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Challenging Data Sets for Point Cloud Registration Algorithms

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Abstract

Many registration solutions have bloomed lately in the literature. The iterative closest point, for example, could be considered as the backbone of many laser-based localization and mapping systems. Although they are widely used, it is a common challenge to compare registration solutions on a fair base. The main limitation is to overcome the lack of accurate ground truth in current data sets, which usually cover environments only over a small range of organization levels. In computer vision, the Stanford 3D Scanning Repository pushed forward point cloud registration algorithms and object modeling fields by providing high-quality scanned objects with precise localization. We aim at providing similar high-caliber working material to the robotic and computer vision communities but with sceneries instead of objects. We propose 8 point cloud sequences acquired in locations covering the environment diversity that modern robots are susceptible to encounter, ranging from inside an apartment to a woodland area. The core of the data sets consists of 3D laser point clouds for which supporting data (Gravity, Magnetic North and GPS) are given at each pose. A special effort has been made to ensure a global positioning of the scanner within millimeter range precision, independently of environmental conditions. This will allow for the development of improved registration algorithms when mapping challenging environments, such as found in real world situations.

The data sets and complementary information are publicly available under the section *Laser Registration Datasets* at:

http://projects.asl.ethz.ch/datasets

1 Motivation

Urban environment navigation has received quite some attention in the last years and triggered the creation of largescale data sets of several kilometer long (Pandey et al. [2011], Huang et al. [2010], Smith et al. [2009]). Even though those data sets are undeniably very useful, other platforms, like the ones used for Search and Rescue missions, encounter a broader range of environments in which the robustness of localization needs to be assessed. Many environments that are likely to be faced are composed of complex structures, and some of them have particular problematic features such as a forest with dense foliage (see Figure 1) that shades GPS signals. On the registration side, the planarity of the environment was taken for granted in early implementations (Chen and Medioni [1991]) and up to recent versions of scan matching algorithms (Pathak et al. [2010]). Clearly, there is a need for semi-structured and unstructured data sets to challenge this planar hypothesis and to validate the robustness of registration solutions in a variety of environments that are encountered in the real world. Recently, Peynot et al. [2010] presented data sets that highlight various situations, but the focus was on atmospheric conditions (airborne dust, smoke and rain). We continue in the same direction but for land-based studies by proposing data sets that cover a larger spectrum of environmental structures, so registration solutions can further be evaluated in real situations.

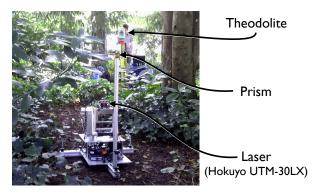


Figure 1: Scanner in targeted unstructured environments with dense foliage cover.

In this data-oriented paper, we present 8 sequences of around 35 point clouds each. The sequences were selected to challenge point cloud registration algorithms with respect to: semi-structured and unstructured environments, rapid variation of scanning volumes, repetitive elements, and finally, dynamic elements. Given that we targeted global positioning evaluations, a special attention was given to the methodology used to record ground truth poses with a consistent protocol for all the sequences.

2 Ground Truth Localization

The notion of *ground truth* is highly dependent on the intention of use and can hardly be absolute. The error of the reference should be significantly lower than the expected outcome of the algorithm to achieve a fair comparison.

Precise global positioning can be reached using an arm that is fixed on a base holding a scanner, but this solution offers a limited motion range. On the other side, GPS and DGPS systems can accommodate a large range of motions but are limited to outdoor locations displaying a clear sky condition. The precision of such systems can be highly variable (i.e., depending of foliage coverage, satellite alignment and number, multi-paths, etc.), which also limits the evaluation of registration precision. Optical motion capture systems, like the one proposed by Vicon, have recently appeared as a precise way to track sensor poses (Pomerleau et al. [2011]). Those systems offer millimeter precision at 100 Hz, but could hardly be installed outdoors or in a highly cluttered environment. Instead of using fixed sensors and mobile markers, Tong and Barfoot [2011] proposed a methodology to reuse directly laser reflectivity readings combined with some reflective beacons. This is a convenient way to ensure ground truth localization in open space, but would lead to the installation of multiple landmarks in a highly occluded environment, like a forest. Finally, Jet Propulsion Laboratory used a theodolite to track specialized prisms fixed on a mobile platform to validate visual odometry performances (Maimone et al. [2007]). The precision reported was less than 2 mm in position, and less than 0.2° in attitude. In addition to the precision, the system reduces infrastructure installation and ensures a fixed precision over all recorded sequences, independently of environmental locations and conditions, which is why we applied this technique to our data sets.

3 Material and Methodology

The data sets were recorded with a partially custom-made rotating scanner used in conjunction with a theodolite, as depicted in Figure 2. The main sensor of the scanner is a laser rangefinder (Hokuyo UTM-30LX) mounted on a tilting device. The sensor has a compact size $(87 \times 60 \times 60 \text{ mm})$ and covers a field of view of 270 degrees with a reading at every 0.25 degree. A comparative study, realized by Wong et al. [2011], concluded that the Hokuyo UTM-30LX has comparable precision and accuracy to the SICK LMS200. The precise control of the motor was ensured by a Maxon Motor EPOS controller. The control system put in place used a dual regulation loop based on 2

encoders. One encoder was located directly on the motor shaft to provide control stability while the second was located at the end of the transmission chain. Encoders had respectively 2000 and 48000 ticks per revolution, the precision difference coping with the gear reduction employed. The later encoder gave us a resolution of 0.00013 rad on the tilting axis. This setup allowed to remove the uncertainty from gear backlash and transmission strap deformation, which was estimated around 5°. Supporting data (Gravity, Magnetic North and GPS) was provided by a consumer grade GPS-aided IMU, Xsens MTi-G.

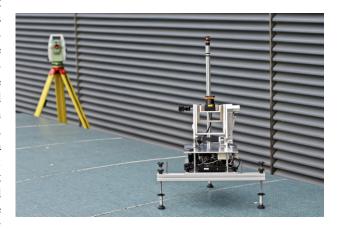


Figure 2: Tilting scanner with the prism mounted at p_0

The theodolite used was the Total Station (TS15) from Leica Geosystems. As it only measures one position at a time, 3 measurements are necessary to retrieve the complete pose (translation and orientation). A specialized reflective prism was mounted on a pole, which could be secured at 3 different locations on the scanner, namely p_0 , p_1 and p_2 (see Figure 3 (a)). A steel guide ensured the pole to be positioned at the same location on the scanner every time. The pole was higher than the scanner to reduce visual occlusion from the theodolite.

Most of the recording process was done manually. The scanner was moved from a location to another by an operator. Extra precautions were taken to ensure that the scanner stayed in place while scanning (usually 20 s) and while the ground truth pose was measured (less than two minutes). On hard floors, rubber feet were used whereas on soft grounds, metal spikes were used. The inertia of the platform also guarantees a good stability while recording a scan. In some cases, like a in compartmented area such as an apartment, a single line of sight cannot track all poses. For those situations, we changed the theodolite pose and then used the last scanner pose as a fixed beacon to relocalize globally the theodolite. We carefully planned those re-localizations to minimize their numbers so that for all the sequences, we never had to relocalize more than twice. We acknowledge that the overall system is costly and time consuming (e.g., 3 hours for 35 scans), but we firmly believe that this methodology is necessary to ensure that high-

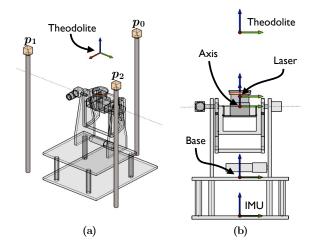


Figure 3: Configuration of the scanner. The dashed line corresponds to the rotation axis. (a) Perspective view with positions of the 3 prisms used to reconstruct the global pose. (b) Reference frame notation.

quality data sets are available for further research.

All sensor data were logged on the same computer so the data are time-stamped based on the same clock. Supporting data were recorded at a different frequency than the laser, and they were segmented per 3D scan pose. In the accompanying web site, we also propose a post-processed version of the supporting data, in which the average values per 3D scan pose can be used.

3.1 Noise Evaluation

In this section, sources of noise, from the global pose down to a measured laser point, are overviewed. The theodolite used has an accuracy proposed by the manufacturer of 1 mm per kilometer. Given the fact that we do not have access to an additional and more precise sensor to validate the ground truth, we evaluated the distances between each prism (d_{12} , d_{02} and d_{01}) over 181 scanner poses measured in different conditions. Figure 4 presents the resulting histograms. The maximum standard deviation (σ_{max}) of the 3 distances is 1.4 mm. Since it is the distance between 2 points, we can assume that σ of one point is approx. 1.0 mm. This error englobes the noise of the theodolite and some human manipulation errors while moving the prism from one position to another.

In the field, we used those inter-prism statistics to cancel spurious pose measurements before taking the 3D scan. The translation component of the global pose is obtained with the mean of the 3 prism positions, which would again lead to a σ_t of $\frac{1.0}{\sqrt{3}} = 0.58$ mm under the assumption of isotropic Gaussian noise. For the rotational components, we used the smallest estimated distance between prisms ($\mu_{12} = 412.5$ mm) and when using basic geometry

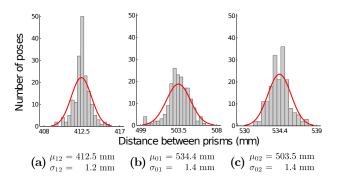


Figure 4: Histograms of the distances between prisms (mm) measured by the theodolite. (a) Distances between p_1 and p_2 . (b) Distances between p_0 and p_2 . (c) Distances between p_0 and p_1

from Figure 5, we can estimate an angular error (σ_{θ}) of 0.003 rad. Those errors applied if the theodolite is kept at the same place during a complete data set recording, which was not the case for 3 data sets. Table 3 shows that, at most, the theodolite was moved 2 times. After a simple error propagation, we can approximate the global position error σ_t to be under 1.8 mm and the orientation error σ_{θ} under 0.006 rad, which is consistent with the level of precision reported by Maimone et al. [2007]. As for the link between the *Theodolite* and the *Base*, the transformation has been computed with a global optimization technique explained in more details in the complementary web site. To evaluate residual errors, we used a different data set then the one used for the optimization.

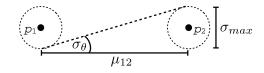


Figure 5: Worst case orientation error given the position error σ_{max} and the smallest expected distance μ_{12} between the prisms p_1 and p_2

As to the transformations from the Laser to the Base, most of them were taken from the construction plans and were machined with a precision under millimeter in centimeter thick aluminum plates. Since encoders work in relative position, a homing procedure needs to be applied to reset the count of the encoders. The offset between the homing position and the position of the rotating frame that is parallel to the Base is directly added in the low level controller (EPOS). This offset has been measured using 2 offthe-shelf laser pointers, typically used for public presentations, fixed on the tilting Axis and on the Base. The 2 laser points were projected on a wall at a distance of 8 m. The angle was adjusted to ensure that the distance between the projected points and the laser pointer were the same. We roughly estimated the homing error σ_h to be under 0.001 rad.

Transform	Sensor	Estimated Pose	Estimated Precision		
$T_{T\leftarrow G}$	Global to Theodolite	t = variable	$0.0006 < \sigma_t < 0.0018 \mathrm{m}$		
		q = variable	$0.0030 < \sigma_{\theta} < 0.0060$ rad		
$T_{B\leftarrow T}$	Theodolite to scanner Base	$t = [0.016 - 0.024 \ 0.606] \mathrm{m}$	residual = 0.004 m		
		$q = [0.000 \ 0.010 \ -0.006 \ -0.999]$	residual = 0.004 rad		
$T_{B\leftarrow A}$	Tilting Axis to scanner Base	$t = [0.000, 0.000, 0.220] \mathrm{m}$	by construction		
	-	q = variable	$\sigma_h < 0.001$ rad		
$T_{B\leftarrow I}$	IMU to scanner Base	$t = [0.000, 0.000, -0.085] \mathrm{m}$	by construction		
		q = [0.000, 0.000, 0.000, 1.000]	by construction		
$T_{A\leftarrow L}$	Laser to tilting Axis	$t = [0.000, 0.000, 0.040] \mathrm{m}$	by construction		
	2	q = [0.001, 0.000, -0.003, 0.999]	by construction		
$T_{L\leftarrow p}$	Point to Laser	$r \in [0.1, 10) \text{ m}$	$\sigma_r < 0.01 \text{ m}$		
· F		$r \in [10, 30]$ m	$\sigma_r < 0.03 \mathrm{m}$		

Table 1: Relative transformation between frames

Finally, the Hokuyo UTM-30LX is a time-of-flight sensor with a minimum range of 0.1 m and a maximal range of 30 m. The specifications of the sensor proposes an accuracy σ_r varying from 0.01 m to 0.03 m depending on the distance and reflectivity of the object.

Values for transformations from different frames depicted in Figure 3 (b) are listed in Table 1 with their estimated precision. We used a right-handed coordinate system with the x-axis pointing forward, y-axis on the left and z-axis upward. All the transformations were given the notation $T_{X \leftarrow Y}$, which can be read as: a transformation T that can express a point, originally in the Y coordinate frame, in a X coordinate frame. Translation vector t is represented as $[t_x, t_y, t_z]$ and the rotation vector q is represented as a quaternion $[q_x, q_y, q_z, q_w]$, where q_w is the real part of the quaternion.

As a general observation, very small angular misalignment can have a large impact on point location at large distances, especially for highly slanted surfaces. For example, we had to tune manually the orientation of *Laser* to the tilting *Axis* by a third of a degree to ensure that a single point cloud joints properly after a rotation of 180°. This slight offset might be due to tolerances in the construction and is related to the divergence of the laser beam that is typically around 1°. Although the global pose of the scanner is in the order of millimeter, it is most likely that the uncertainty of the reflected points in the environment is way larger when the beams have a diameter of several centimeters at a few meters of distance. This uncertainty is inherent to the sensors and occurs in most robotic systems. Further evaluations should be considered to give more precise error bounds.

4 Overview of the Data Sets

The aim of the proposed data sets is to provide unregistered point clouds for researchers who are seeking to evaluate their registration solutions on a common base. The point clouds are provided in *Base* frame, which can be compared against the measured global poses. We also provide globally consistent point clouds for researchers doing environmental modeling. Before presenting the specific sequences, we first introduce the nomenclature used to characterize the different sequences. The abbreviations defined below are reused in Table 2, which also presents an overview of the 8 sequences recorded. The organization of the environment is characterized as follows:

Structured (S): The environment can mainly be explained by geometric primitives (e.g., offices or buildings).

Unstructured (US): The environment mainly involves more complex structures (e.g., a dense forest or a very untidy room).

Semi-structured (SS): The environment has both geometric and complex elements (e.g., partially collapsed building or a park essentially composed of a flat ground and some trees).

Considering a static sensor pose, we also defined 3 types of dynamic elements:

Intra-scan motions (AM): An element is moving while the data are captured. The longer time it takes to capture the data, the more deformed the element will be (e.g., walking persons or cars). This is comparable to motion blur for a fixed camera.

Inter-scan motions (EM): A dynamic event occurs punctually with respect to data acquisition (e.g., moved furniture or doors opened).

Global motions (GM): An event affects the environment at a global scale, and dynamic elements are detected by multi-

ple views recorded at different time periods (e.g., seasonal changes or a building collapsing).

Finally, environment locations are divided into two categories: **Outdoors** (OUT) and **Indoors** (IN).

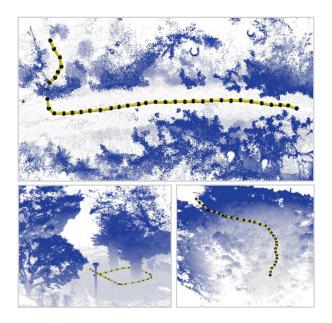


Figure 6: Unstructured and semi-structured data sets. Top: aerial view of *Wood* with the upper part of the vegetation removed. Bottom left: part of *Gazebo* with the wine trees on the right and some large trees on the left. Bottom right: aerial view of *Plain*. For all figures, the lines and black balls correspond to the scanner poses and point clouds were colored to emphasize the depth of the structure from the virtual camera perspective.

The sequences were recorded over half a year (between August 2011 and January 2012). Figures 6 and 8 present a visual overview of all sequences showing the variety of environments covered. Table 3 gives the number of 3D scans, the average number of points per 3D scan and the number of times the theodolite was relocated for each data set. The two last columns give an indication of the volumes covered with a bounding box in which the scanner was moved (*Pose Volume*) and with a bounding box of the global map (*Scene Volume*).

4.1 Unstructured Environments

The sequence named *Wood* is a good example of a challenging environment for registration algorithms that contains both complex structures and intra-scan dynamic elements. Figure 1 shows the starting position of the recorded path. This environment is mainly constituted of vegetation (trees, bushes, etc.) with a small paved road crossing the wood as the only structural element. While recording the data, some people were walking on the road. The scanner path starts in the wood and continues for approximately 12 scans before joining the small road for the next 14 scans. The sequence was recorded at two different seasons (i.e., summer and late autumn), which gives the opportunity to test registration algorithms robustness against Global Motion (i.e., seasonal changes). Figure 7 shows a visible example of the impact of those changes on trees, which were manually extracted from the global map for each season.

Another sequence called *Mountain Plain* was recorded on a small area of an alpine plain located at 1920 m altitude. There is no major vertical structure in the environment and the main element on the ground is dry vegetation (around 50 cm height). The motivation behind this data set is to evaluate robustness of registration algorithms against lowconstrained, unstructured environment. The opposite of a low-constrained environment would be an apartment where the ceiling and walls are large enough to fix the position and orientation of the sensing platform easily. This data set is also very interesting because the hypothesis of a planar motion of the scanner does not hold since the scanner is going down a hill before ending in a flat area.

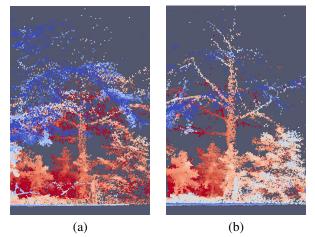


Figure 7: Extracts of global representations highlighting seasonal changes: (a) summer, (b) late autumn. Point cloud colors were selected to enhance depth of the screenshot.

4.2 Other Environments

To ease comparisons between a more complete spectrum of environmental structures, we also provide 5 more sequences recorded with the same methodology. The two sequences named *Gazebo* were recorded in summer and winter in a park, in which there were grass, paved small roads and sparse trees. The main construction is a gazebo with rock walls and a ceiling covered with wines trees. This place is a good representative of semi-structured environments with a mixture of man-made structures and vegetation. Some people were walking while the scanner was recording, whereas others stayed seated for several scans

Sequence Name	IN	OUT	S	SS	US	AM	EM	GM	Particularities
ETH Hauptgebaude Apartment	√ √		√ √			\checkmark	5		Repetitive elements like pillars. Single floor apartment with 5 rooms.
Stairs	\checkmark	\checkmark	√				•		Rapid variations of scanning volumes.
Gazebo (x2) Mountain Plain		\checkmark		\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	Recorded in summer and in winter. Pasture with few vertical structures.
Wood (x2)		\checkmark			\checkmark	\checkmark		\checkmark	Recorded in summer and in autumn.

Table 2: Overview of the data sets with their characteristics

	Nb. Scans	Nb. Points per Scan	Re-localization	Poses Volume	Scene Volume
Sequence Name				$(\mathbf{x} \times \mathbf{y} \times \mathbf{z})$	$(\mathbf{x} \times \mathbf{y} \times \mathbf{z})$
ETH Hauptgebaude	36	191 000	0	$24 \times 2 \times 0.50 \text{ m}$	$62 \times 65 \times 18 \text{ m}$
Apartment	45	365 000	2	$5 \times 5 imes 0.06$ m	$17 \times 10 \times 3$ m
Stairs	31	191 000	0	$10 \times 3 \times 2.50$ m	$21 \times 111 \times 27 \text{ m}$
Gazebo Summer	32	170 000	1	$5 imes 4 imes 0.07 \ m$	$35 \times 45 \times 16$ m
Gazebo Winter	32	153 000	1	$4\times5\times\!\!0.09\ m$	$72{\times}~70{\times}19~m$
Mountain Plain	31	102 000	0	$18 \times 6 \times 2.70 \text{ m}$	$36\!\times 40\times 8\ m$
Wood Summer	37	182 000	0	$10 \times 15 \times 0.50$ m	$30{\times}~53{\times}20~m$
Wood Autumn	32	178 000	0	$6 \times 12 \times 0.50 \text{ m}$	$36 \times 60 \times 22$ m

Table 3: Characteristics of the point clouds for each data set

under the gazebo. The sequence called Stairs aims at evaluating robustness of registration algorithms against rapid variations of scanned volumes. The path starts indoors, crosses some doorways and finishes outdoors. The scanner passes over 5 steps, which offers a more complex motion than a flat floor. ETH Hauptgebaude tackles the problem of repetitive elements with multiple pillars and arches in a hallway. Those elements may create multiple local minima, which can trigger interesting observations for registration algorithms. Finally, the sequence Apartment is a well-structured environment including: a kitchen, a living room, a bathroom, an office and a bedroom. Special care was taken to include outer-scan motion by moving a person, some furniture and boxes in between scans. The registration complexity of this environment is considered low, so it could be used as a reference for other types of environments. In both sequences ETH Hauptgebaude and Apartment, the scanner moved indoors on a flat ground.

5 Data Formats

All data are available as comma-separated value (csv) files with the first line consisting of headers. This format is natively supported by many languages and software (including Matlab, Python) and can be easily parsed. Point clouds are available in local coordinates (i.e, frame named *Base* in Figure 3 (b)) and in global coordinates. The provided ground truth poses directly give the transformation from the origin to the frame *Base* for a given scan. The axis origin of the global coordinate was selected to be the first scanner pose of each data set. Supporting data are given in the *IMU* frame. Moreover, we provide screenshots of all sensor information and photographs of the environments to facilitate the understanding of the scene context. No ground truth informations are available for dynamic elements included in the scenes. For a rapid overview of the data sets, we also provide VTK files in global coordinates. More explanations on all file headers and contents are available on the web site.

6 Conclusion

In this paper, we introduced new data sets covering a diversity of challenging environments for registration algorithms. Although some of those environments can be found in available data sets, our *Laser Registration Data Sets* englobe them all in a coherent group recorded with the same methodology and material. We achieved precise localization of the scanner using a theodolite, which gave us the ability to record data sets in GPS denied environments, indoors or outdoors with the same setup. The precision achieved is also higher than when using data sets that are already available to the community, which should ease the evaluation of registration algorithms on a fair base.

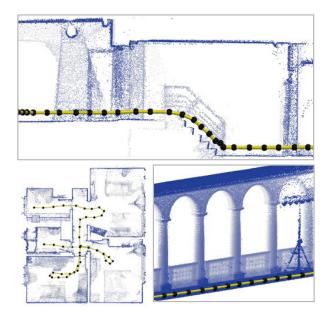


Figure 8: Structured data sets. Top: side view of the *Stairs*. Bottom left: top view of the *Apartment* with the ceiling and floor removed. Bottom right: cut view of a hallway from *ETH Hauptgebaude* showing arches and pillars. For all figures, the lines and black balls correspond to the scanner poses and point clouds were colored to emphasize the depth of the structure from the virtual camera perspective.

Acknowledgements

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