995.
- [5] Chaum D. Blind signature for untraceable payments. In Advances in Cryptology Crypto 82, pages 199–203. Plenum Press N.Y., 1983.
- [6] Chaum D. and Van antwerpen H. Undeniable signatures. In Advances in Cryptology-Crypto89, volume 435 of Lectures Notes in Computer Science, pages 212–216. Springer-Verlag, 1990.
- [7] Chaum D., Fiat A., and Naor M. Untraceable electronic cash. In *Advances in Cryptology Crypto 88*, volume 403 of *Lectures Notes in Computer Science*, pages 319–327. Springer-Verlag, 1990.
- [8] Cox B., Tygar J.D., Sirbu M. Netbill security and transaction protocol. In *The first USENIX Workshop on Electronic Commerce*, New York, 1995.
- [9] ElGamal T. A public key cryptosystem and a signature scheme based on discrete logarithms. *IEEE Transactions* on *Information Theory*, IT-31(4):469-472, 1985.
- [10] Feinstein H. L. Final report: Nist small business innovative research (sbir) grant: role based access control: phase 1. technical report. In SETA Corp., Jan. 1995.
- [11] Ferraiolo D. F. and Kuhn D. R. Role based access control. In 15th National Computer Security Conference, 1992.
- [12] Ferraiolo D. F., Barkley J. F., Kuhn D. R. Role-based access control model and reference implementation within a corporate intranet. In *TISSEC*, volume 2, pages 34–64, 1999.
- [13] Franklin M., Yung M. Secure and efficient off-line digital money. In Proceedings of the Twentieth International Colloquium on Automata, Languages and Programming, volume 700 of Lectures Notes in Computer Science, pages 265-276. Springer-Verlag, 1993.

- [14] Goldschlag D., Reed M., and Syverson P. Onion routing for anonymous and private Internet connections. *Communica*tions of the ACM, 24(2):39-41, 1999.
- [15] MastercardVisa, editor. SET 1.0 Secure electronic transaction specification. http://www.mastercard.com/set.html, 1997.
- [16] Okamoto T. An efficient divisible electronic cash scheme. In Advances in Cryptology-Crypto'95, volume 963 of Lectures Notes in Computer Science, pages 438-451. Springer-Verlag, 1995.
- [17] Pointcheval D. Self-scrambling anonymizers. In Proceedings of Financial Cryptography, Anguilla, British West Indies, 2000. Springer-Verlag.
- [18] Poutanen T., Hinton H. and Stumm M. Netcents: A lightweight protocol for secure micropayments. In The 3rd USENIX Workshop on Electronic Commerce, Boston, Massachusetts, August, 1998.
- [19] Rivest R. L., Shamir A., and Adleman L. M. A method for obtaining digital signatures and public-Key cryptosystems. *Communications of the ACM*, 21(2):120-126, February 1978.
- [20] Rivest R. T. The MD5 message digest algorithm. *Internet RFC 1321*, April 1992.
- [21] Sandhu R. Role activation hierarchies. In Third ACM Workshop on RoleBased Access Control, October, 1998.
- [22] Schnorr C. P. Efficient signature generation by smart cards. *Journal of cryptology*, 4(3):161–174, 1991.
- [23] Wang H., Zhang Y. A protocol for untraceable electronic cash. In Hongjun Lu and Aoying Zhou, editor, Proceedings of the First International Conference on Web-Age Information Management, volume 1846 of Lectures Notes in Computer Science, pages 189-197, Shanghai, China, 2000. Springer-Verlag.
- [24] Wang H., Zhang Y. Untraceable off-line electronic cash flow in e-commerce. In Proceedings of the 24th Australian Computer Science Conference ACSC2001, pages 191–198, Gold-Coast, Australia, 2001. IEEE computer society.
- [25] Yiannis T. Fair off-line cash made easy. In Advances in Cryptology-Asiacrypt'98, volume 1346 of Lectures Notes in Computer Science, pages 240-252. Springer-Verlag, 1998.
- [26] Yiannis T., Yung M. On the security of ElGamal-based encryption. In International Workshop on Practice and Theory in Public Key Cryptography (PKC '98), volume 1346 of Lectures Notes in Computer Science, Yokohama, Japan, 1998. Springer-Verlag.

