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# ***Reliability* and *Timeliness* Analysis of *Fault-tolerant* Distributed Publish/Subscribe Systems**

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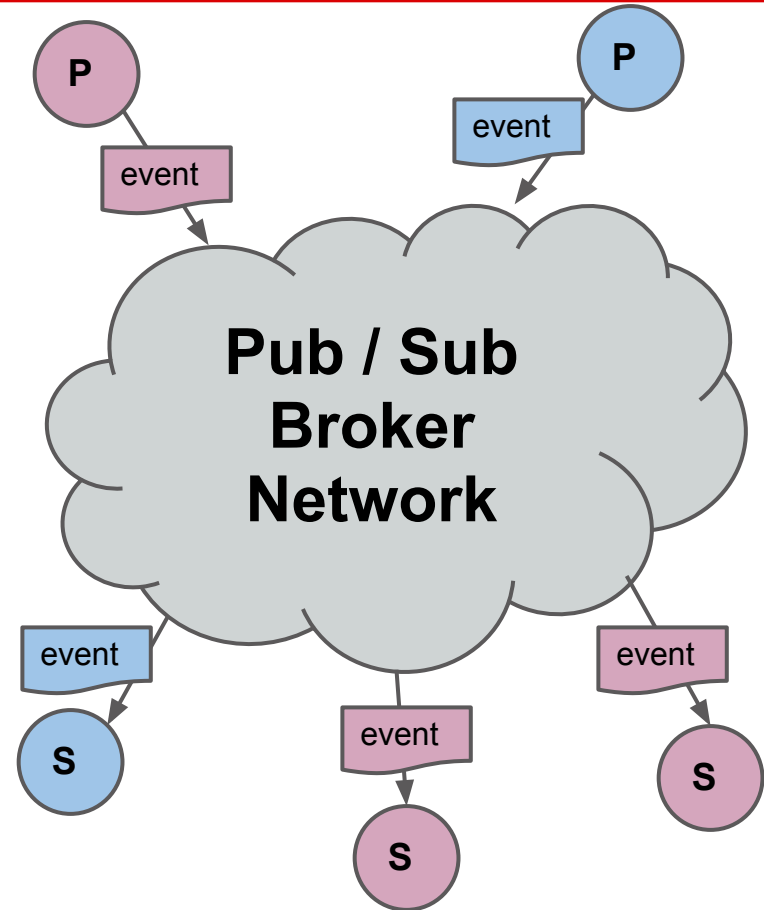
Guijun Wang  
Boeing Research and Technology



# Publish / Subscribe Systems

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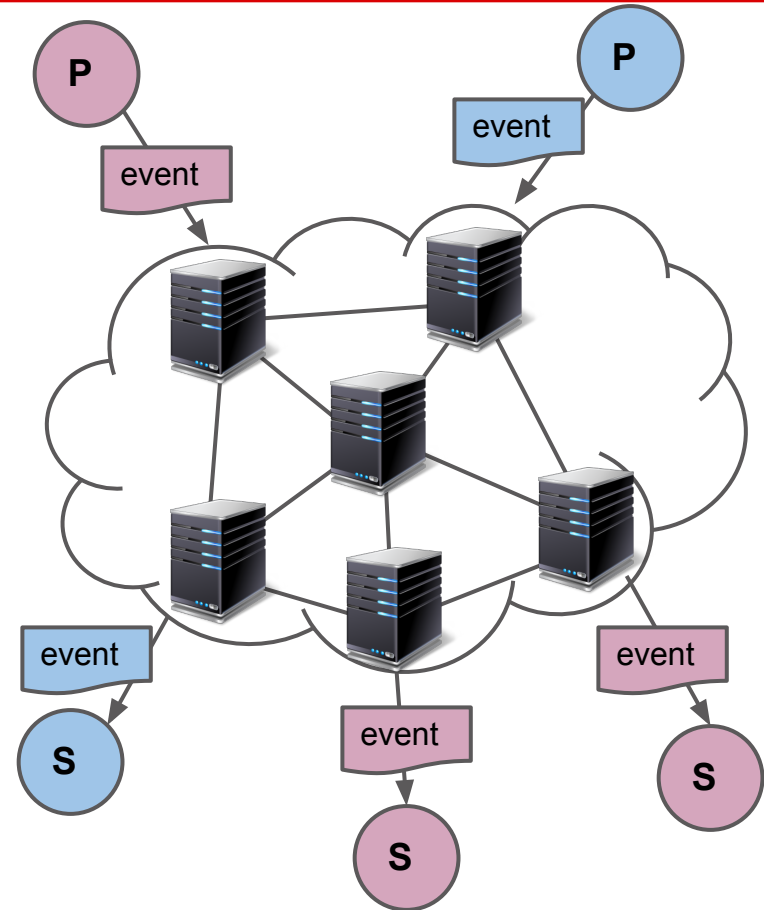
- Pub/sub system is an interest-based communication paradigm
- Each user can be either publisher or subscriber.
- Pub/sub broker network handles routing / matching / recovery.



# Publish / Subscribe Systems

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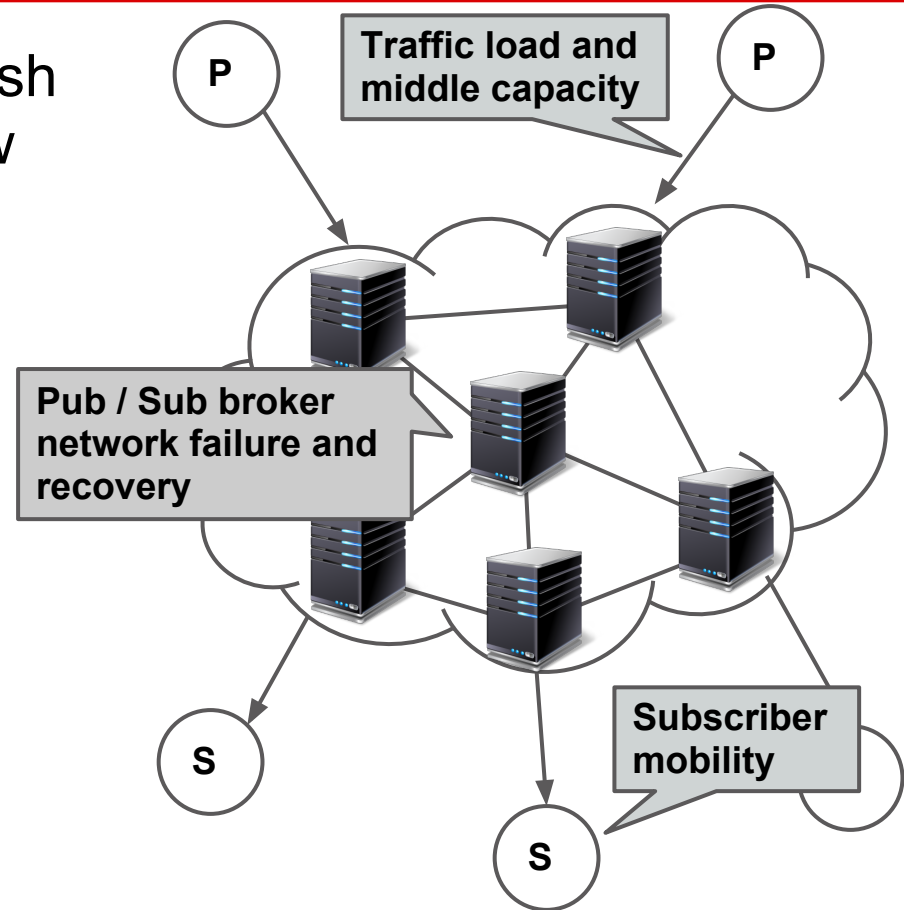
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# Goal : Pub / Sub Performance Analysis

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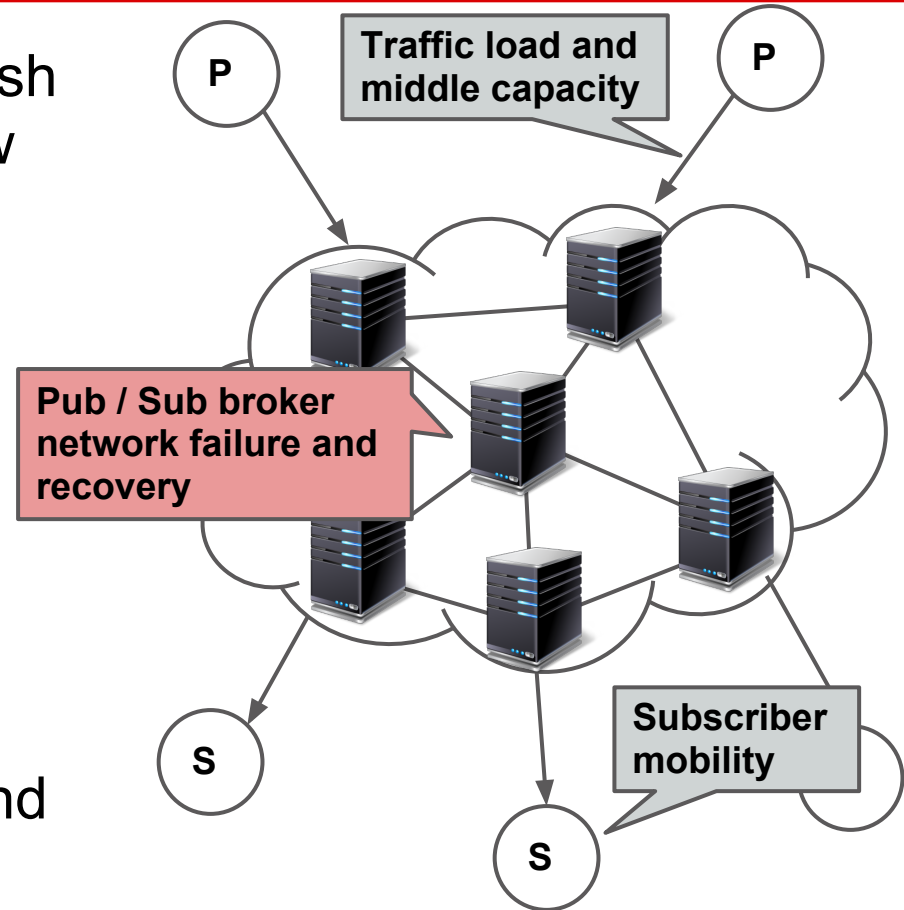
- Question : Given a publish / subscribe network, how to predict reliability / timeliness perceived by each subscriber ?
- Several factors affect subscriber's QoS.



# Goal : Pub / Sub Performance Analysis

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- Question : Given a publish / subscribe network, how to predict reliability / timeliness perceived by each subscriber ?
- Several factors affect subscriber's QoS.
- This paper focuses on broker network failure and recovery.



# Goal : Pub / Sub Performance Analysis

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This paper proposes an analytical model that :

- captures failure / recovery behavior of publish / subscribe middleware.
- predicts reliability and timeliness perceived at each subscriber.
- supports several commonly used publish / subscribe fault tolerance algorithms

The proposed analytical model can be used in :

- subscriber admission control
  - broker network planning
  - fault-tolerant publish / subscribe protocol selection
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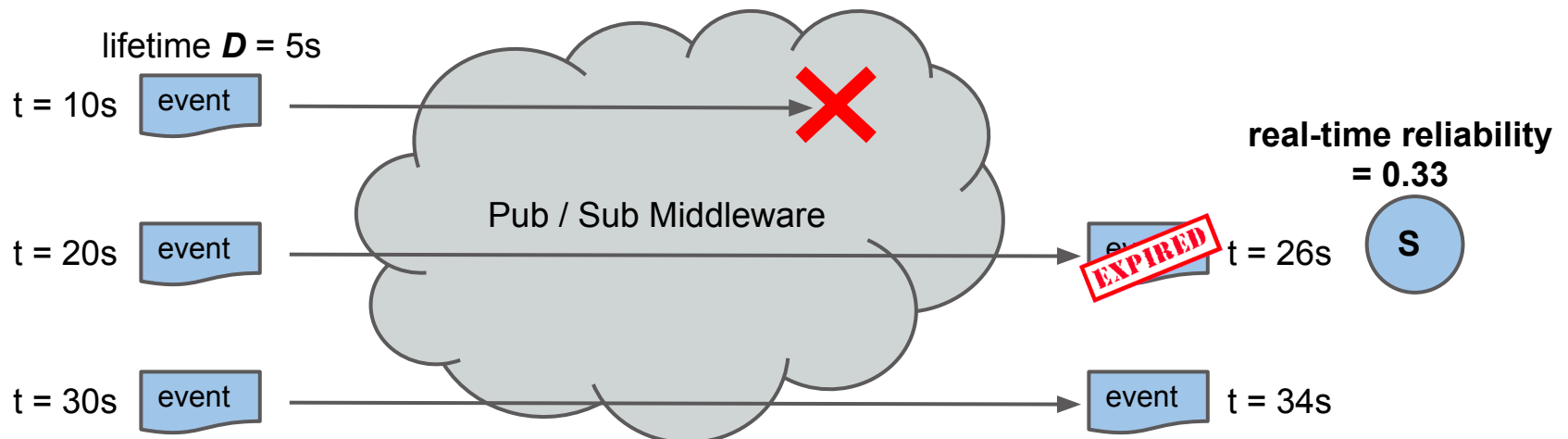
# Outline

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- Motivation
  - ***Model & Assumptions***
  - Reliability / Timeliness Analysis
  - Results
  - Conclusion
-

# Model : Subscriber Real-time Reliability

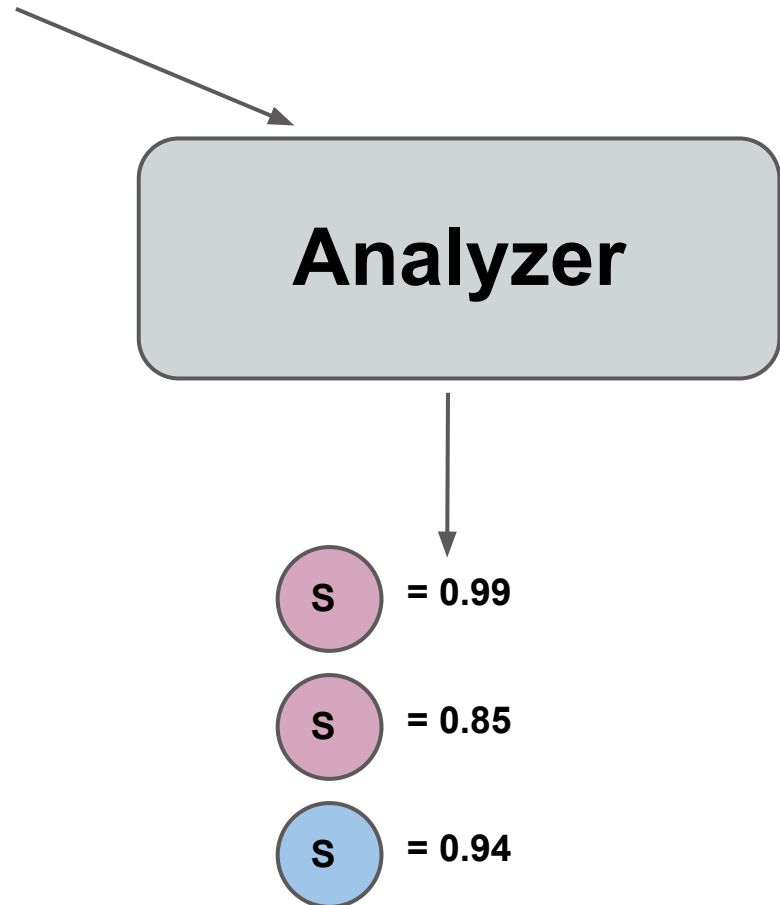
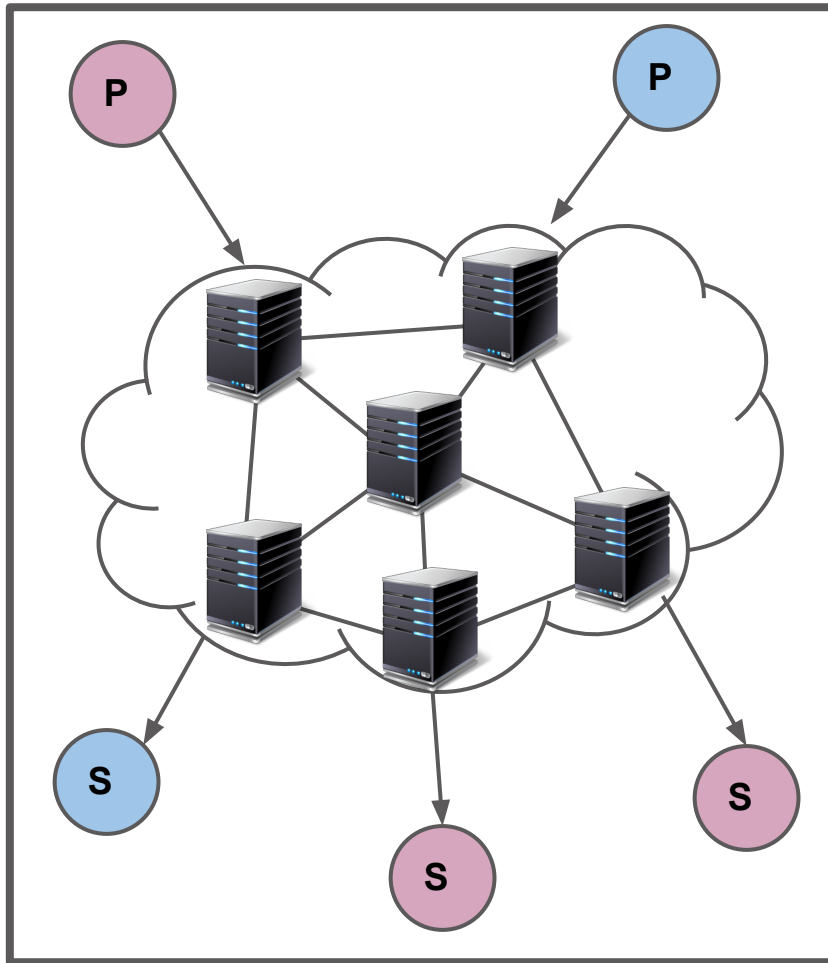
- Each published event has its **lifetime** (i.e., the period of time after which the event is expired after being published). In this paper, we assume all events have the same lifetime value  **$D$** .
- **Subscriber Real-time Reliability** = fraction of events of subscriber's interest that are delivered to the subscriber before they are expired.








# Analytical Framework

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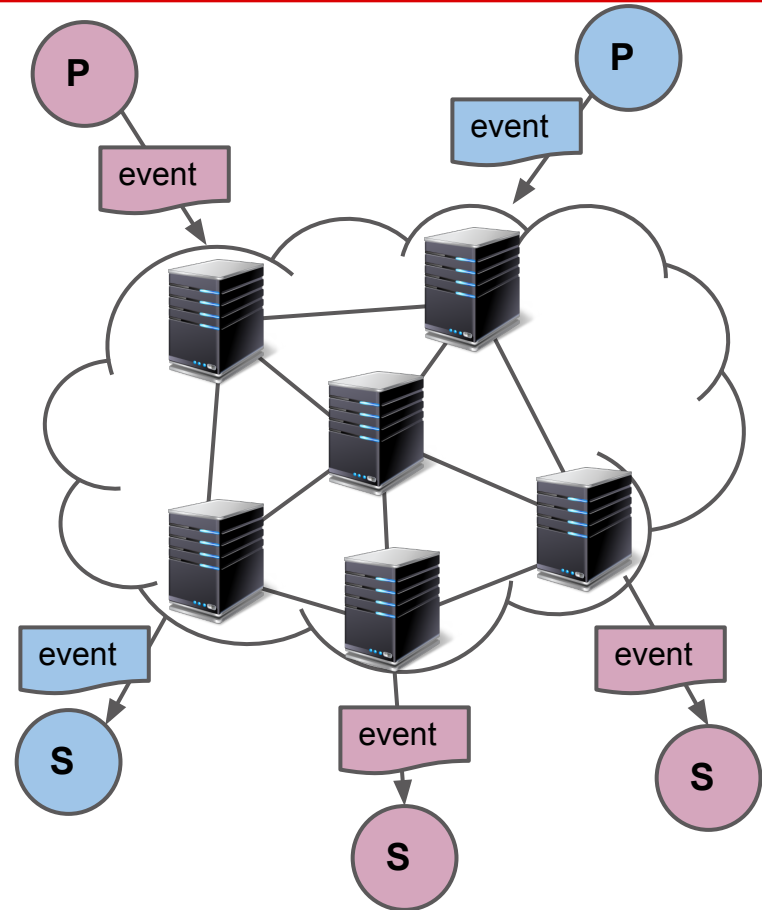
# Model : System Components

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Component	Known Variables
 <p>Subscribers</p>	<ul style="list-style-type: none"><li>• Each subscriber's topic <math>\tau_s</math></li></ul>
 <p>Publishers</p>	<ul style="list-style-type: none"><li>• Each publisher's topic <math>\tau_p</math></li><li>• Each publisher's average publishing rate <math>\lambda_p</math> (events / second)</li></ul>
 <p>Brokers / Links</p>	<ul style="list-style-type: none"><li>• Each broker's failure rate <math>\gamma_B</math> (exponentially distributed)</li><li>• Each broker's recovery rate <math>\sigma_B</math> (exponentially distributed)</li><li>• Each link's failure rate <math>\gamma_L</math> (exponentially distributed)</li><li>• Each link's recovery rate <math>\sigma_L</math> (exponentially distributed)</li></ul>

# Assumption : Pub/Sub Routing

- Upon joining, a new subscriber subscribes to its local broker.
- The local broker stores the subscription to its routing table and propagates the subscription to other brokers.
- The model supports any pub/sub routing protocol that has **path consistency** property (i.e., always use the same broker path to route events from a publisher to a subscriber)



# Outline

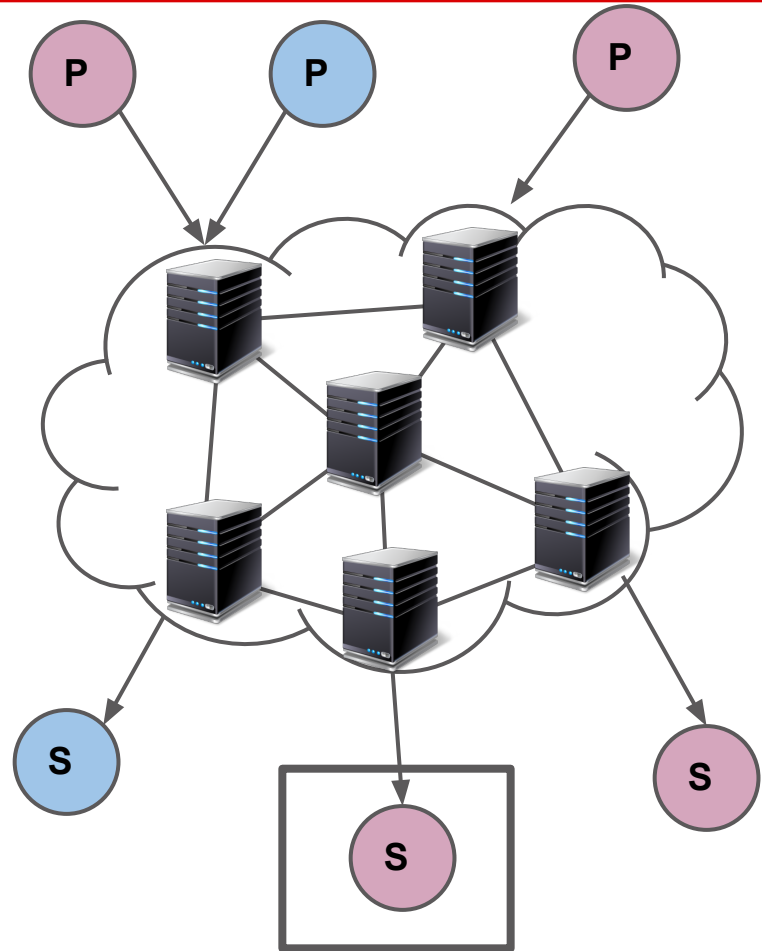
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# Reliability / Timeliness Analysis

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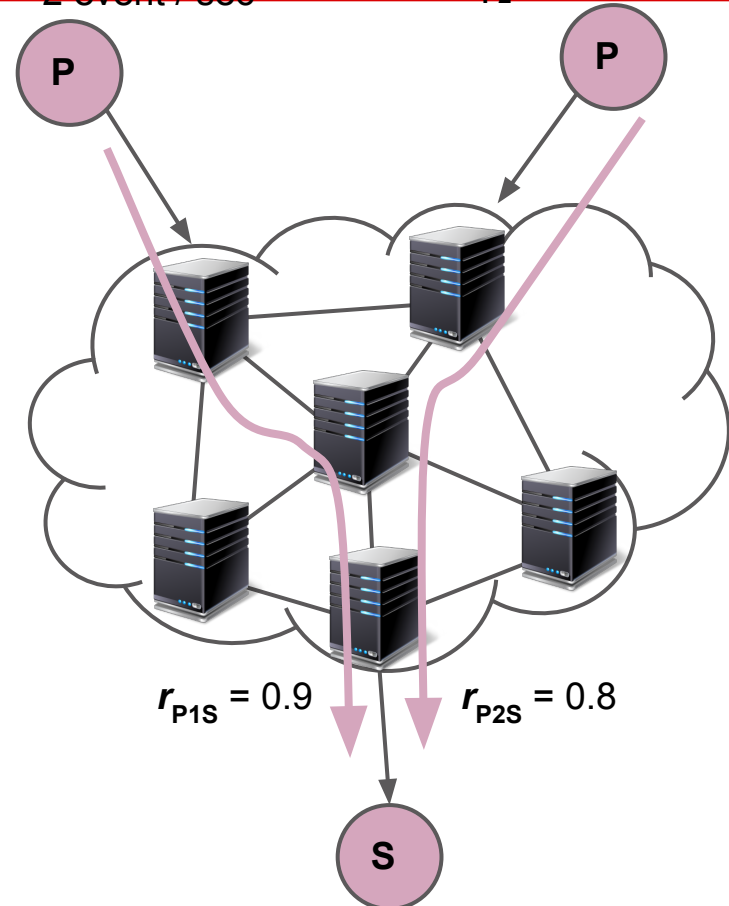
- Question : Given the entire publish / subscribe graph and each component's parameters, how can we estimate each subscriber's real-time reliability?



# Reliability / Timeliness Analysis

- Question : Given the entire publish / subscribe graph and each component's parameters, how can we estimate each subscriber's real-time reliability?
- Answer : Assuming path consistency property, estimate pair-wise real-time reliability between each publisher - subscriber pair.
- Subscriber real-time reliability is then equal to the weighted average of all pair-wise reliability between the subscriber and all publishers with the same topic.

$$\lambda_{P1} = 2 \text{ event / sec} \qquad \lambda_{P2} = 1 \text{ event / sec}$$

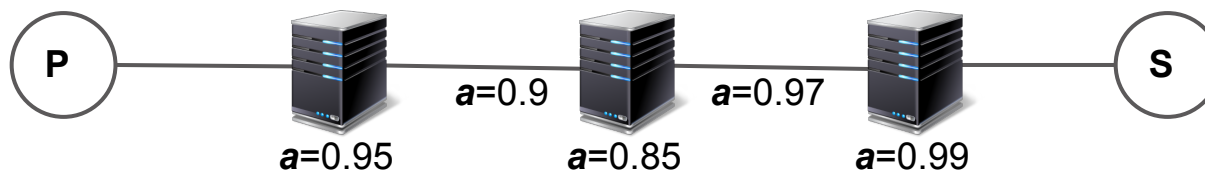


$$r_s = (0.9 \cdot 2 + 0.8 \cdot 1) / (2 + 1) = \mathbf{0.87}$$

# Pair-wise Reliability : Basic Routing

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- In basic protocol, an event is loss if at least one component along the path fails.
- Each broker  $B$  has availability  $a_B$ , which is equal to  $(1/\sigma_B) / (1/\gamma_B + 1/\sigma_B)$
- Each link  $L$  has availability  $a_L$ , which is equal to  $(1/\sigma_L) / (1/\gamma_L + 1/\sigma_L)$
- Pair-wise reliability is the multiplication of each component's availability.



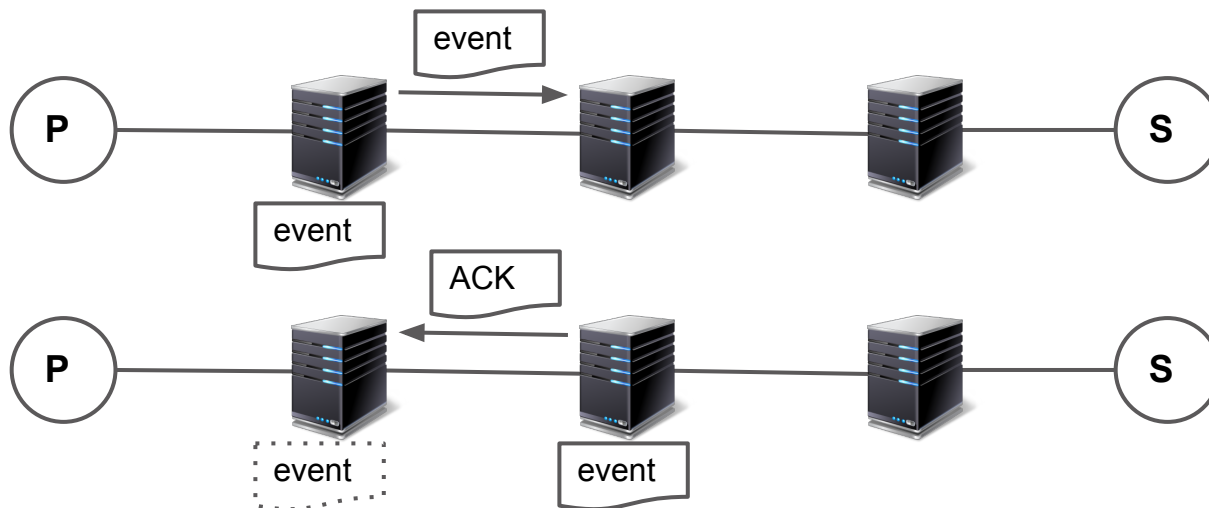
$$r_{PS} = 0.95 * 0.9 * 0.85 * 0.97 * 0.99 = \mathbf{0.70}$$

# Event Retransmission

([Chand & Felber '04][Espository et al '09])

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- In retransmission protocol, each broker stores incoming event into its persistent storage before sending acknowledgement back to the sender.
- The broker keeps retransmitting event until it receives acknowledgement message from the next hop, then it discards the buffered event.
- In retransmission protocol, an event will never get lost at broker or link. However, an event may expire due to buffering delay.

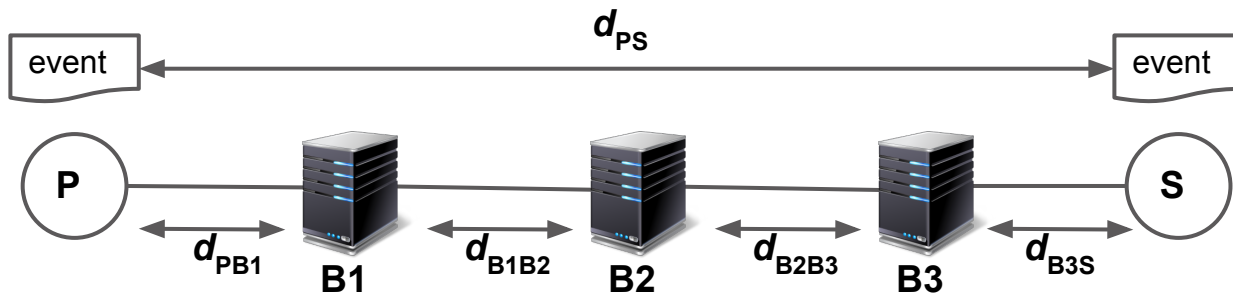




# Pair-wise Reliability : Retransmission

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- To compute path reliability in retransmission protocol, we compute the probability that the end-to-end delivery delay is less than the event lifetime.



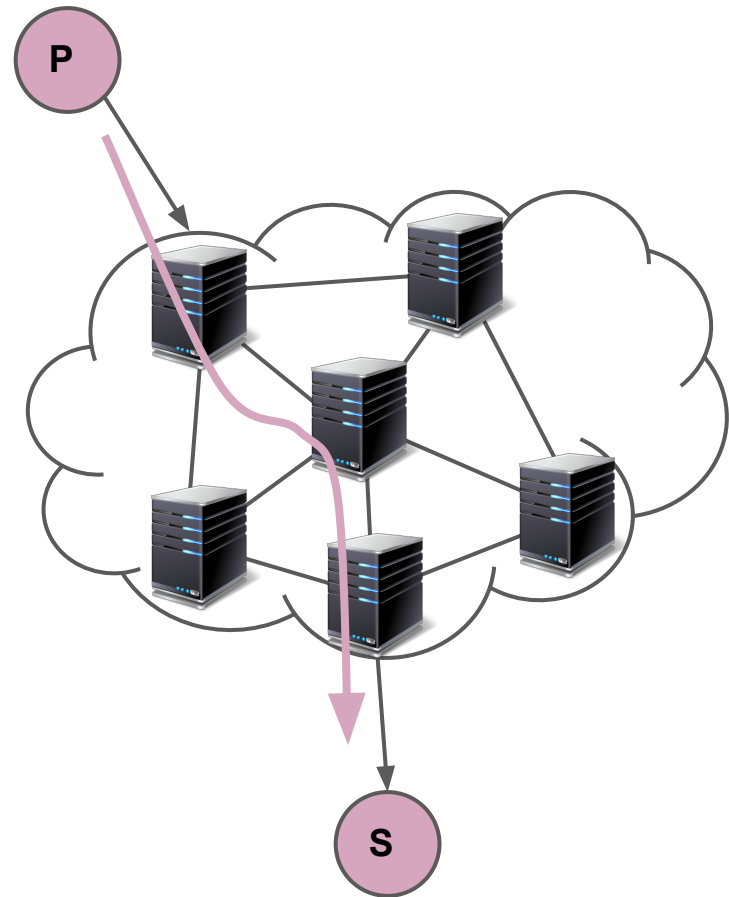
$$r_{PS} = P[d_{PS} < D] = P[d_{PB1} + d_{B1B2} + d_{B2B3} + d_{B3S} < D]$$

- Assuming all brokers / links failure and recovery durations are exponentially distributed, we can estimate per-hop delivery delay distribution using Markov theory (See paper for proof).
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# Multi-path Routing ([Chand & Felber '04][Jaeger '07] [Kazemzadeh & Jacobsen '09])

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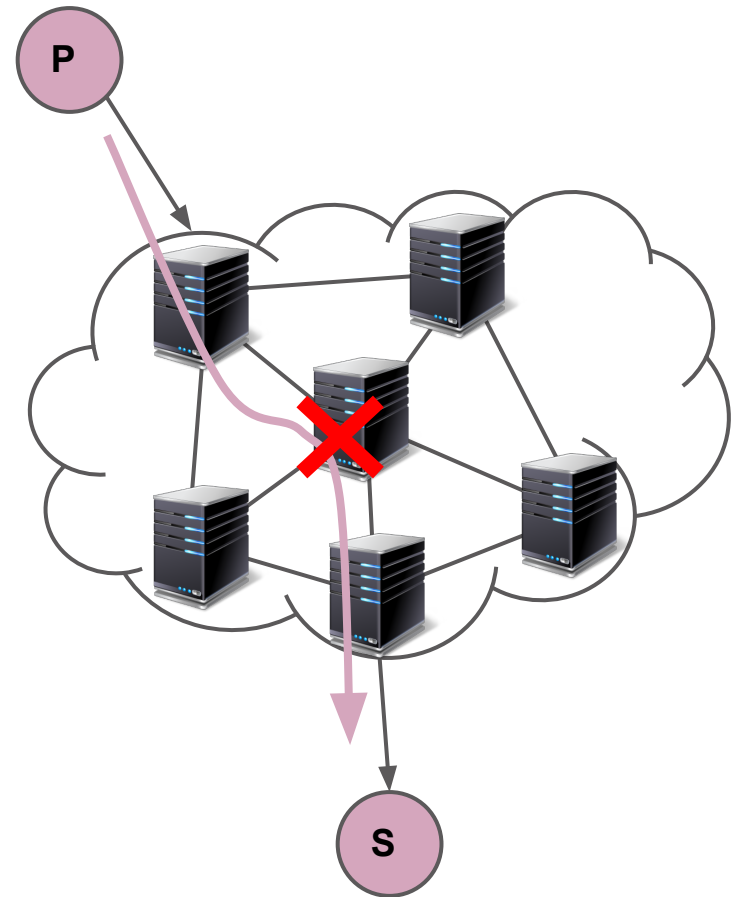
- Brokers run failure detection and new path discovery protocol.
- If the next hop fails, broker forwards event to an alternative neighbor.
- Assuming relatively fast discovery protocol, the event is always delivered on time as long as the publisher and subscriber are connected.



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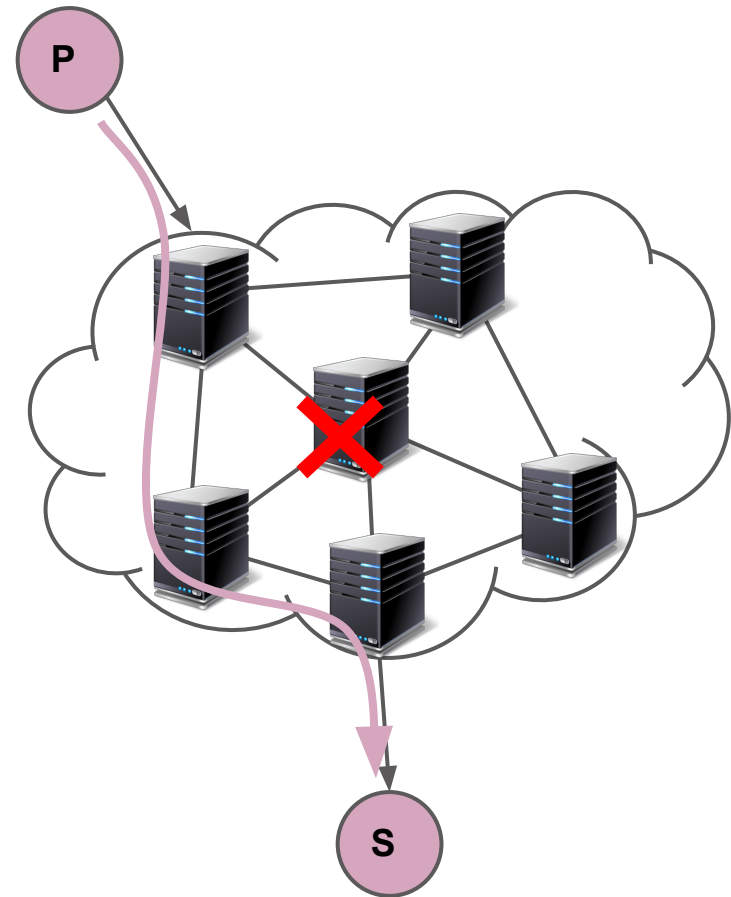
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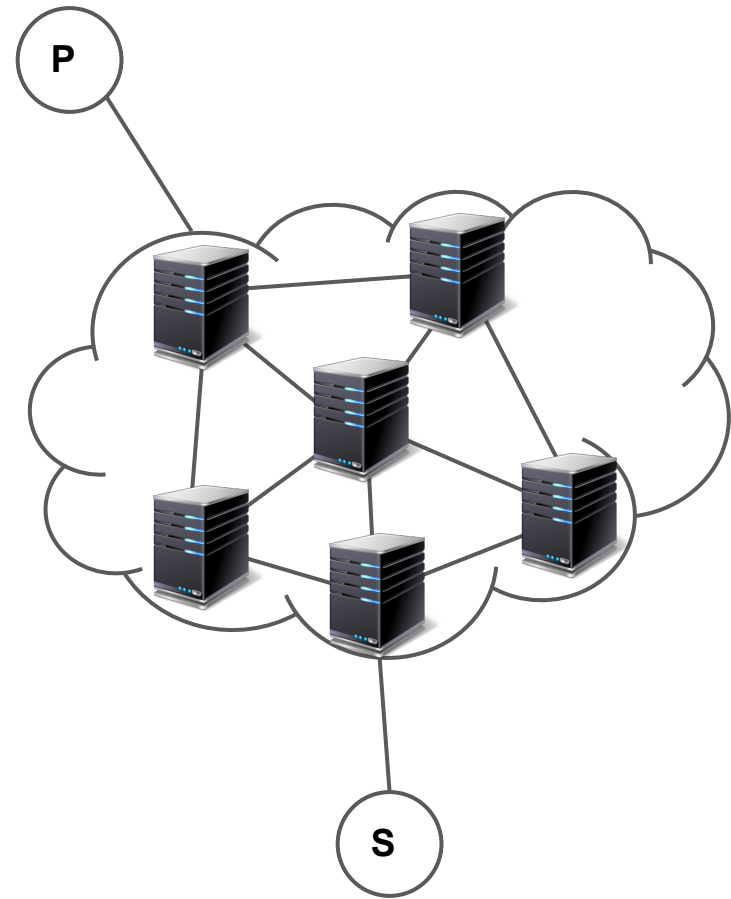
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# Pair-wise Reliability : Multi-path Routing

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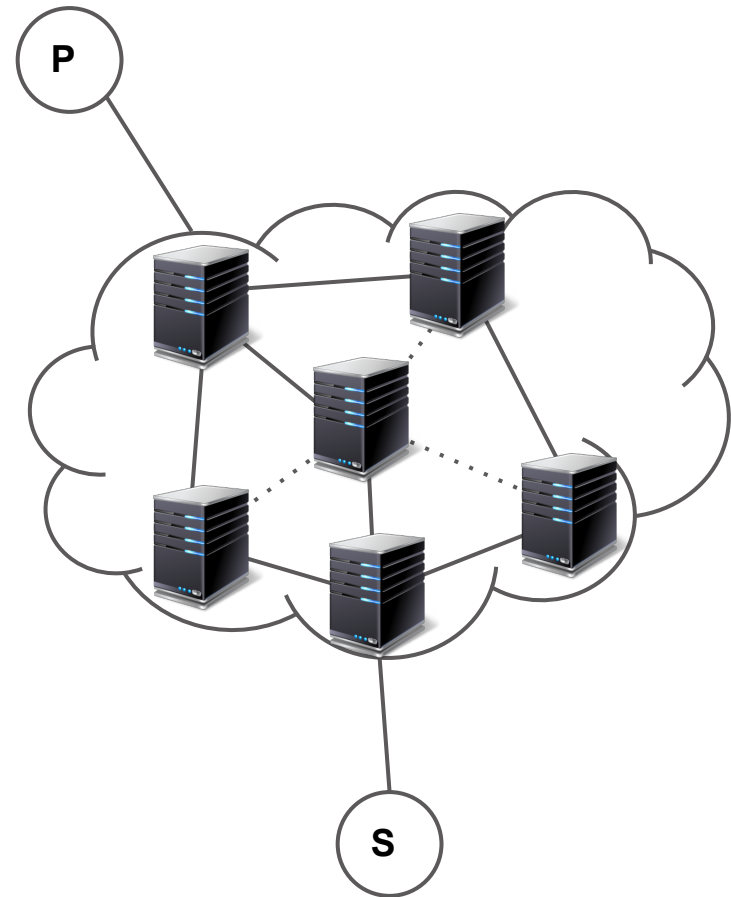
- Pair-wise reliability between publisher and subscriber with multi-path routing is equal to the probability that the publisher and subscriber is connected.
- Finding connection probability in a graph is NP-hard.



# Pair-wise Reliability : Multi-path Routing

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- Pair-wise reliability between publisher and subscriber with multi-path routing is equal to the probability that the publisher and subscriber is connected.
- Finding connection probability in a graph is NP-hard.
- Estimate lower bound instead by reducing the graph into multiple independent paths.

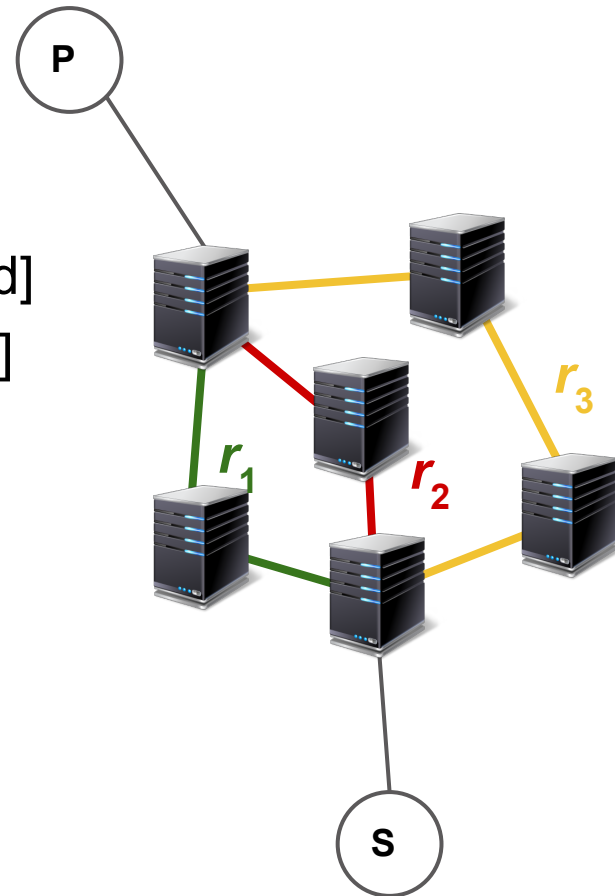


# Pair-wise Reliability : Multi-path Routing (Cont.)

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$$\begin{aligned} r_{PS} &> P[\text{at least one path is connected}] \\ &= 1 - P[\text{all paths are disconnected}] \\ &= 1 - (1 - r_1)(1 - r_2)(1 - r_3) \end{aligned}$$

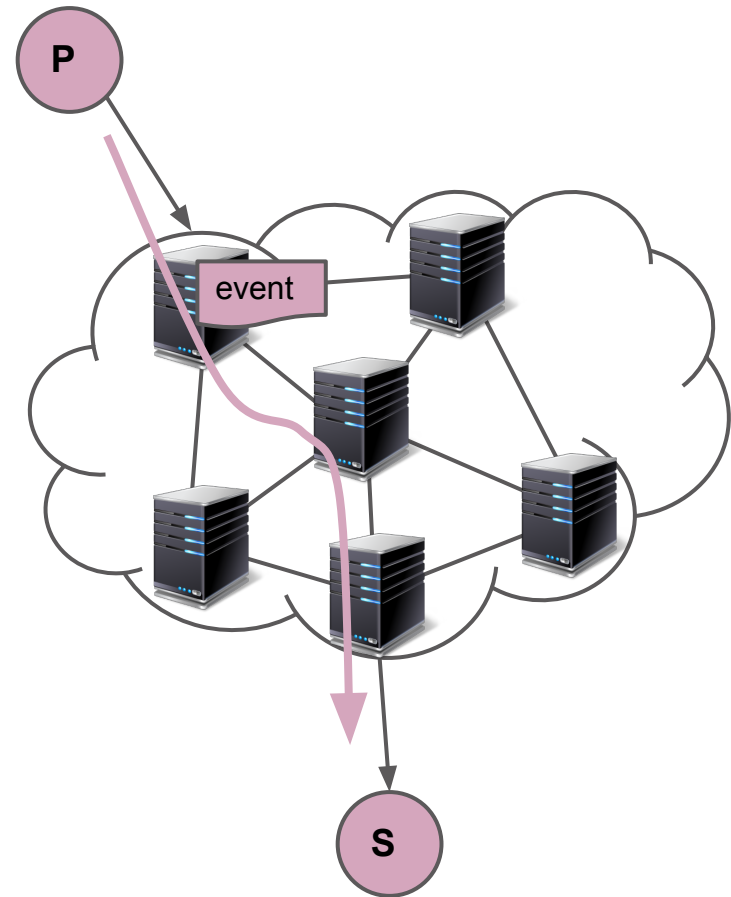
$r_1$ ,  $r_2$ ,  $r_3$  can be computed using reliability analysis for basic routing protocol.



# Retransmission + Multi-path Routing

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- Retransmission and multi-path routing can be combined.
- Use retransmission on the default forwarding path and opportunistic forwarding on alternate path.
- Event is not lost even when publisher and subscriber are disconnected.

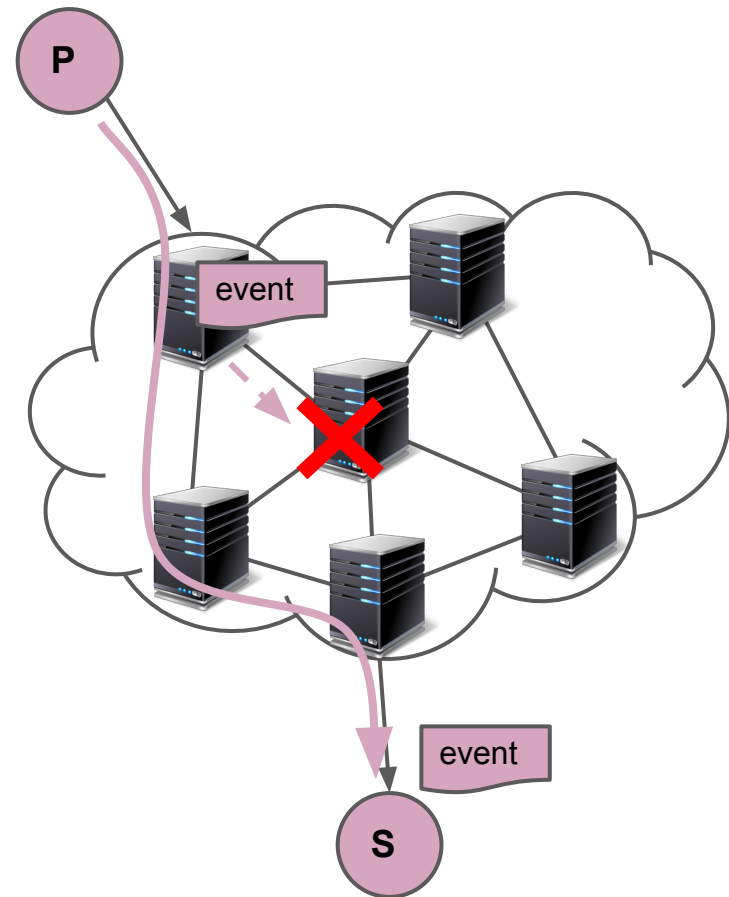




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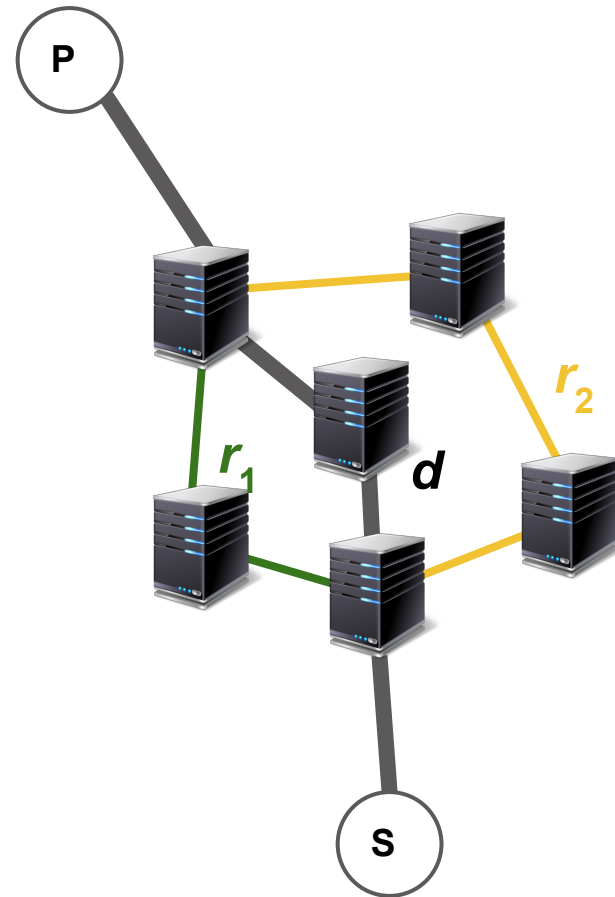
# Retransmission + Multi-path Routing (Cont.)

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$$r_{PS} = P[d < D] + P[d > D] \cdot (1 - (1 - r_1)(1 - r_2))$$

$P[d < D]$  can be computed using reliability analysis for retransmission protocol.

$r_1, r_2$  can be computed using reliability analysis for basic routing protocol.



# Outline

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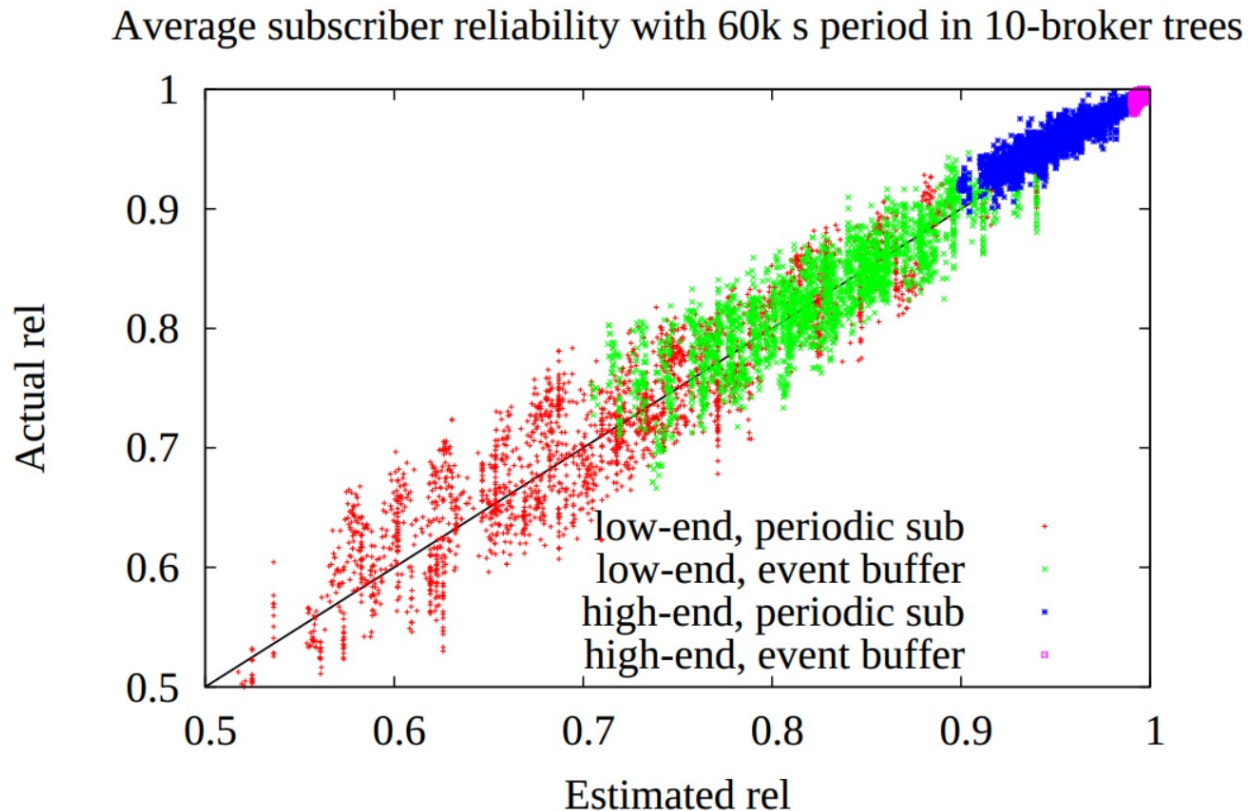
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# Evaluation Setting

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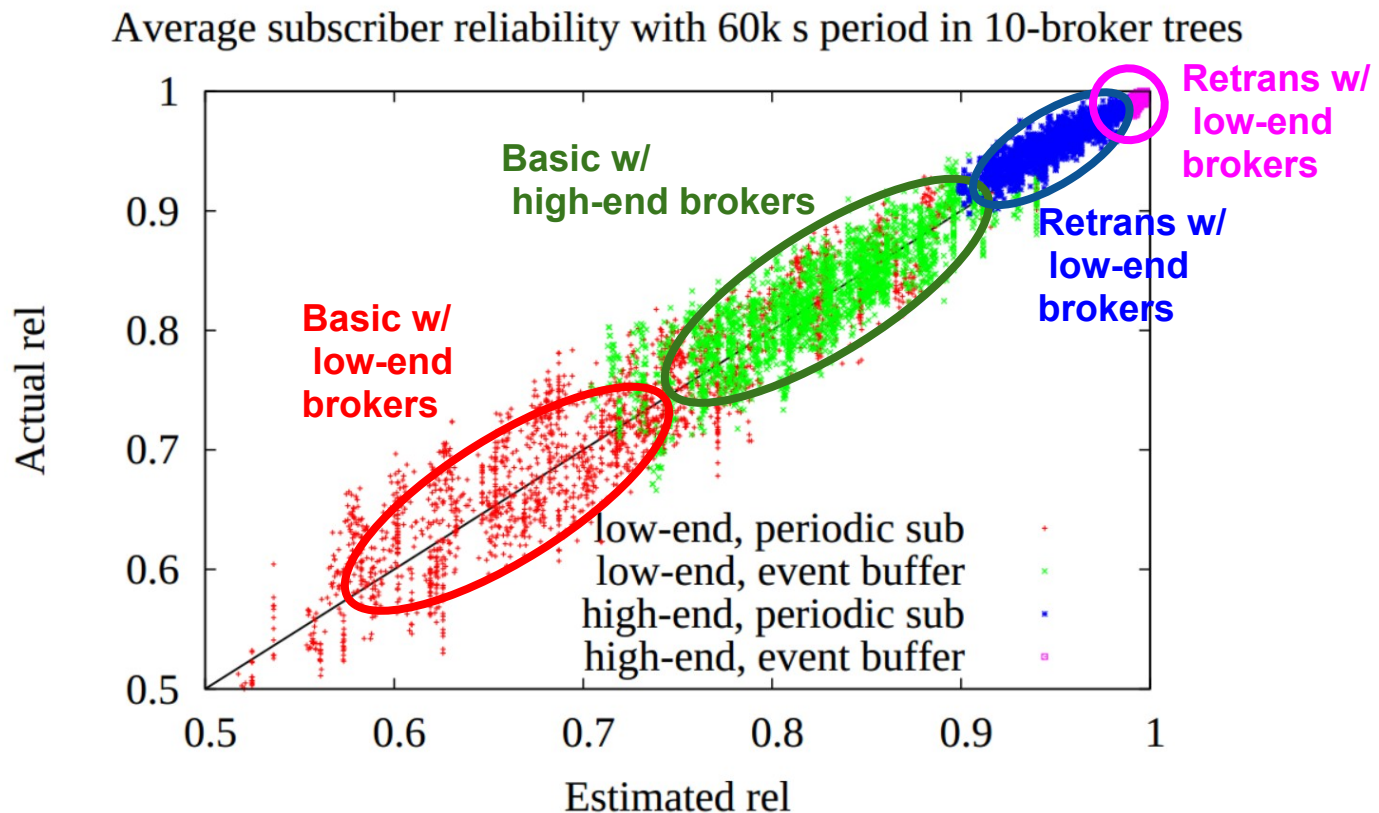
- NS-2 network simulator, simulating 10-broker networks.
  - Period (MTBF + MTTR) is set to 60k seconds (approximately 17 hours) for brokers and links.
  - Each link has availability set to 0.99 (hence  $MTBF = 0.99 * 17$  hours,  $MTTR = 0.01 * 17$  hours).
  - Two sets of brokers (observed from data traces).
    - Low-end brokers ([0.9, 0.95] availability range)
    - High-end brokers ([0.99, 0.999] availability range)
  - Event lifetime set to 3600 seconds (1 hour).
  - Four protocols (basic, retransmission, multi-path, retransmission + multi-path)
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# Results (Tree topology)



- Each dot in the graph represents one subscriber.

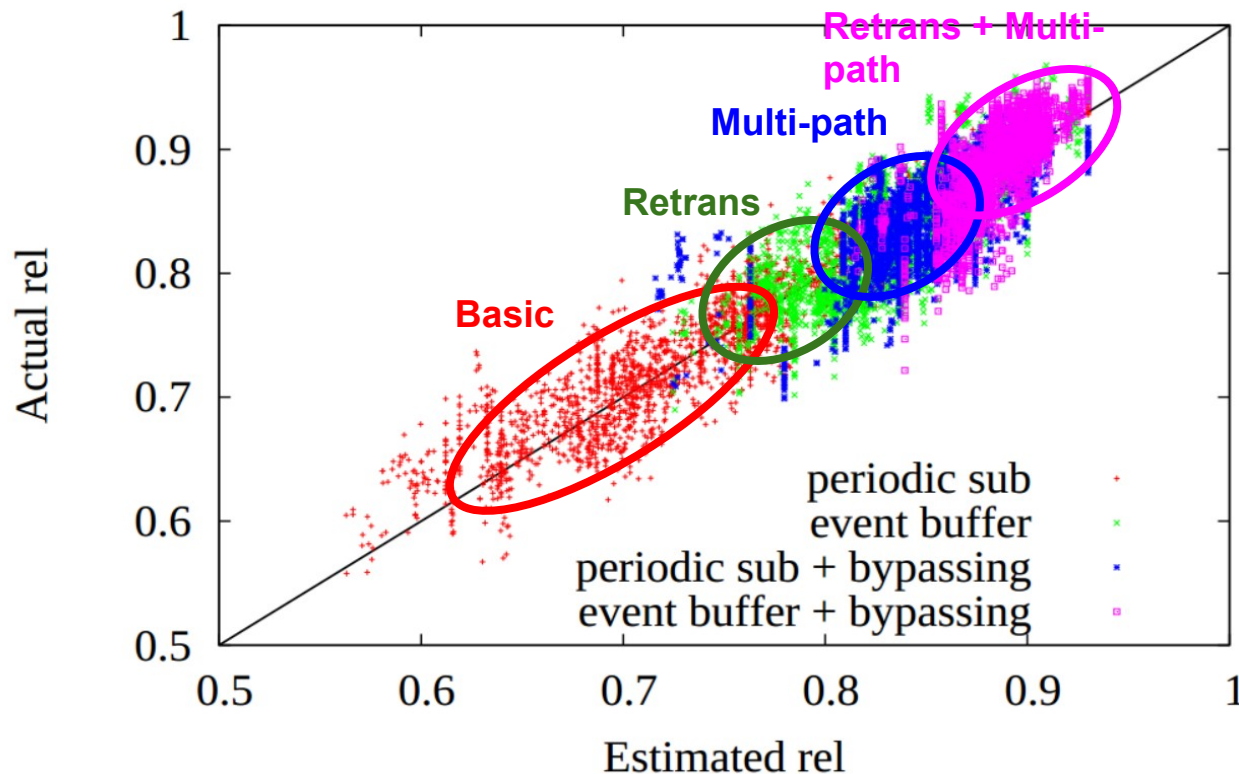
# Results (Tree topology)



- Each dot in the graph represents one subscriber.
- Retransmission protocol provides a magnitude of improvement over basic protocol.

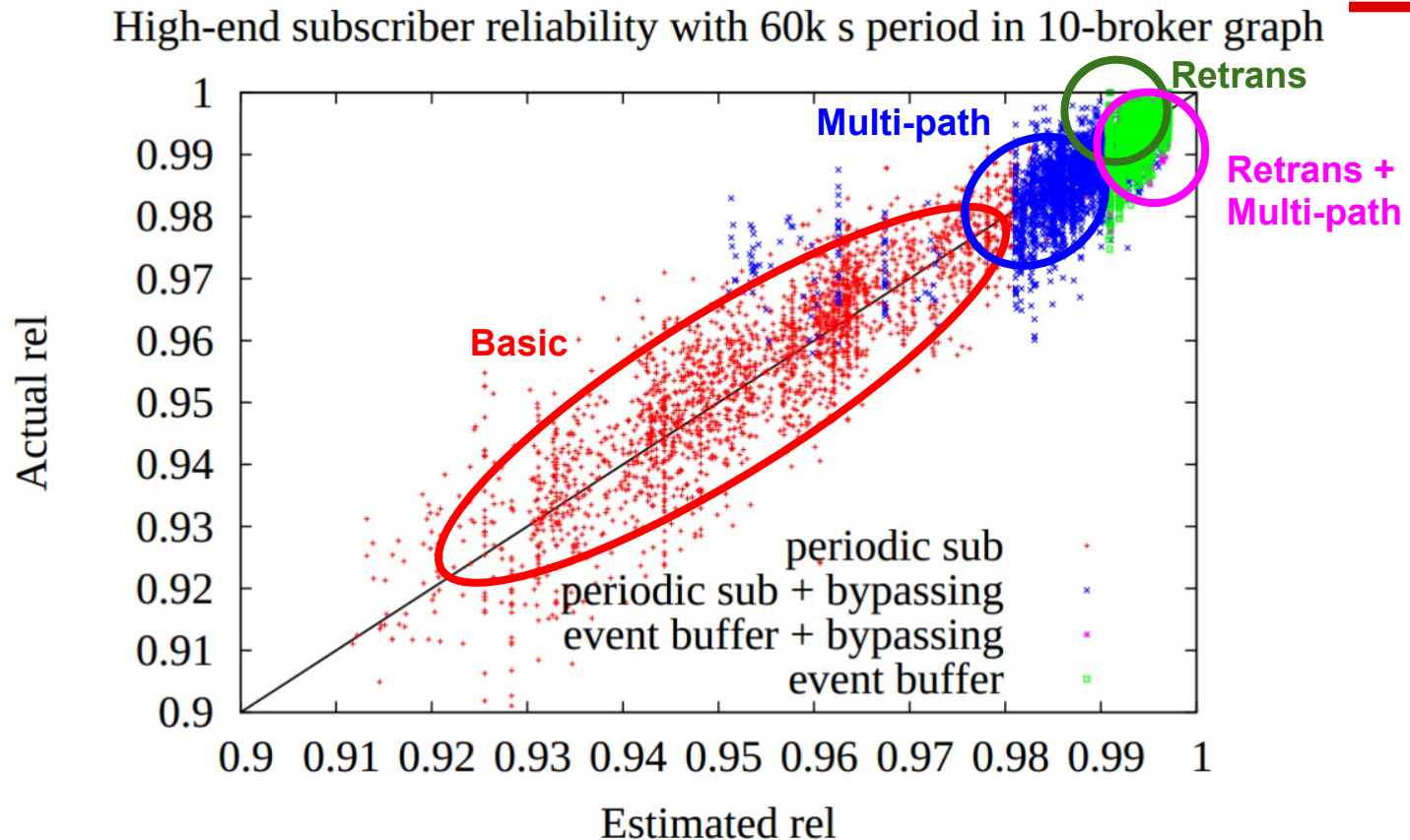
# Results (Random Low-end Broker Graph)

Low-end subscriber reliability with 60k s period in 10-broker graph



- Average node degree = 4
- **Basic routing** < **retransmission** < **multi-path** < **hybrid**

# Results (Random High-end Broker Graph)



- Retransmission protocol is better than multi-path routing.
- Combining retransmission with multi-path routing does not improve reliability very much.



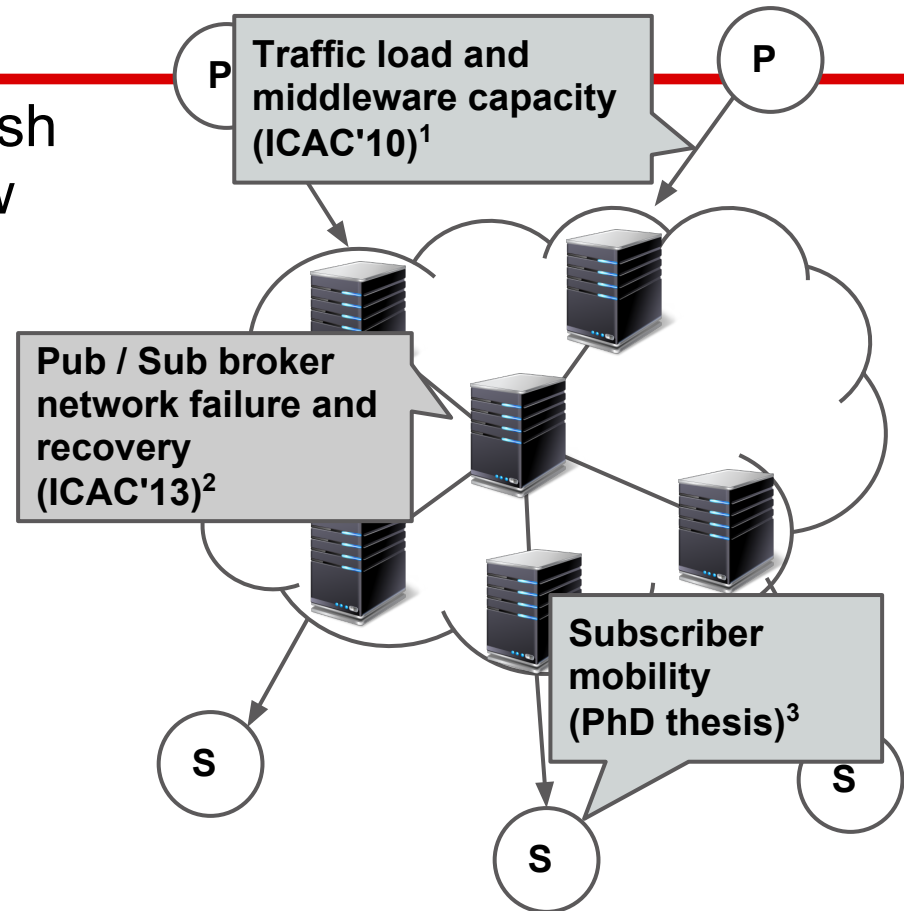
# Conclusions

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- Our work presents an analytical model to predict reliability and timeliness in distributed publish / subscribe systems that abstracts
    - broker / link failure and recovery
    - several commonly used fault tolerance schemes.
  - Evaluation results suggest that different fault tolerance schemes perform differently based on
    - Broker network quality
    - Event lifetime
    - Graph connectivity
  - The proposed analytical model can be used as a building block for
    - subscriber admission control
    - broker network planning
    - fault-tolerant publish / subscribe protocol selection
-

# Pub / Sub Performance Analysis

- Question : Given a publish / subscribe network, how to predict reliability / timeliness perceived by each subscriber ?
- Several factors affect subscriber's QoS.



<sup>1</sup>Pongthawornkamol et al, "Probabilistic QoS modeling for reliability/timeliness prediction in distributed content-based publish/subscribe systems over best-effort networks", ICAC 2010.

<sup>2</sup>Pongthawornkamol et al, "Reliability and Timeliness Analysis of Fault-tolerant Distributed Publish/Subscribe Systems", ICAC 2013.

<sup>3</sup>Pongthawornkamol et al, "Reliability and timeliness analysis of content-based publish/subscribe systems", Ph.D. Thesis.

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**Thank you !**

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